

# Boston University

## CAS CS 640: AI

Lecture on  
Introduction to Computer Vision

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October 10, 2024

# Learning Objectives for this Lecture



Computer Science

- ❑ Understand formats of images used as inputs to AI models: greyscale, color, medical scans
- ❑ Understand differences and similarities between pre-2012 “traditional computer vision” and post-2012 neural-network-based computer vision & see examples
- ❑ Understand why convolution is powerful
- ❑ Understand the connection between convolution and correlation
- ❑ Understand template matching with image pyramids
- ❑ Understand CNNs as a learning hierarchy of features

# What is a digital image?



Computer Science

- ❑ Digital images are fields of colored dots
- ❑ Each dot is called a  
pixel = picture cell
- ❑ In the medical domain, a pixel can be a  
voxel = volumetric cell

# Image Processing



Computer Science

- ❑ The engineering field of image processing proceeds computer vision by decades.
- ❑ Goal: Restore noisy images or send encoded image through a channel

# Image Processing



Computer Science

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- ❑ Standard test image

Lena Soderberg '72



# Image Processing



Computer Science

- ❑ The engineering field of image processing proceeds computer vision by decades.
- ❑ Goal: Restore noisy images or send encoded image through a channel
- ❑ Standard test image with detail, shading, texture, sharp & blurry regions:  
Lena Soderberg '72  
controversy!





# Color Models



Computer Science

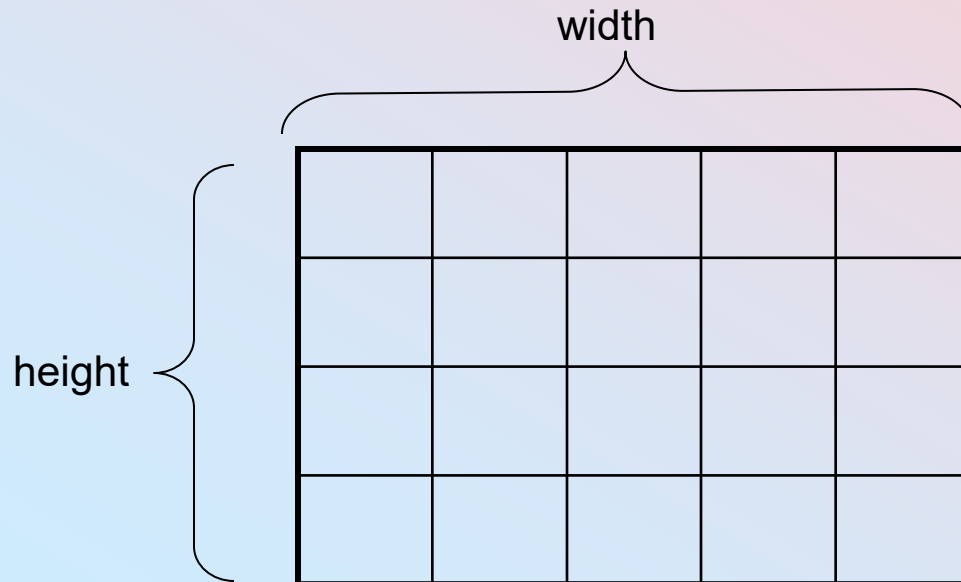
- ❑ Images can be gray scale, color, or color with an alpha (transparency) channel (used in graphics for overlaying images)
- ❑ Most common color representation is RGB (Red, Green, Blue)
- ❑ Other models include CMYK (used for print) and YUV (often used for input from cameras, compression, and transmission)

# What is an image?



Computer Science

- ❑ Images are 2 dimensional arrays of data, with an associated width, height, and color depth.
- ❑ Images typically use one byte per color channel per pixel.
- ❑ Gray images have 1 channel. RGB images have 3 color channels. RGBA images have 4 color channels.



Slide credit: Diane Theriault

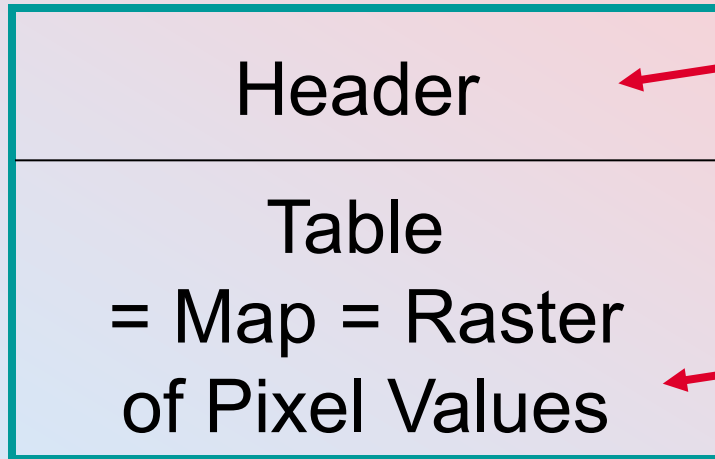


# Digital Image File Formats



Computer Science

## Image:



Size of table, color,  
compression scheme

Gray-scale images: generally  
1 byte per pixel

Color images: 3 numbers  
(each 1 byte) per pixel

Medical images, e.g.,

CT, MRI:  
typically 2 bytes per voxel

# Example: PGM Image



Computer Science

Image file

Image ??

