

# Planning for Embedded Systems: A Real-Time prospective

AZER BESTAVROS

Department of Computer Science  
Boston University

bestavros@cs.bu.edu

September 1991

**Abstract:** We investigate the problem of planning for embedded systems where issues of safety, liveness, and responsiveness are much more important than intelligence. We argue that in such systems, a planning agent should produce a *behavioral specification* that, when *superimposed* on running behaviors, preserves the properties critical to the mission of the system. In this respect, we propose the Time-constrained Reactive Automata (TRA) formalism [Best91b] for plan generation and verification.

**Keywords:** Embedded systems; Artificial intelligence; Automata theory; Modeling; Specification languages; Planning; TRA.

## 1 Introduction

Embedded computing systems are characterized by the rigidity of their performance and reliability requirements, which are dictated by the critical nature of their missions and the demanding and often hostile environments with which they interact.

A computing system is *embedded* if it is explicitly viewed as being a component of a larger system whose primary purpose is to monitor and control an "unintelligent" environment. Examples of such systems include ballistic-missile-defense systems, command and control systems, nuclear reactors, industrial process-control plants, robotics, space shuttle and aircraft avionics, aircraft collision avoidance systems, automotive control, switching circuits and telephony systems, data-acquisition systems, and real-time databases, just to name a few. The leaping advances in computing technologies witnessed in the last few decades have resulted in an explosion in the extent and variety of such systems. This trend is only likely to continue in the future.

Viewed simply, any embedded system has two parts: an *external interface* and a *programmed system*. The external interface consists of a number of devices such as sensors and actuators that interact with the environment. The programmed system collects information from the sensors and responds by producing actions to drive the actuators. The sustained demands of the external environment pose

relatively rigid and urgent requirements on the performance of the programmed system. These requirements are usually stated as constraints on the real-time behavior of the system. Wirth [Wirt77] singled out this processing-time dependency as the one aspect that differentiates embedded systems from other sequential and parallel systems.

The complexity of embedded systems coupled with the critical nature of their missions makes the importance of their safety, liveness and responsiveness unquestionable. On the other hand, the dynamic, unpredictable, and often hostile nature of their external environments dictates the incorporation of some level of intelligence to cope (*react*) with environmental changes or even to adopt new behaviors (*plan*) to insure missions success. Research in the real-time aspects of embedded systems has focussed on issues of specification, verification, analysis, languages, models and semantics [Stan88], whereas research in the intelligence aspects of these systems was geared towards planning, learning, knowledge representation and logic.

With research in real-time and intelligence aspects of embedded systems drifting apart, it has become evident that some kind of "common ground" is needed to make embedded systems both *intelligent* and *realistic*. Recently several attempts were made to achieve that goal. Most of these attempts were initiated by the AI research community in an effort to make planning applicable to embedded systems. Among these we cite: Brook's subsumption architecture [Broo86], Maes' situated agents [Maes90], Nilsson's action networks [Nils88], Lyons'  $\mathcal{RS}$  process algebra [Lyon90c, Lyon90a], Allens' formal temporal logic [Alle86, Pela88], and Rosenschein's situated-automata [Rose85]. One problem with most of these attempts is the way planning for embedded systems is perceived. Planners are considered an integral part of the tight (continuous) loop of sensing and acting on the environment. This led to the notion of reactive planning [Maes89], [Lyon91a] where plans are described as a selection algorithm between pre-compiled (or hardwired) behaviors based on the state of the environment. Although closer to reality than traditional planners, reactive planners fail in one or both of the following aspects. First, they do not allow for *derived* (creative or learned) behaviors. Sec-

ond, they deal with time as an afterthought making the verification of safety conditions (in the form of timing properties) much harder. As we mentioned earlier, this latter deficiency is unacceptable. In a way, customers would prefer an unintelligent safe system over an intelligent potentially unsafe one!

## 2 Levels of Reactive Control

We single out four levels of real-time control *Servo*, *Selective*, *Teleo-selective*, and *Intelligent*. One common aspect shared between these types of control is that, at any given point in time, a unique *reactive* behavior – certified to preserve the safety, liveness and responsiveness of the embedded system – is followed. This notion of continuous reactivity is crucial to embedded systems [Nils90].

A *servo control* system consists usually of a *unique behavior* that uses feedback to guarantee a tight coupling between its input and output signals. Designers of servo systems are often concerned with questions of stability, transient and steady state responses<sup>1</sup>, compensation, ... *etc.* Power steering is an example of a servo control system. It has one behavior, to keep the steering wheel (input) and the front wheels (output) tightly coupled.

Using *selective control*, a system’s behavior is selected from amongst a fixed number of competing behaviors based on stimuli from the external environment (world) in order to achieve a *unique goal*. Temperature control is an example of a reactive control system where either a cooling or heating behavior is selected depending on the ambient temperature. The cooling/heating behaviors might themselves be servo controlled. Examples of reactive control systems include Brooks’ subsumption architecture and Brockett’s Motion Description Language (MDL) [Broc88].

Using *teleo-selective* control, a system’s behavior is selected from amongst a fixed number of competing behaviors based on stimuli from the environment and motivations to achieve one of a *set of pre-determined goals*. Examples of teleo-selective systems include Nilsson’s action networks [Nils88], Maes’ situated agents [Maes90], and our earlier work using Input Output Timed Automata [Best90a, Best90c, Best90b].

In *intelligent* control, a system’s behavior is selected from amongst a number of fixed and superimposed *synthesized behaviors* based on stimuli from the environment and motivations to achieve a run-time goal. The process of synthesizing a behavior is carried out by a planning agent *outside* the sensing/acting loop based on a *perceived* model of the world and a set of goals to be achieved. Figure-1 shows the architecture of an intelligent control system.