P2		
3	3	255
<hr/>		
0	255	0
220	0	20
0	130	0

# Example: PGM Image



Computer Science

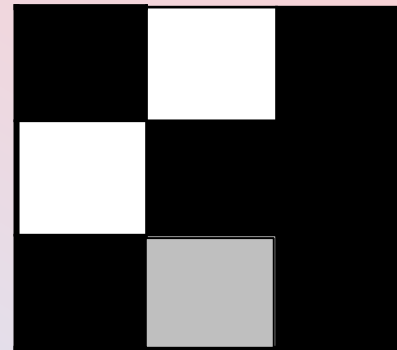
Image file

Image

P2

3 3 255

0	255	0
220	0	20
0	130	0



# Light: Electromagnetic Waves



Computer Science

Wavelength  $\lambda$

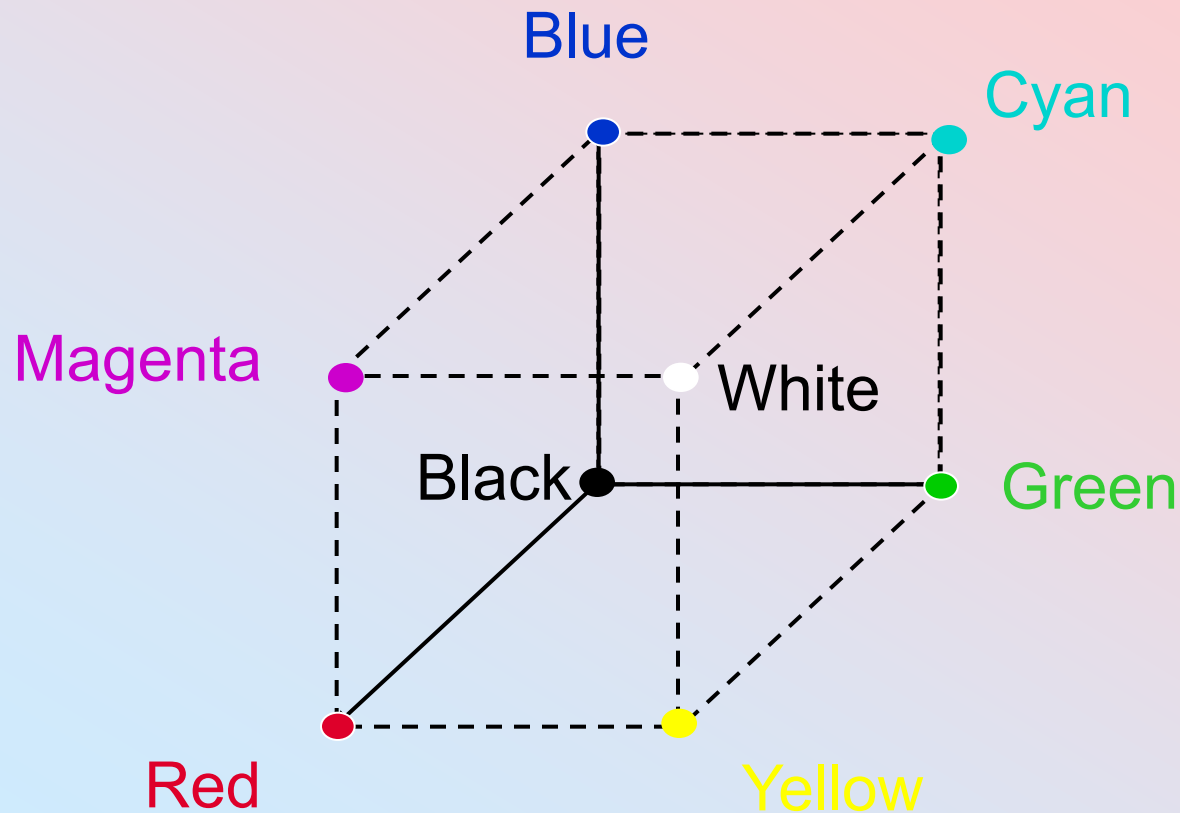


# RGB Color Space



Computer Science

## Additive Space



# Example: PPM Image



Computer Science

Image file

P3

3 3 255

0	0	0	255	0	0	0	0	0
0	255	0	0	0	0	255	255	0
0	0	0	0	0	255	0	0	0

Image ??



# Example: PPM Image



Computer Science

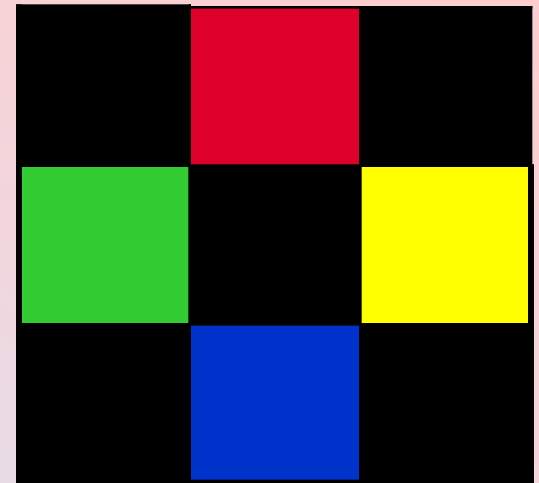
## Image file

P3

3 3 255

0	0	0	255	0	0	0	0	0
0	255	0	0	0	0	255	255	0
0	0	0	0	0	255	0	0	0

## Image



# How do I get at the data?



Computer Science

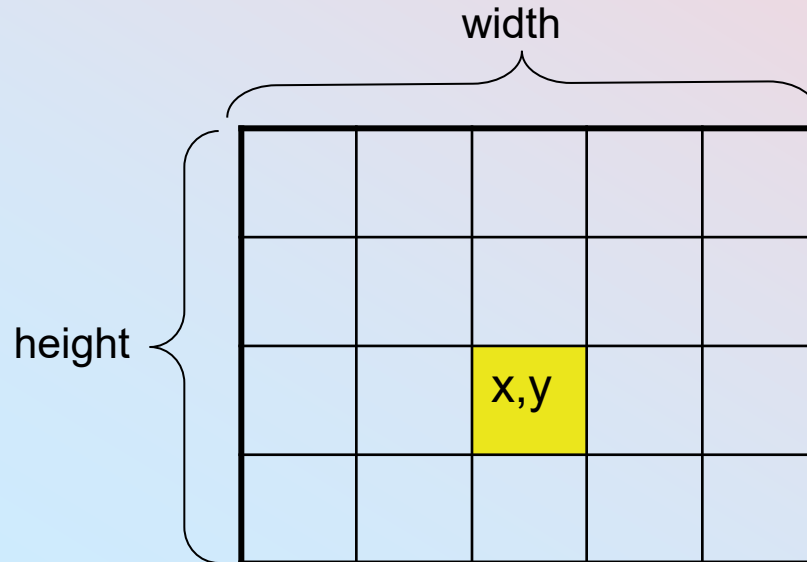
- ❑ Some image-handling APIs have nice interfaces, but speed can be a problem.
- ❑ You will probably have to handle the bytes of data directly at some point

# How do I get at the data?



Computer Science

- ❑ X = desired row
- ❑ Y = desired column
- ❑ C = color channel (red, green, blue, ...).
- ❑ Bpp = Bytes per pixel (color channels)
- ❑ Image data is normally stored in row major order
- ❑ Note that there may be multiple values associated with each x,y pixel
- ❑  $\text{Data}(x,y,c) = y * (\text{width} * \text{Bpp}) + x * \text{Bpp} + c$



Slide credit: Diane Theriault

# Example of a “Traditional” Computer Vision Algorithm: Color to Gray Scale Conversion



Computer Science

- ❑ Pre-neural-network-revolution Computer Vision: Algorithms
- ❑ Example of such a pre-2012 algorithm:

Converting from color to gray scale,  
a very common operation

# Color-to-Grayscale Conversion



Computer Science



Four Conversion Algorithms:

1. “Quick and dirty” conversion: Grab the Green Channel:  $G$
2. Average R, G, B:  $(R+G+B)/3$
3.  $\text{Max}(R, G, B)$
4. Weigh them:  $0.3 \cdot R + 0.6 \cdot G + 0.1 \cdot B$

Slide credit: Diane Theriault

# Image File Formats



Computer Science

- ❑ PPM / PGM is the simplest file format ever, but not supported by Photoshop or MS Image Viewer. Uncompressed.
- ❑ BMP: Microsoft's uncompressed image format
- ❑ GIF: Images are compressed using run-length encoding, and reducing the number of colors used. Patent expired 2003.
- ❑ JPEG: Images are compressed by removing high frequency information
- ❑ DICOM: Digital Imaging and Communications in Medicine

Slide credit: Diane Theriault



# Tools of the Trade



Computer Science

- ❑ OpenCV is a widely used, open-source computer vision library maintained by Intel
- ❑ Provides libraries for image I/O, movie I/O and camera capture
- ❑ Industrial strength computer vision and image processing implementations
- ❑ “Quick and dirty” GUI toolkit

# Today's Computer Vision: Mostly (but not all) Neural Networks



Computer Science

- ❑ Deep convolutional neural networks
- ❑ Transformers
- ❑ Diffusion models
  
- + traditional computer vision algorithms,  
representations, geometry, and tricks

Deep learning does not work well for:

Multi-view geometry, i.e., 3D object pose and 3D scene representation, and object tracking

# Traditional Computer Vision Algorithm: Template Matching



Computer Science

- ❑ *Template matching = search algorithm*
- ❑ *Goal: Find object shown in template image in a scene image.*
- ❑ *More specific goal: Find the location of the scene subimage that best matches the template image*
- ❑ *Mathematical definition of match:*
  - *Scene subimage  $s$ , template image  $m$*
  - *Same size images =  $n$  pixels*
  - *$s_i$  =  $i$ th pixel grey value in subimage of scene*
  - *$m_i$  =  $i$ th pixel grey value in template image  $m$*
  - *Sum-squared match equation  $SSD = \sum_{(i=1 \text{ to } n)} (s_i - m_i)^2$*
  - *Alternative match equation: Normalized Correlation Coefficient*
  - *Both match equations involve multiplying pixel values  $s_i m_i$*

# 1D Discrete Convolution



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1D Convolution:

Time signal  $f$  and shifted time signal  $g$  are multiplied and added:

$$\begin{aligned}(f * g)[n] &\stackrel{\text{def}}{=} \sum_{m=-\infty}^{\infty} f[m] g[n - m] \\ &= \sum_{m=-\infty}^{\infty} f[n - m] g[m].\end{aligned}$$

2D generalization:

$f$  = input image,  $g$  = template image  
(or CNN function)

# 2D Convolution Example



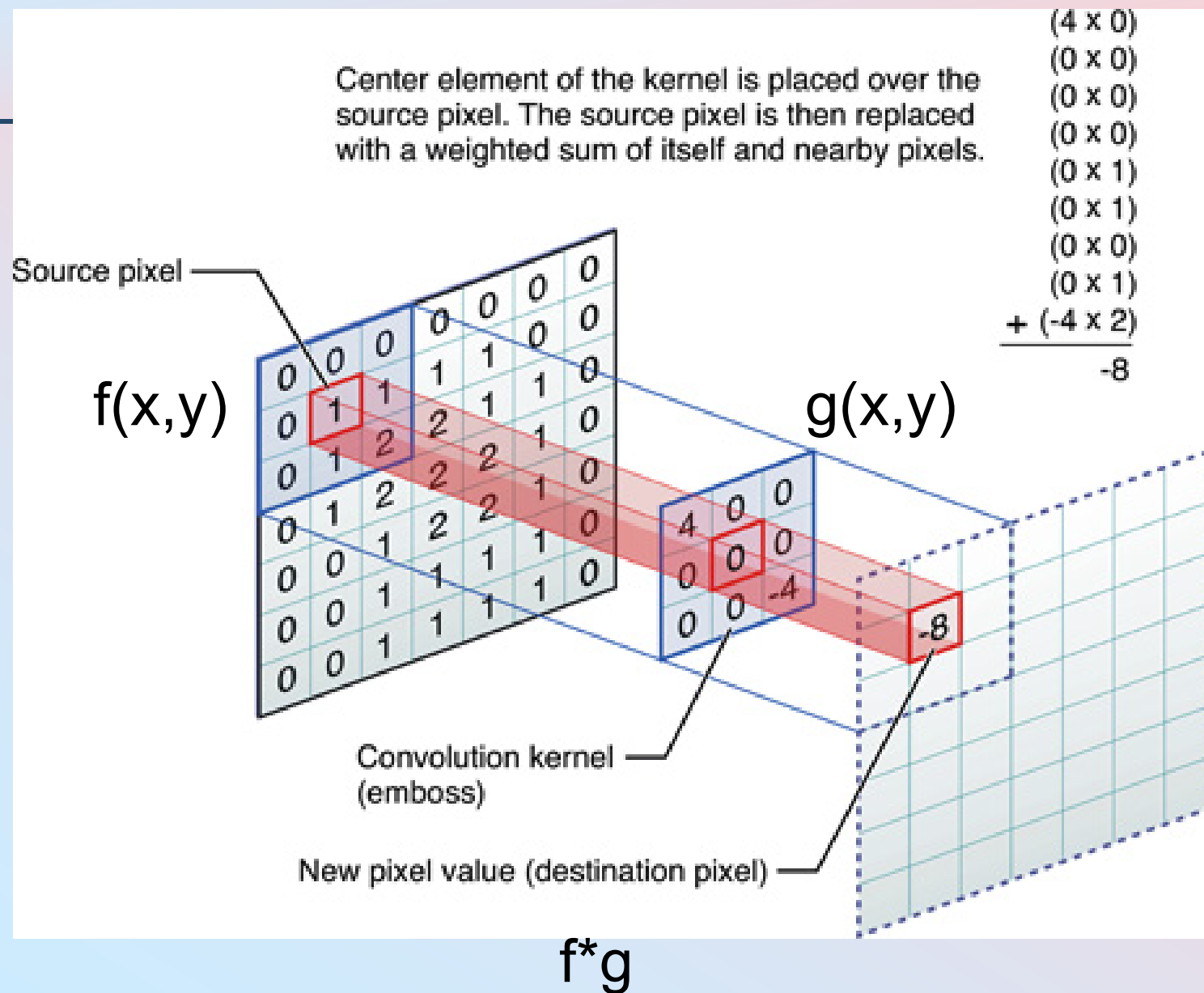
Computer Science

1 <sub>x1</sub>	1 <sub>x0</sub>	1 <sub>x1</sub>	0	0
0 <sub>x0</sub>	1 <sub>x1</sub>	1 <sub>x0</sub>	1	0
0 <sub>x1</sub>	0 <sub>x0</sub>	1 <sub>x1</sub>	1	1
0	0	1	1	0
0	1	1	0	0