The success of the planning process, which entails a safe progress towards achieving the planner’s goals, depends heavily on the existence of an accurate description of the behavior of the world. This can be achieved in two different ways. On the one hand, a cognition agent might be able, through observation

<sup>1</sup>For example overshoot, settling time, steady state errors.

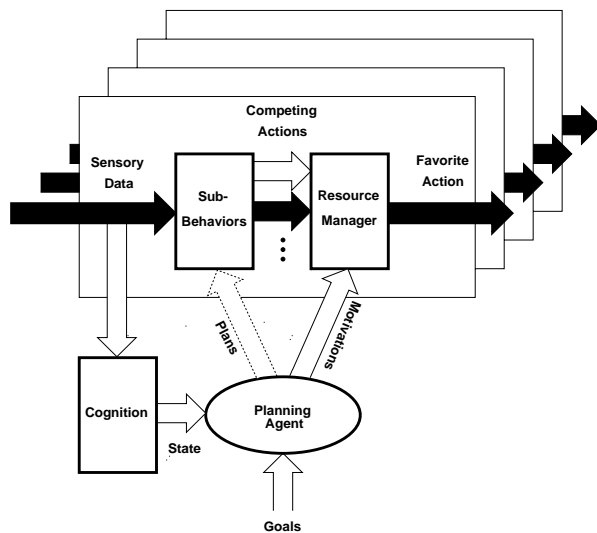


Figure 1: Intelligent control system architecture.

and learning, to provide the planning agent with a *perceived* behavioral specification of the world. The potential inaccuracy of this process – due, for example, to a rapidly changing environment – dictates that perceived world specifications be used only in conjunction with the plan synthesis process. On the other hand, the verification process can rely only on invariants about the world’s behaviors, which are asserted and guaranteed by the system designers. We call these assertions *hardcore specifications*.<sup>2</sup>

Most of the current research in real-time planning falls in the first three levels of control systems discussed earlier, where plans are pre-compiled (hardwired) into the sensing/acting loop. During run-time, the system is executing a pre-compiled plan. Recent attempts at building intelligent embedded systems [Kael86, Lyon91b, Lyon91a] are mostly concerned with the dynamic, unpredictable, and often hostile nature of the environment. The consideration of safety issues expressed as timing constraints has been minimal. This is primarily due to the lack of a computational model powerful enough to capture timing properties relevant to real-time specification and verification, and expressive enough to serve as a framework for planning. In the next section, we propose such a framework, namely the TRA model, to be used as a vehicle for planning in real-time systems. In particular, it is suitable as a formalism for the representation of actions as well as for verification purposes.

## 3 The TRA Model

For a complete treatment of the model, we refer the reader to [Best91a].

### 3.1 Novelties

The TRA model differs from others (like Hoare’s

<sup>2</sup>In embedded systems, it is usually assumed [Leve91] that an external mechanism is responsible for securing the safety of the system. Examples of such mechanisms include human intervention, using limit switches, ... *etc.*

CSP model [Hoar85], Reed and Roscoe’s timed CSP model [Reed88], Arbib and Lyons’  $\mathcal{RS}$  process-based model [Lyon89], and Baeten and Bergstra’s real-time process algebra [Baet91]) in that it does not allow the specification of systems that are not *reactive*. A system is reactive if it cannot block the occurrence of events not under its control. This property is crucial for accurate and realistic modeling of embedded and real-time systems. A sufficient condition to ensure that a model is reactive is the *input enabling* property proposed in [Lync88]. The TRA model is input enabled. It distinguishes clearly between environment-controlled actions, which cannot be restricted or constrained, and locally-controlled actions, which can be scheduled and disabled.

The TRA model is unique in that it admits the causal nature of physical processes. A system is *causal* if given two inputs that are identical up to any given point in time, there exist outputs (for the respective inputs) that are also identical up to the same point in time. The TRA model enforces causality by requiring that any locally-controlled actions be produced only as a *result* of an earlier *cause*.

*Spontaneity* is a notion closely related to causality. A system is *spontaneous* if its output actions at any given point in time  $t$  cannot depend on actions occurring at or after time  $t$ . In particular, if an output occurs simultaneously with (say) an input transition, the same output could have been produced without the simultaneous input transition [Sree90]. Simultaneity is, thus, a mere coincidence; the output event could have occurred spontaneously even if the input transition was delayed. The TRA model enforces spontaneity by requiring that simultaneously occurring events be independent; time has to *necessarily* advance to observe dependencies.

The TRA model distinguishes between two notions of time, namely *real* and *perceived*. Real time cannot be measured by any single process in a given system; it is only observable by the environment. Perceived time, on the other hand, can be specified using uncertain real time delays. The TRA model, therefore, does not provide for (or allow the specification of) any *global* or *perfect* clocks. As a consequence, the only measure of time available for system processes has to be relative to *imperfect, local* clocks. This distinction between real time and perceived time is important when dealing with embedded applications where specifications are usually given with respect to real time, but have to be implemented relying on perceived time.

### 3.2 Basic Definitions

An embedded system is viewed as a set of interacting automata called TRAs (Time-constrained Reactive Automata). TRAs communicate with each other through *channels* (see Figure-2). A channel is an abstraction for an *ideal* unidirectional communication. The information carried on a is called a *signal*, which consists of a sequence of *events*. An event underscores the instantiation of an *action* at a specific point in time. TRA channels have finite capacities, and the signals they carry are single valued; they cannot convey more than one event simultaneously.