Image

4		

Convolved  
Feature







Computer Science

# Why is Convolution Powerful?

# Signal Processing:



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**Convolution is used to define a “matched filter” for locating “targets” in time signals**

**Template matching is optimal algorithm if noise is Gaussian.**

# Optimality of Template Matching



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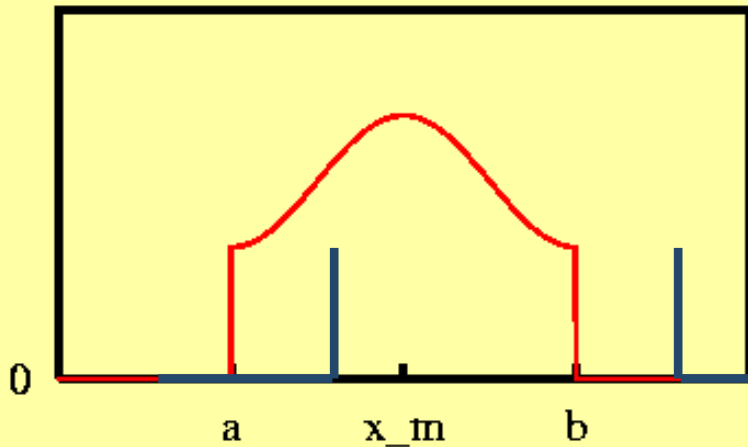
Betke, Makris, IJCV 2001