Similar to [Alur90, Lewi90], we adopt a continuous model of time. We represent any point in time by a nonnegative real  $t \in \mathfrak{R}$ . Time intervals are defined by specifying their end-points which are drawn from the set of nonnegative rationals  $\mathcal{Q} \subset \mathfrak{R}$ . A time interval is viewed as a set over nonnegative real numbers. It can be an empty set, in which case it is denoted by  $\varepsilon$ , it can be a singleton set, in which case it is denoted by the  $[t, t]$ ,  $t \in \mathcal{Q}$ , or else it can be an infinite set, in which case it is denoted by  $[t_l, t_u]$ ,  $(t_l, t_u]$ ,  $[t_l, t_u)$ , or  $(t_l, t_u)$  – the closed, right-closed, left-closed, and open time intervals, respectively, where  $t_l, t_u \in \mathcal{Q}$  and  $t_l < t_u$ . The set of all such infinite time intervals is denoted by  $\mathcal{D}$ .

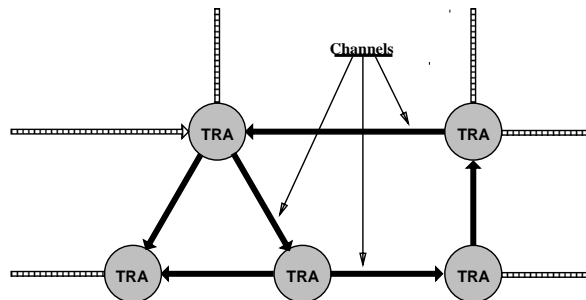


Figure 2: TRA objects and channels.

Figure-3 illustrates the notions of actions, events, and signals of a channel MOVE of some TRA. Let North, South, East, and West be the possible values that can be signaled on MOVE. MOVE(East) is, therefore, a possible action of the TRA. The instantiation of MOVE(East) at time  $t_1$  denotes the occurrence of an event  $\langle \text{MOVE}(\text{East}) : t_1 \rangle$ . The sequence  $\langle \text{MOVE}(\text{East}) : t_1 \rangle \langle \text{MOVE}(\text{North}) : t_2 \rangle \langle \text{MOVE}(\text{South}) : t_3 \rangle \dots \text{etc.}$  constitutes a signal.

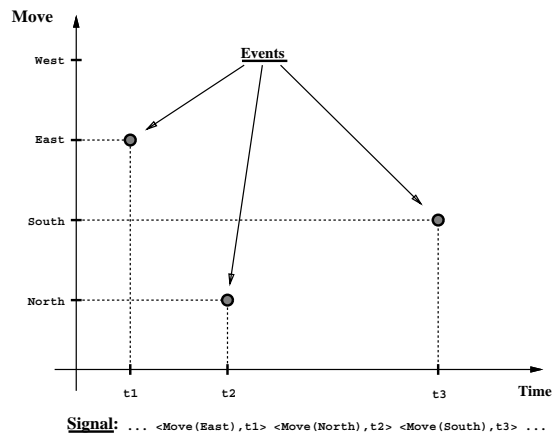


Figure 3: Signals, events, and actions.

At any point in time, a TRA is in a given *state*. The set of all such possible states defines the TRA’s *state space*. The state of a TRA is visible and can only be changed by local *computations*. Computations (and thus state transitions) are triggered by actions and might be required to meet specific timing constraints.

### 3.3 The TRA Object

Formally, a TRA object (see Figure-4) is a sextuple  $(\Sigma, \sigma_0, \Pi, \Theta, \Lambda, \Upsilon)$ , where

- $\Sigma$ , the TRA signature, is the set of all the channels of the TRA. It is partitioned into three disjoint sets of input, output, and internal channels. We denote these by  $\Sigma_{in}$ ,  $\Sigma_{out}$ , and  $\Sigma_{int}$ , respectively. The set consisting of both input and output channels is the set of external channels ( $\Sigma_{ext}$ ). These are the only channels visible from outside the TRA. The set consisting of both output and internal channels is the set of local channels ( $\Sigma_{loc}$ ). These are the locally controlled channels of the TRA.

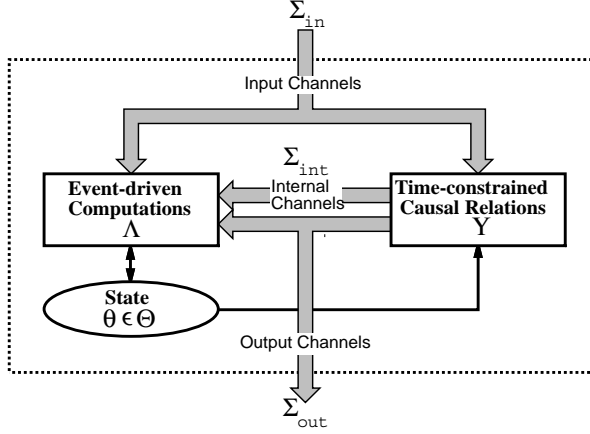


Figure 4: Basic components of a TRA object.

- $\sigma_0 \in \Sigma_{in}$  is the start channel.
- $\Pi$ , the signaling range function, maps each channel in  $\Sigma$  to a possibly infinite set of actions that can be signaled on that channel. Action sets of different channels are disjoint. The function  $\Pi$  naturally generalizes to sets of channels in the following manner:  $\Pi(\Sigma_i) = \bigcup_j \Pi(\sigma_{ij})$ , where  $\sigma_{ij} \in \Sigma_i$ . In particular, the set of all the TRA actions is given by:  $\Pi(\Sigma)$ . The set of input, output, internal, external, and local actions are similarly given by  $\Pi(\Sigma_{in})$ ,  $\Pi(\Sigma_{out})$ ,  $\Pi(\Sigma_{int})$ ,  $\Pi(\Sigma_{ext})$ , and  $\Pi(\Sigma_{loc})$ , respectively.
- $\Theta$  is a possibly infinite set of states of the TRA.
- $\Lambda \subseteq \Theta \times \Pi(\Sigma) \times \Theta$  is a set of possible computational steps of the TRA. TRAs are input enabled which means that for every  $\pi \in \Pi(\Sigma_{in})$ , and for every  $\theta \in \Theta$ , there exists at least one step  $(\theta, \pi, \theta') \in \Lambda$ , for some  $\theta' \in \Theta$ .
- $\Upsilon \subseteq \Sigma \times \Sigma_{loc} \times \mathcal{D} \times 2^\Theta$  is a set of time constraints on the operation of the TRA. A time constraint  $v_i \in \Upsilon$  is a quadruple  $(\sigma_i, \sigma'_i, \delta_i, \Theta_i)$  whose interpretation is that: if an action is signaled at time  $t \in \mathbb{R}$  on the channel  $\sigma_i$ , then an action should be fired on the channel  $\sigma'_i$  at time  $t'$ , where  $t' - t \in \delta_i$ , provided that the TRA does not enter any of the states in  $\Theta_i$  for the open interval  $(t, t')$ . The channel  $\sigma_i \in \Sigma$  is called the *trigger* of the time constraint, whereas  $\sigma'_i \in \Sigma_{loc}$

is called the *constrained* channel.  $\Theta_i \subseteq \Theta$  defines the set of states that disable the time constraint; once triggered a time constraint becomes and remains *active* until *satisfied* or *disabled*. A time constraint is satisfied by the firing of an action on the channel  $\sigma'_i$  within the imposed time bounds; it is disabled if the TRA enters in one of the disabling states in  $\Theta_i$  before it is satisfied (see Figure-5). The interval  $\delta_i$  specifies upper and lower bounds on the delay between the triggering and satisfaction (or disabling) of the time constraint  $v_i$ .

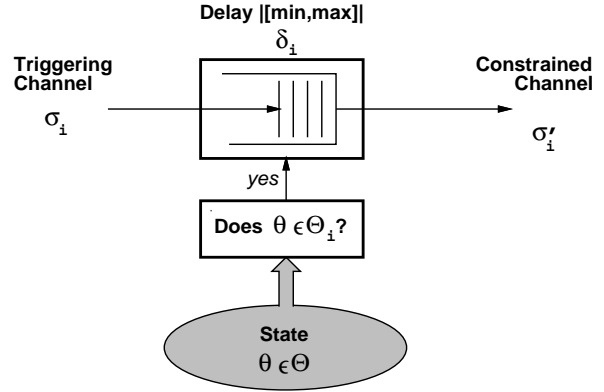


Figure 5: Time-constrained causal relationship.

As an example of a TRA specification, consider the the up/down counter whose state diagram is shown in Figure-6. The counter accepts commands issued on the input channel *cmd* to count up or down and signals the value of the current count (state) on the output channel *cnt*. The counter starts its operation once an action is fired on the *init* channel. The value of the *init* signal determines the starting state of the counter. The counter is constrained to produce a count every at least 1.9 and at most 2.1 units of time, once it starts execution. The formal TRA specification of the counter is shown in Figure-7.

### 3.4 The TRA Operational Semantics

In this section, we describe the rules governing the reaction of a TRA object to the events occurring on its input channels. Once these rules are specified, the possible behaviors of a given TRA can be determined.

In standard automata theory, there is no distinction between choosing a transition and firing it; both of them occur instantaneously. In the TRA model, a distinction is made whereby choosing (scheduling) a transition and executing (committing) that transition are not necessarily instantaneous activities. They are “distinct” in that they may be separated in time. As a matter of fact, a scheduled transition does not necessarily have to be committed; it can be abandoned due to unforeseeable conditions. The distinction between the two activities is also pronounced in the way the TRA model differentiates between input and local events. Input events are uncontrollable; they are not scheduled. Local events are.

The *state* of a TRA at an arbitrary point in time is not sufficient to construct its *future behavior*. To

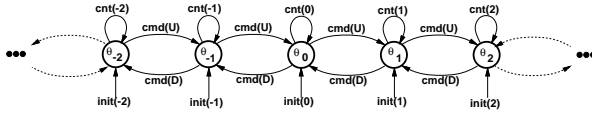


Figure 6: State diagram of up/down counter.

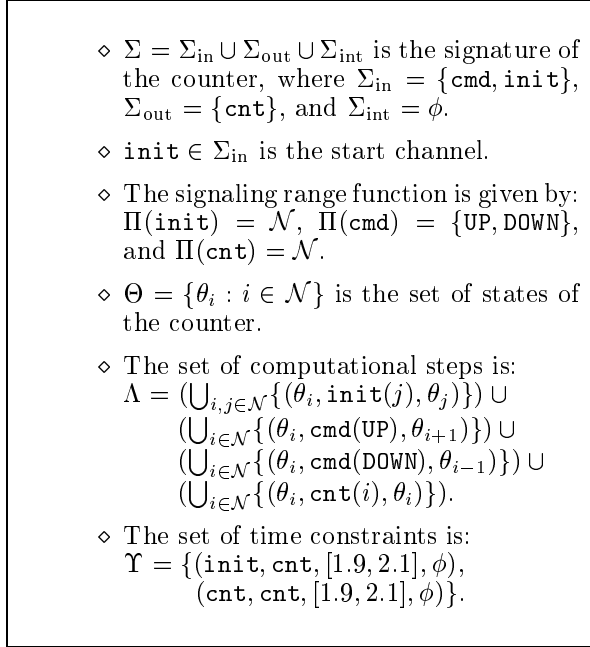


Figure 7: TRA-specification of up/down counter.

explain why this is true consider the example shown in Figure-8, where a TRA is known to be in some state  $s$  at time  $t_1$ . Assume that, due to a triggering event at some earlier time  $t_0$ , an action is scheduled to fire at some point in a future interval given by  $[t_0 + t_{l_0}, t_0 + t_{h_1}]$ . Knowing only the state of the TRA at time  $t_1$  is obviously not sufficient to predict future behaviors. In addition to the state, the intervals of time where scheduled transitions might fire have to be recorded. We encapsulate this knowledge in our notion of *intentions*.