# 1D Position Estimation: $\sum \text{object} * \text{background}$

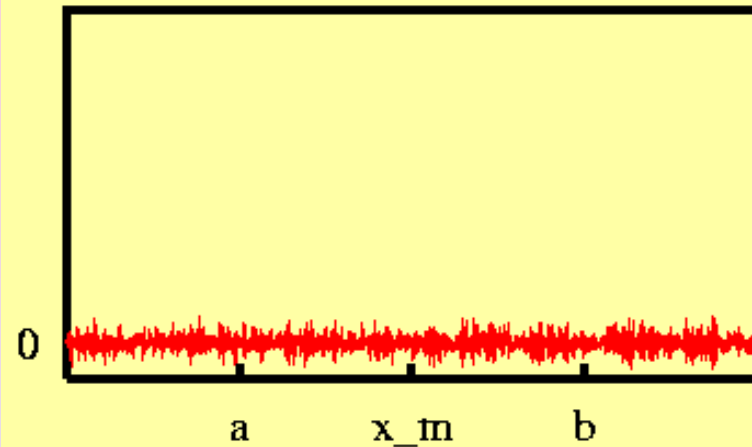


puter Science

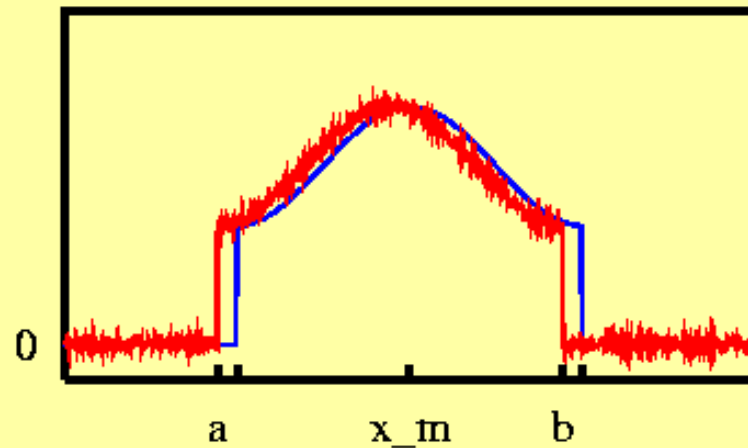
(a) Object



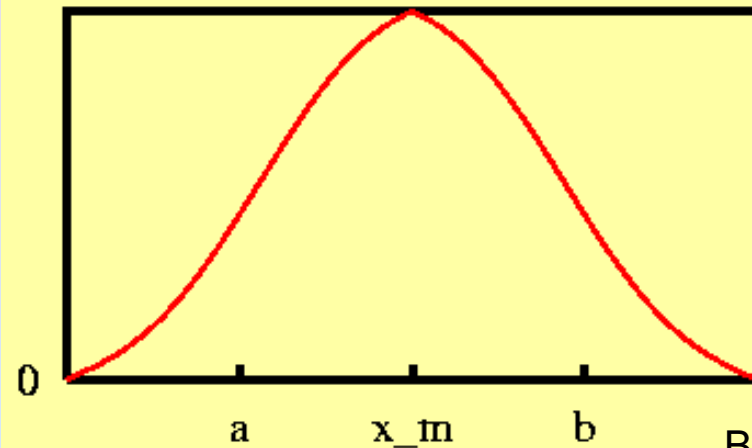
(b) Zero-mean Background



(c) Object and Zero-mean Background



(d) Classical Matched Filter Output

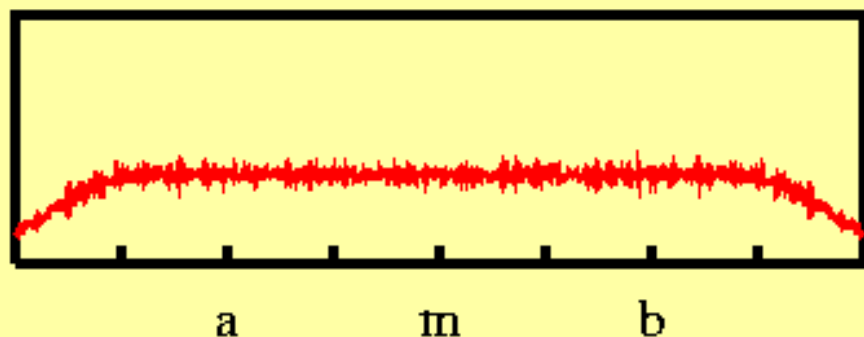


# Another 1D convolution example:

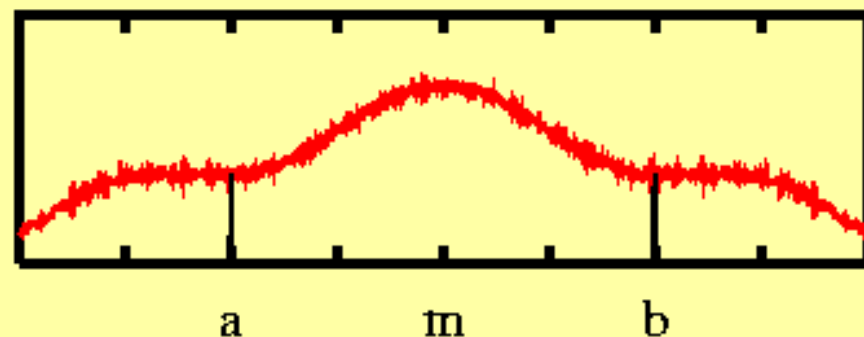


Computer Science

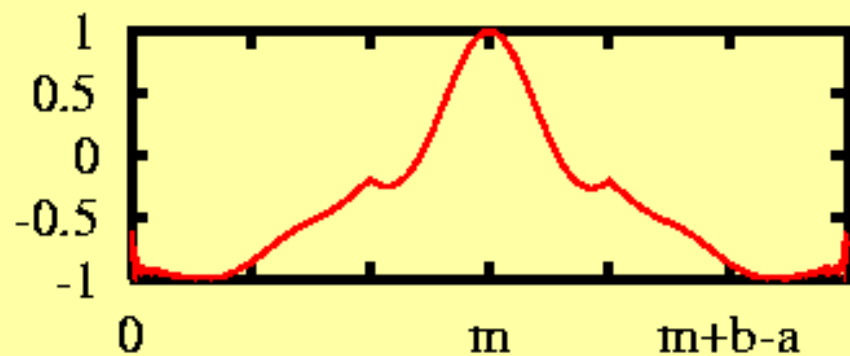
Nonzero-mean Background



Scene with Object



Norm. Correlation Coefficient



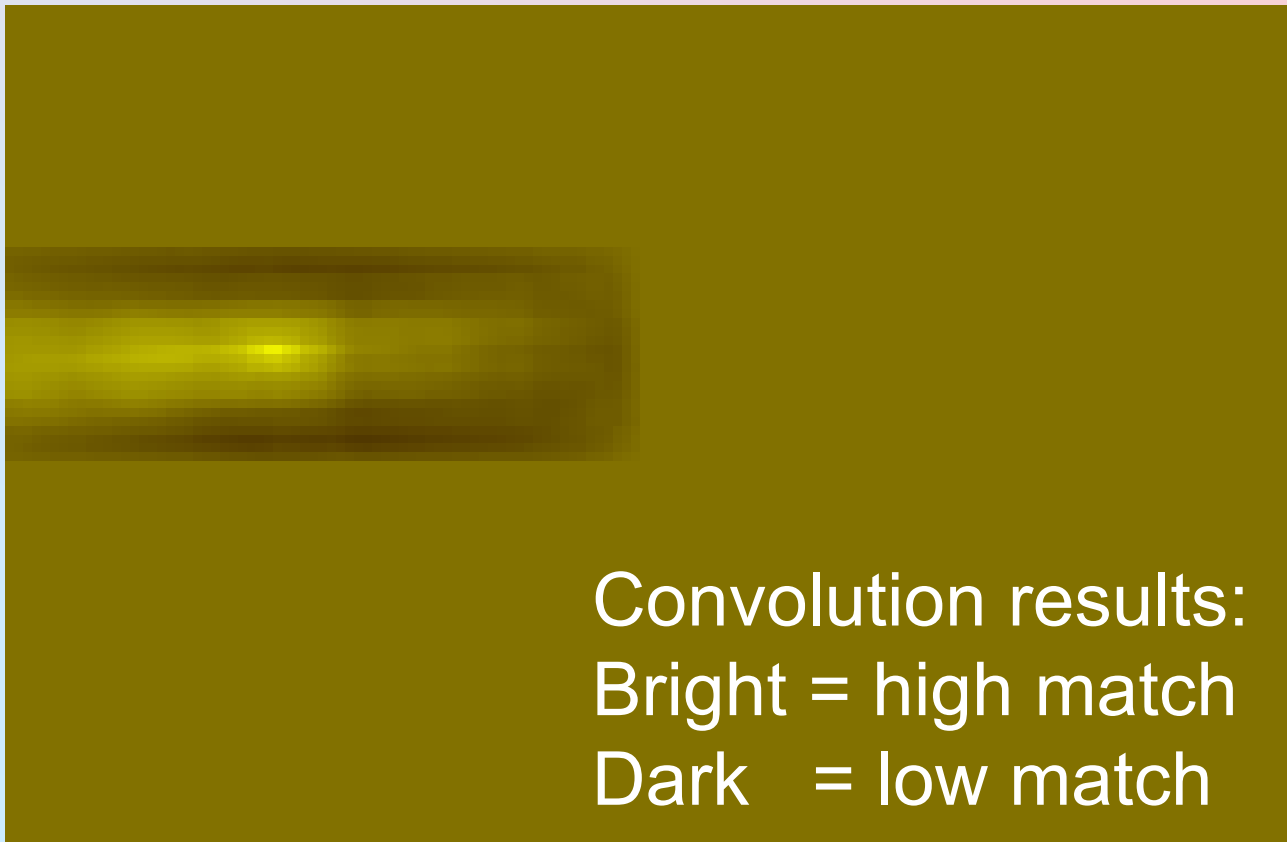
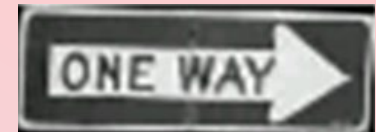
= convolution/std-devs

# 2D Position Estimation



Computer Science

Convolution of one-way sign with itself:  
Both scene and template image are



Convolution results:  
Bright = high match  
Dark = low match

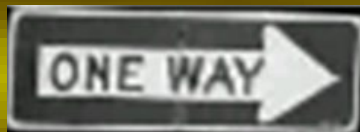


# 2D Position Estimation



Computer Science

Convolution of one-way sign with itself:  
Both scene and template image are



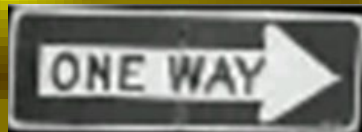
Perfect match

# 2D Position Estimation



Computer Science

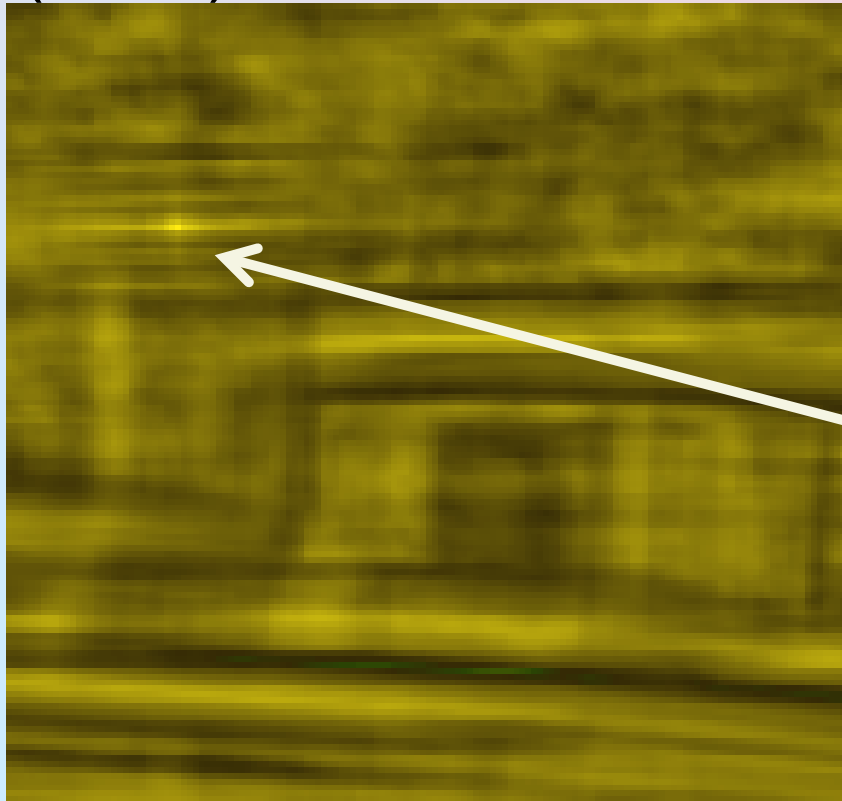
Convolution of one-way sign with itself:  
Both scene and template image are



Bad match

# 2 D Position Estimation

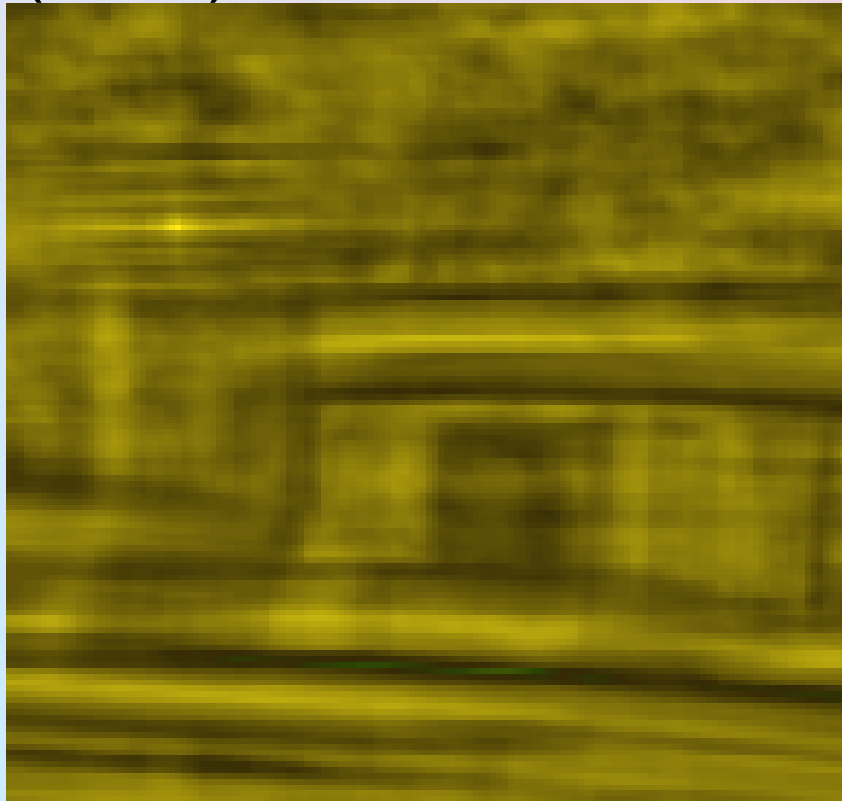
Convolution of one-way sign with scene  
(NCC)



Peak in  
performance surface  
(= negative loss fct)  
at correct location

# 2 D Position Estimation

Convolution of one-way sign with scene (NCC)



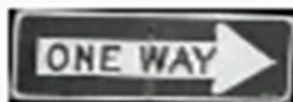
This performance surface is computed for **correct** size of one-way sign

Different surfaces for different sizes of object

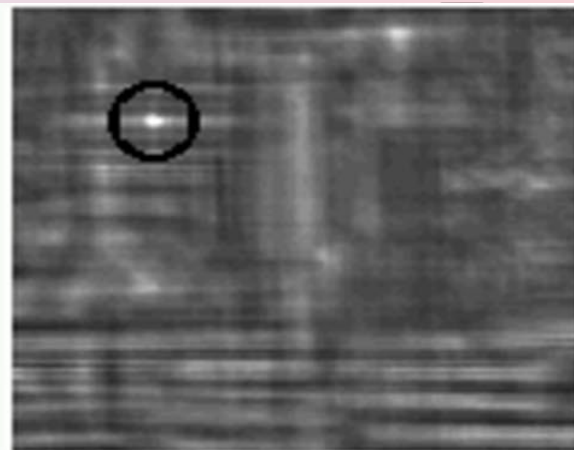
# Sample Performance Surfaces



1



complexity: 250  
size:  $73 \times 27$   
max. cor. coef. 0.82  
**correct match**



2



complexity: 33  
size:  $73 \times 27$   
max. cor. coef. 0.64  
**incorrect match**



3



(shown enlarged)  
complexity: 25  
size:  $21 \times 5$   
max. cor. coef. 0.70  
**incorrect match**