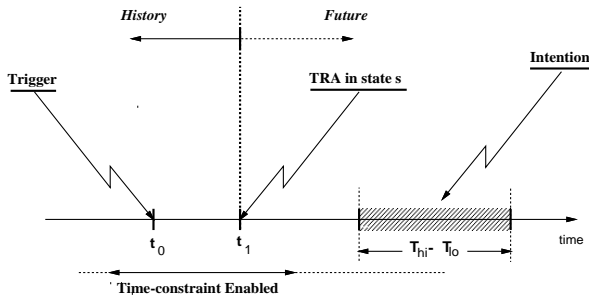


Figure 8: The notion of a TRA status.

Let  $v_i = (\sigma_i, \sigma'_i, \delta_i, \Theta_i) \in \Upsilon$  be a time constraint. As we explained before,  $v_i$  identifies a time-constrained causal relationship between the events signaled on  $\sigma_i$  and those signaled on  $\sigma'_i$ . In particular, the occurrence of a triggering event on  $\sigma_i$  results in an intention to perform an action on  $\sigma'_i$

within the time frame imposed by  $\delta_i$ . At any given point in time, a TRA might have several such outstanding intentions. We define the *intention vector*  $I = \vec{\Delta}$  to be a vector of  $r$  sets of intentions, where  $r = |\Upsilon|$ . Each entry in  $I$  is associated with one of the TRA's time constraints. In particular, if  $v_i = (\sigma_i, \sigma'_i, \delta_i, \Theta_i) \in \Upsilon$  is one of the TRA's time constraints, then  $I[v_i] = \{\delta_{i1}, \delta_{i2}, \dots, \delta_{ik}, \dots, \delta_{im}\}$  denotes a set of  $m$  time intervals during which actions on the channel  $\sigma'_i$  are intended to be fired as a result of earlier triggers on  $\sigma_i$ . Each one of the intervals in  $\Delta_i$  can be thought of as an independent *activation* of the time constraint  $v_i$ . An empty intentions set,  $I[v_i] = \phi$ , indicates the absence of any activations of  $v_i$ . The empty intention vector,  $I_\phi$ , consists of  $r$  such empty sets.

At any point in time, the intention vector of a TRA can be thought of as extending the TRA's state. This is captured in our notion of a TRA status.

**Definition 1** We define the status of a TRA  $(\Sigma, \sigma_0, \Pi, \Theta, \Lambda, \Upsilon)$  at any point in time  $t \in \mathbb{R}$  to be the tuple  $(\theta, I)$ , where  $\theta \in \Theta$  and  $I$  are the TRA's state and intention vector at time  $t$ , respectively.

A TRA changes its status only as a response to the occurrence of an input or an intended local event. Five conditions have to be met for a status transition to take place. We informally present these conditions in the following definition. For a formal treatment refer to [Best91b].

**Definition 2** Assume that the status  $(\theta, I)$  of a TRA was entered at time  $t$  as a result of an event  $\langle \pi : t \rangle$ , where  $\pi \in \Pi(\sigma_j)$ ,  $\sigma'_j \in \Sigma$ . Furthermore, assume that at time  $t'$  ( $t' \geq t$ ), an action  $\pi' \in \Pi(\sigma'_j)$  is fired, where  $\sigma'_j \in \Sigma$ . As a result, the TRA will assume a new status  $(\theta', I')$ . The status  $(\theta', I')$  is called a successor of the status  $(\theta, I)$  due to the event  $\langle \pi' : t' \rangle$ , if and only if the following conditions hold:

1. Legality:  $(\theta, \pi', \theta') \in \Lambda$ .
2. Spontaneity:  $t' = t$  only if  $\pi$  and  $\pi'$  are independent and occur in different components.<sup>3</sup>
3. Safety: None of the intentions in  $I$  expired at time  $t'$ .
4. Causality: If  $\sigma'_j \in \Sigma_{\text{loc}}$ , then there exists an intention in  $I$  to perform an action on  $\sigma'_j$  and  $t'$  is a possible time to commit that intention.
5. Consistency: The intentions in  $I$  continue to exist in  $I'$  unless otherwise dictated by the occurrence of the event  $\langle \pi' : t' \rangle$ .

<sup>3</sup>TRA components represent a weak notion of spacial locality. For a formal treatment, we refer the reader to [Best91b].

We use the notation  $(\theta, I) \xrightarrow{\langle \pi' : t' \rangle} (\theta', I')$  to denote the *direct status succession* from  $(\theta, I)$  to  $(\theta', I')$  due to the firing of the event  $\langle \pi' : t' \rangle$ . Furthermore, we use the notation  $(\theta, I) \xrightarrow{\alpha} (\theta', I')$  to denote the *extended status succession* from  $(\theta, I)$  to  $(\theta', I')$  due to the firing of the sequence of events  $\alpha$ .

A TRA is said to have reached a *stable status*  $(\hat{\theta}, \hat{I})$ , if all entries of the intention vector are empty sets. That is  $\hat{I} = I_\phi$ . Obviously, a TRA will remain in a stable status until it is excited by an external input event. This follows directly from the causality requirement for a status succession.

To start executing, a TRA  $(\Sigma, \sigma_0, \Pi, \Theta, \Lambda, \Upsilon)$  is put in a stable status  $(\theta_0, I_0)$ , where  $I_0 = I_\phi$  and  $\theta_0 \in \Theta$ . The status  $(\theta_0, I_0)$  is called an *initial status*. The execution is initiated at time  $t_0$  with the firing of an action  $\pi_0$  on the start channel  $\sigma_0$ , where  $\pi_0 \in \Pi(\sigma_0)$ . The event  $\langle \pi_0 : t_0 \rangle$  is called the *initiating event*.