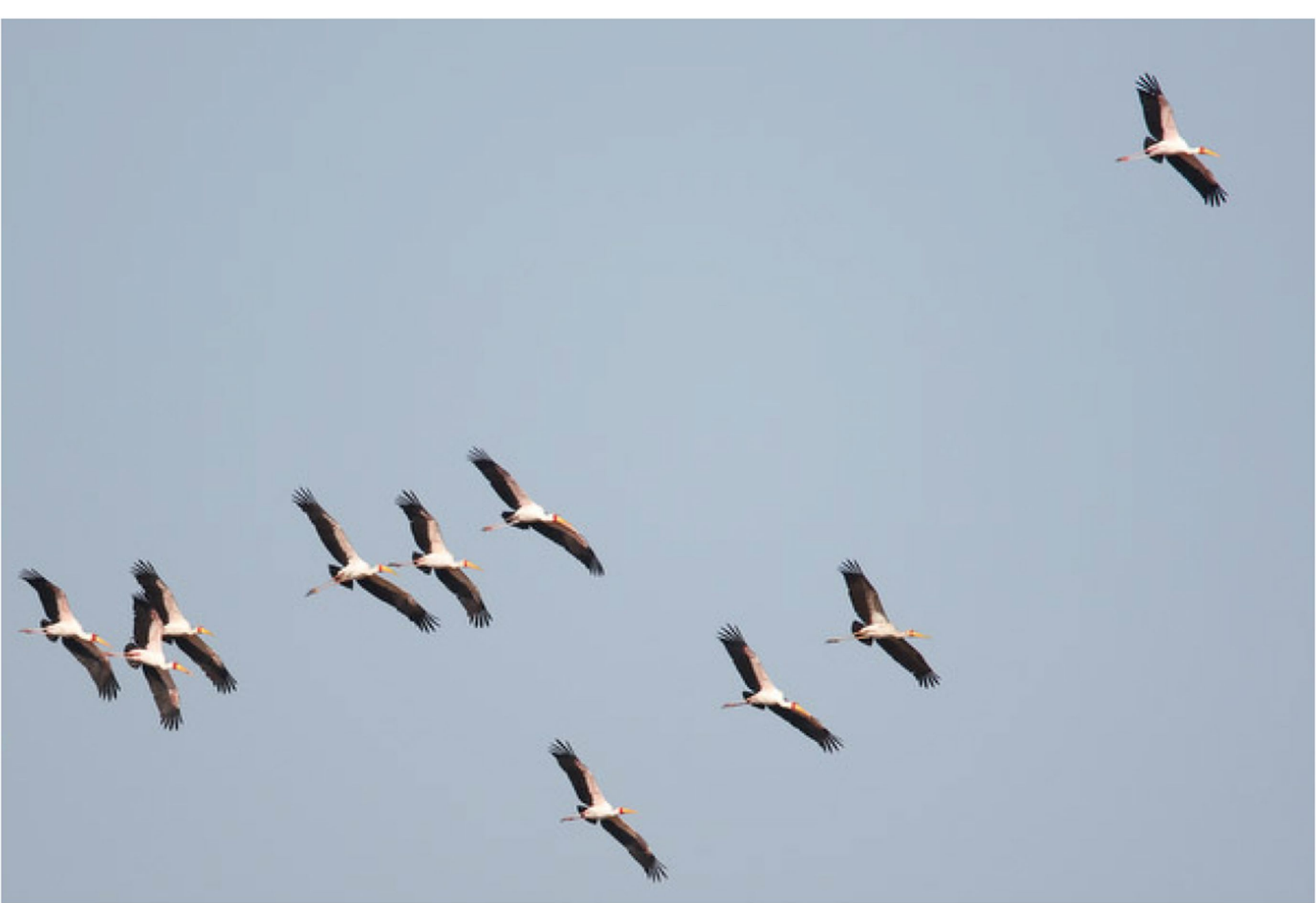
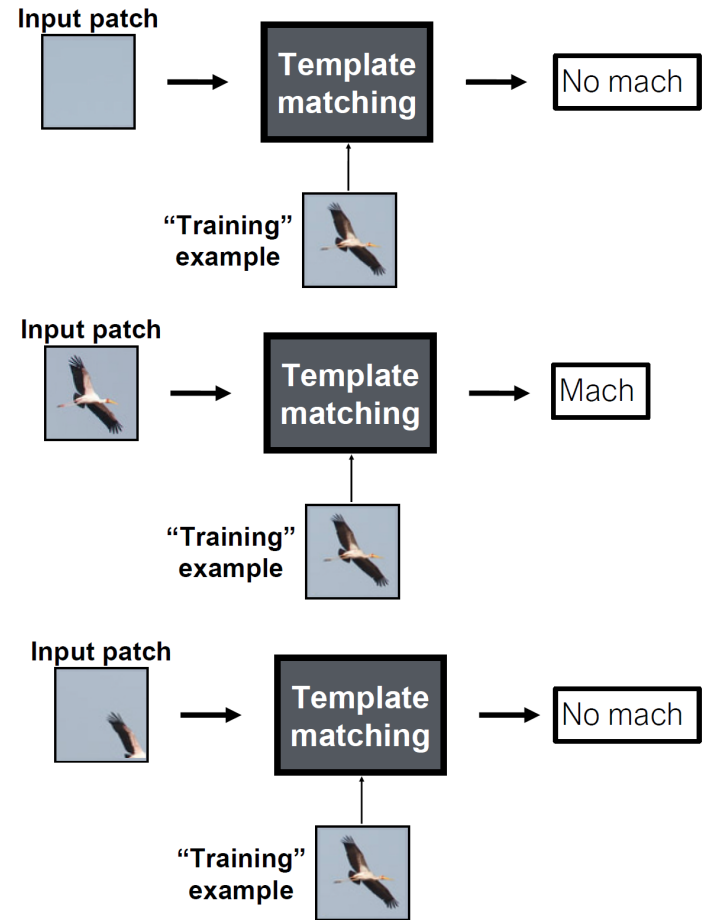
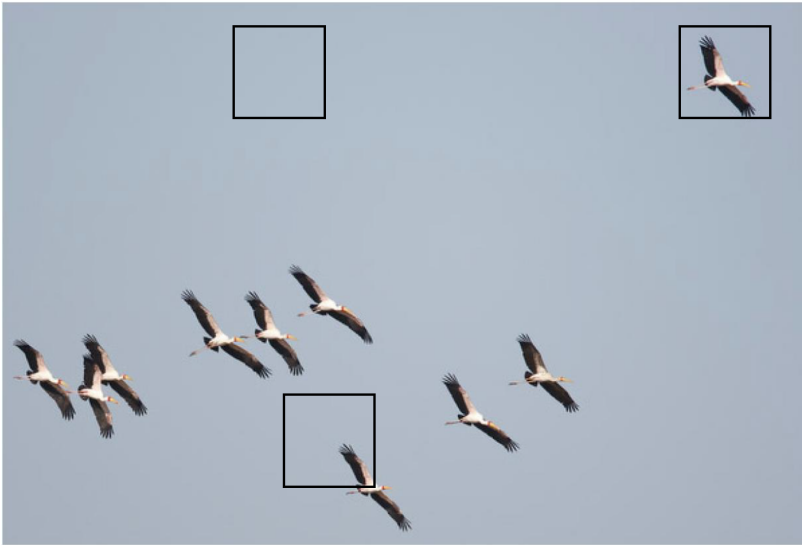
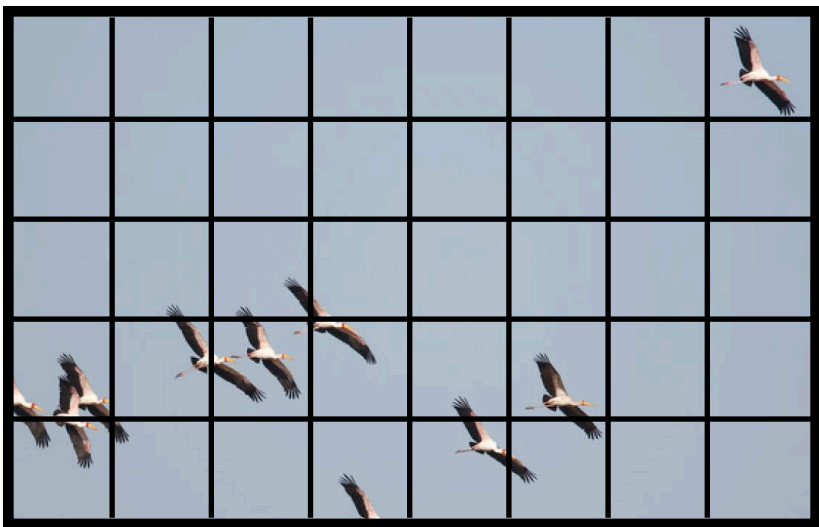