An *execution* of a TRA is a possibly infinite string of alternating statuses and events that starts with an initial status and an initiating event. A *schedule*  $\alpha$  of an execution  $e$  is the sequence consisting of *all* the events appearing in  $e$ . Since internal events are invisible from outside a TRA, we will often be interested only in external events. We define  $\beta$  to be a *behavior* of a TRA  $\mathcal{A}$ , if it consists of all the *external* events appearing in some schedule  $\alpha$  of  $\mathcal{A}$ . We denote the set of all possible behaviors of  $\mathcal{A}$  by  $behs(\mathcal{A})$ . Obviously,  $behs(\mathcal{A})$  describes all the possible interactions that  $\mathcal{A}$  might be engaged in, and, therefore, constitutes a specification of the system that  $\mathcal{A}$  models.

A TRA  $\mathcal{A}$  is said to *implement* another TRA  $\mathcal{B}$  if  $\mathcal{A}$  does not produce any behavior that  $\mathcal{B}$  could have produced [Lync88]. In other words, all of  $\mathcal{A}$ 's behaviors (the implementation) are possible behaviors of  $\mathcal{B}$  (the specification). The reverse, however, is not true. There might exist behaviors of  $\mathcal{B}$  that cannot be generated by  $\mathcal{A}$ . The notion of a TRA implementing another is used mainly in verification [Best91a].

### 3.5 TRA Composition Operation

The composition of a countable collection of *compatible* TRAs,  $\{\mathcal{A}_i : i \in \mathcal{I}\}$ , is a new TRA  $\mathcal{A} = \mathcal{A}_0 \times \mathcal{A}_1 \times \dots \times \mathcal{A}_i \times \dots = \prod_{i \in \mathcal{I}} \mathcal{A}_i$ . The execution of  $\mathcal{A}$  involves the execution of all its components  $\mathcal{A}_{i \in \mathcal{I}}$ , each starting from an initial status and observing every external event signaled by either the environment (input) or by any TRA in the collection  $\{\mathcal{A}_i : i \in \mathcal{I}\}$ . The *compatibility* condition for composition insures that, for each channel in the composition, there is at most one writer, a finite number of readers, and that the signaling ranges of readers and writers are compatible to preserve the input enabled property.

The input signature of the composition  $\mathcal{A}$  consists of those channels that are inputs to one or more of the component TRAs, and which are not outputs of any of the component TRAs. The output signature of the composed TRA consists of all the outputs of all the component TRAs. Similarly, the internal signature of the composed TRA consists of all the internal channels of all the component TRAs. The start channel of the composed TRA is the start channel of

one or more of its component TRAs.<sup>4</sup> The signaling range function of the composed TRA is defined so as to preserve its input-enabled property. In particular, the signaling range of an input channel consists of only those actions that can be accepted by all readers of that channel. A computational step of the composed TRA is necessarily a step of one of its components. Similarly the time-constrained causal relationships of the composed TRA are exactly those of the component TRAs. The formal definition for the composition operation can be found in [Best91b].

The TRA composition operation is more general than those reported in [Lync88, Tutt88, Best90a] in that it allows the specification of both *parallel* and *sequential* composition. In particular, the introduction of the *start channel* permits the execution of two TRAs to be concurrent if they share the same start channel, or to be serialized if the start channel of one (child) is an output of the other (parent). Through appropriate composition, our model is capable of representing all of the composition operations in [Lyon89, Lyon90b].

### 3.6 CLEOPATRA

CLEOPATRA<sup>5</sup> is a convenient language for the specification of embedded systems under the TRA formalism. CLEOPATRA specifications are executable and can be transformed, mechanically and unambiguously, into formal TRA objects for verification purposes [Best91b]. Throughout this paper, we will use CLEOPATRA to specify reactive behaviors.

In CLEOPATRA, systems are specified as interconnections of TRA objects. Each TRA object has a set of *state variables* and a set of *channels*. Time-constrained causal relationships between events occurring on the different channels, and the computations (state transitions) that they trigger, are specified using *Time-constrained Event-driven Transactions*. The behavior of a TRA object is described using TETs. TRA objects can be composed together to specify more complex TRAs.

In CLEOPATRA, TRAs are defined in *classes*. For example, Figure-9 shows the CLEOPATRA specification of the class of integrators that use trapezoidal approximation.

An integrator from the `integrate` TRA-class has two parameters, namely `TICK` and `TICK_ERROR`. Its signature consists of an input channel `in`, and an output channel `out`. Both `in` and `out` carry actions whose values are drawn from the set of reals. The body of `integrate` specifies a state space consisting of three real state variables `x0`, `x1` and `y`. It specifies two TETs. The first specifies that the response to an action on the input channel `in` is to store its value in state variable `x1`. The second specifies a transaction that is triggered initially by the `init` signal, and subsequently with every firing of `out`. After an amount of time bounded by a delay of `TICK ± TICK_ERROR` from when the transaction is triggered, an action of value `y` is signaled on `out`, and a state transition that

<sup>4</sup>Without loss of generality, we assume that TRA to be  $\mathcal{A}_0$ .

<sup>5</sup>A C-based Language for the Event-driven Object-oriented Prototyping of Asynchronous Time-constrained Reactive Automata.

```

TRA-class integrate(double TICK, TICK_ERROR)
  in(double) -> out(double)
{
  state:
  double x0 = 0, x1 = 0, y = 0;
  act:
  in(x1) -> :
  ;
  init(),out() -> out(y):
  within [TICK-TICK_ERROR~TICK+TICK_ERROR]
  commit { y=y+TICK*(x0+x1)/2; x0 = x1;}
}

```

Figure 9: Specification of the `integrate` class.

updates the value of the state variable `y` and `x0` is committed.

## 4 TRA-based Specification

The TRA model and the *CLEOPATRA* language are ideal for specifying reactive behaviors of embedded systems. In this section we overview our experience in specifying basic, subsuming, and competing reactive behaviors, which correpond respectively to the servo, selective, teleo-selective classes of control systems that we discussed earlier.

In modeling embedded systems, it is important that basic resources (e.g. actuators and sensors) be included in the system specification. The TRA framework has proven to be appropriate for representing the behavior of such low level controls. In particular, we used it to specify and simulate position and velocity feedback linear and non-linear control systems, as well as complex asynchronous digital circuits and systems [Best91b].

For reactive behaviors at a higher level, Rodney Brooks [Broo87] proposes the *subsumption architecture* as a methodology for specifying and building complex control systems. This architecture suggests the use of a vertical decomposition of the control system into a number of parallel independent task-achieving behaviors organized in a hierarchy of *dominant* and *inferior* behaviors. The subsumption architecture can be supported easily and effectively using the TRA model. In [Best91b], we showed that the TRA model is more general than the subsumption architecture. In particular, using the `subsume` TRA-class shown in Figure-10, dominant and inferior behaviors can be patched together to describe a complex behavior.

The subsumption architecture is suitable for the specification of task-achieving behaviors that can be *statically* organized as a hierarchy of dominant and inferior behaviors. It cannot deal with applications with *dynamically* changing priorities. In particular, if the priority of a behavior depends on the task (or goal) to be achieved, and if such a goal is dynamically changing, then this behaviour can be dominant in some situations and inferior in others. Rather than dominant and inferior behaviors, such systems are described in terms of *competing behaviors*.

```

typedef enum{0,1,X} tristate;

TRA-class subsume(double DELAY)
  dominant(tristate),inferior(tristate)
  -> behavior(tristate)
{
  state:
  tristate d_val = X, i_val = X ;
  act:
  dominant(d_val) -> behavior(d_val):
  before DELAY
  unless(d_val == X && i_val != X)
  commit { i_val = X ; }
  inferior(i_val) -> behavior(i_val):
  before DELAY
  unless(d_val != X)
  ;
}

```

Figure 10: The subsumption TRA in *CLEOPATRA*

The TRA framework is ideal for the specification of systems with competing behaviors. Examples of TRA behavioral specification of such systems were given in [Best90a]. The use of the TRA model in the specification and simulation of these systems is similar to Nilsson's action networks [Nils88], and Maes' situated agents [Maes90]. TRA specifications, however, allow (potentially automated) analysis to be performed on behaviors. For instance, given a finite-state TRA description, it is possible to obtain a finite-state description of all of its possible behaviors, and thus, proving assertions about these behaviors. This can be done using techniques similar to those suggested in [Lewi89, Alur90]. In addition, the TRA model provides a vehicle for efficient simulation and implementation using *CLEOPATRA*. Silicon compilation of *CLEOPATRA* specifications for simple behaviors is also a possibility [Frie91].

As an example of TRA-specification of competing behaviors, consider the specification of *Buggy*, a bug-like autonomous creature. Buggy has two actuators to move in 2-D and two noisy sensors to locate predators, and detect floor cracks in a limited neighborhood. Buggy has two potentially competing behaviors, searching for food along cracks, and keeping itself away from predators (or obstacles). Buggy has only one goal: to survive (i.e. avoid starvation and predators). Buggy's urge to find food increases as time elapses and no food is found. Its fear from predators increases as its distance from them decreases. Dynamically, the behavior that is more important to Buggy's survival subsumes the other.

Buggy's competing behaviors were specified using *CLEOPATRA*. Figure-11 shows one of Buggy's simulated behaviors in a room with two cracks and a predator going in a circle. In this behavior one can identify some of Buggy's basic behaviors. In particular, when Buggy's sensors fail to detect any cracks or obstacles in its immediate neighborhood, Buggy's behavior is to *wander* randomly until the sensors return some readings. The pace of this wandering behavior (speed and rate of direction change) depends on the state of Buggy – its hunger and fear levels. Other basic behaviors of Buggy include approaching a crack, following a crack, and running away from ob-

stacles. In addition to the basic behaviors of Buggy, one can also identify a number of *emergent behaviors*. An emergent behavior is not specified explicitly; it emerges from the composition of other basic behaviors. For example, in Figure-11, two behavioral patterns can be easily singled out. The first is a hesitant behavior, in which, driven by hunger and fear, Buggy switches back and forth between approaching a crack to find food and running away from it to escape from the nearby rotating predator. The second is a routine behavior, in which Buggy reaches a limit-cycle of approaching a crack, following it, and running away from it.

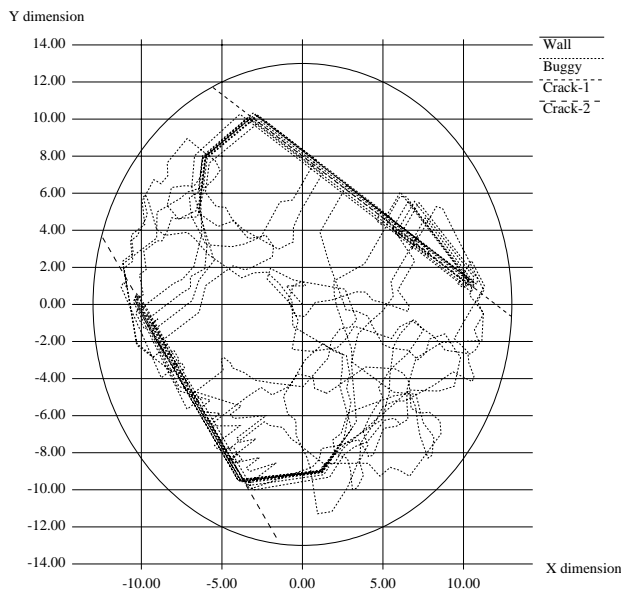


Figure 11: Basic and emergent behaviors of Buggy.

## 5 TRA-based Planning

As we argued earlier, planning in embedded systems entails synthesizing reactive behaviors that, when composed with existing behaviors (including the perceived behavior of the world), would result in the state of the world *potentially* progressing towards the satisfaction of a given set of goals – while *always* preserving system safety. We emphasize the word “potentially” because, synthesized behaviors are generated based on a perceived state of the world that might be inaccurate or dynamically changing. Also, we emphasize the word “always” because, as we explained earlier, the safety of an embedded system is far more important than its intelligence.

### 5.1 A simple planning example

Consider the robot *Sneaky*, who is assigned the task of going into a high security room. A security alarm sounds if the room’s door is left open for more than a given amount of time. Also, an alarm will be signaled if a password is not correctly input within a given

time frame after walking into the room. Figure-12 shows a partial *CLEOPATRA* specification of the perceived environment and the basic behaviors of the robot. The goal of the planner is to synthesize a behavior that when composed with the world’s specification would result in Sneaky being in the room. Figure-13 shows a partial specification of such a behavior. The safety of the system requires that the security alarm does not go off at any time (because of Sneaky). This can be formally proved by composing the TRAs representing Sneaky’s behavior and the environment’s specification, and showing that starting from an initially safe state, the composition cannot reach a state where the alarm goes off.

### 5.2 Planning through learning

The architecture we proposed in figure 1 decouples the planning agent from the tight loop between the embedded system and its environment. In a way, this architecture allows the agent to perform explicit reasoning at execution time without interfering with the system’s reactive and timely behavior. Another advantage of such an architecture is that it allows the planning agent to modify a synthesized behavior based on its performance.

To exemplify this notion of planning by learning from experience, consider the simulated behavior of *Buggy* shown in Figure-11. A planning agent observing such a behavior will notice the reoccurrence of a limit cycle in which Buggy discovers food on a crack, eats it while moving along the crack and, after a while, realizing it became very close to an obstacle leaves that path to get away from the wall. Eventually, however, it becomes hungry again, and goes back to the crack repeating almost exactly the same path. On other occasions, however, Buggy loses the crack and starts a random wandering phase away from the crack where there is no food, and thus,

becomes threatened with starvation. A planning agent can benefit from observing such a behavior in a number of different ways. For example, by realizing that Buggy never starves when locked in a limit cycle, it might develop a subsuming *routine behavior* that makes it go blindly in that triangular limit cycle, once it finds one.

Similar potentials for learning from reactive behaviors were explored in [Maes89] where an autonomous mobile robot learned how to coordinate the use of its actuators to move forward. This work is limited in that the notion of “what to learn” is defined and static throughout the life-span of the creature – namely, coordination. In other words, rather than learning a “new” behavior, the creature is merely perfecting an existing behavior.

## 6 Conclusion

In this paper, instead of trying to adapt planning to real-time systems, we followed the alternative approach of redefining planning in a way acceptable to the real-time research community. In other words, instead of making intelligent systems real, we try to fit intelligence in real systems. This seems to be



```

GrabKnob -> :
  within [2~5]
  commit { Grabbing = TRUE ; }
ReleaseKnob -> :
  within [2~5]
  commit { Grabbing = FALSE ; }
Turn -> OpenDoor:
  unless (!Grabbing)
  within [40~50]
  commit { DoorOpen = TRUE ; }
OpenDoor -> Alarm:
  unless (ValidPasswd)
  within [40~50]
  commit { AlarmSet = TRUE ; }
OpenDoor -> Alarm:
  unless (!DoorOpen)
  within [100~110]
  commit { AlarmSet = TRUE ; }
MoveIn -> :
  unless (Grabbing || !DoorOpen)
  within [20~30]
  commit { RobotIn = TRUE ; }
EnterPasswd -> :
  unless (!RobotIn)
  within [5~8]
  commit { ValidPasswd = TRUE ; }
PressButton -> CloseDoor:
  unless (!RobotIn)
  within [40~50]
  commit { DoorOpen = FALSE ; }

```

Figure 12: Partial world model for Sneaky.

```

Init -> GrabKnob:
  within [1~2] ;
GrabKnob -> Turn:
  within [6~7] ;
Turn -> ReleaseKnob:
  within [60~60] ;
ReleaseKnob -> MoveIn:
  within [6~7] ;
MoveIn -> EnterPasswd:
  within [35~40] ;
MoveIn -> PressButton:
  within [35~80] ;

```

Figure 13: Partial synthesized plan for Sneaky.

the only viable approach especially in critical applications where lives and expensive machinery are at stake. We believe that for such systems, planning agents should produce *behavioral specifications* that, when *superimposed* on running behaviors, preserve the properties critical to the mission of the system. In this respect, we propose the TRA model as a framework for real-time plan generation and verification.

The TRA model is ideal for specifying reactive behaviors for embedded systems. On the one hand, its input enabled nature allows the specification of task-achieving behaviors in a realistic manner. On the other hand, its formal capabilities and compositional nature make possible the analysis and verification of safety conditions within a given environment. We have developed a specification language *CLEOPATRA* based on the TRA model. Behavioral specifications written in *CLEOPATRA* can be compiled and executed efficiently for simulation purposes.

Our experimentation with the TRA model as a backbone for building *intelligent control systems* is ongoing. In particular, we are working on an ex-

periment that involves the management of sensorimotor activities for a robotics application that includes manipulative and active vision tasks executed in a dynamic environment. Our experiment involves research in three different areas: real-time systems, software engineering, and artificial intelligence. The use of the TRA framework provides the necessary link between all three areas. It offers formal verification and analysis capabilities to guarantee real-time properties. It offers an expressive executable specification language to validate customers needs, and defines clear interfaces between the different system components. It offers a formalism suitable for the specification and generation of reactive tasks.

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