Image Credit: Efros/Freeman

# Convoluting template with subimage



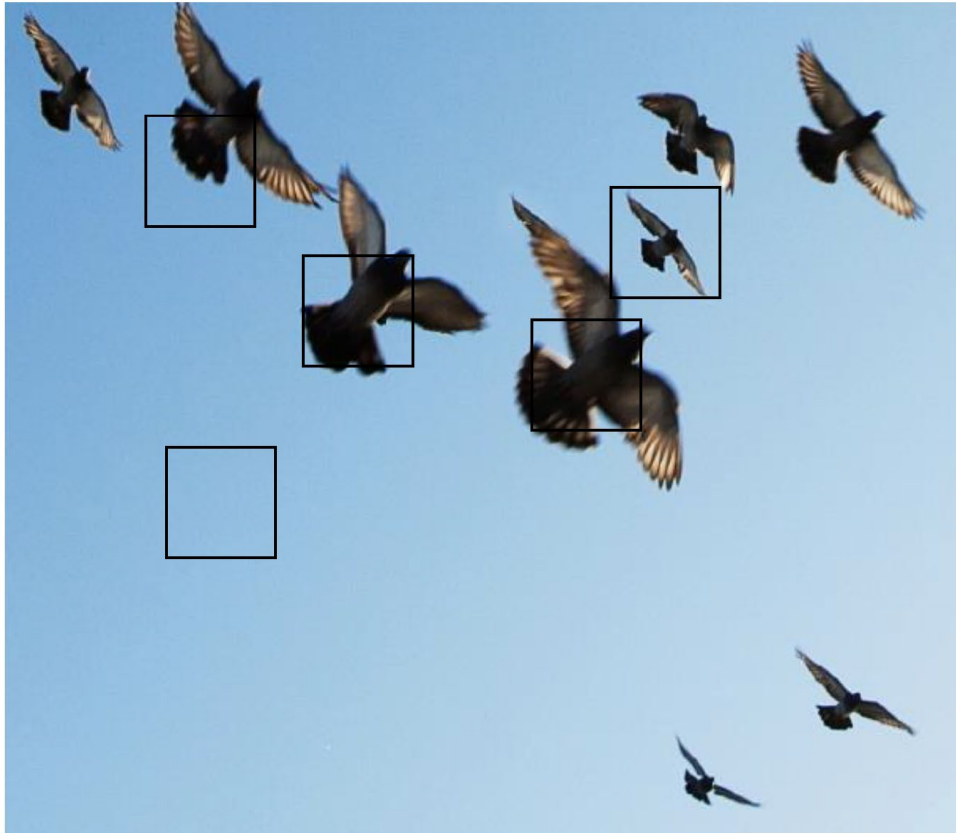




Sky	Sky	Sky	Sky	Sky	Sky	Sky	Bird
Sky	Sky	Sky	Sky	Sky	Sky	Sky	Sky
Sky	Sky	Sky	Sky	Sky	Sky	Sky	Sky
Bird	Bird	Bird	Sky	Bird	Sky	Sky	Sky
Sky	Sky	Sky	Bird	Sky	Sky	Sky	Sky

Image Credit: Freeman

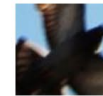
# What if object in image appears in a range of sizes?



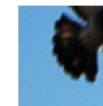
“Training”  
example



Mach



No mach



No mach



No mach

⋮

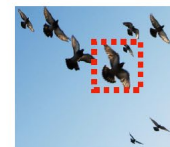
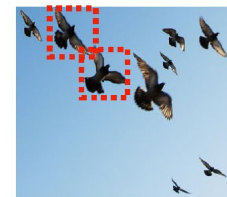
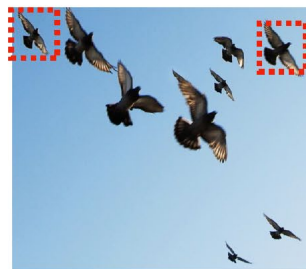
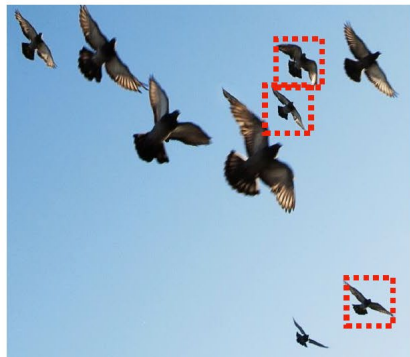
# Multi-Scale Pyramids



Template

# Multi-Scale Pyramids

Multiscale image pyramid



Template

A multiscale image pyramid provides an alternative image representation to achieve translation and scale invariance

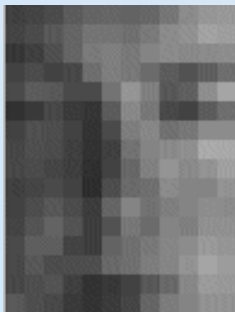
# Multi-Resolution Matching



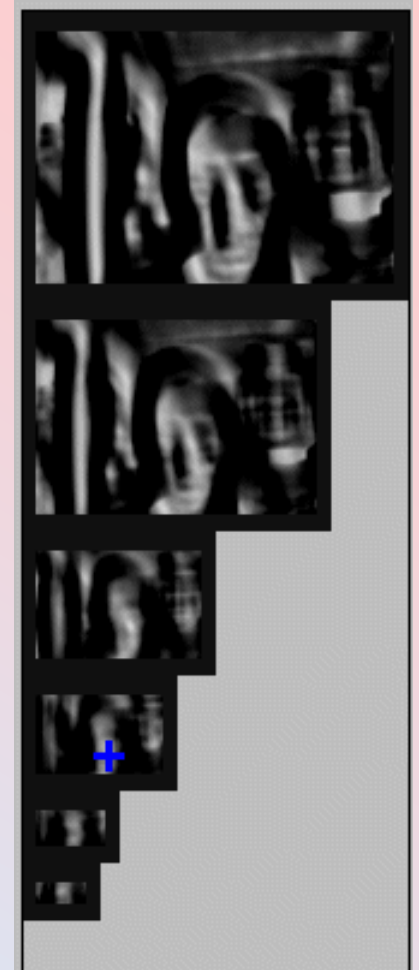
Computer Science

Normalized correlation coefficient over multi-resolution search space:

$$r = \frac{1/n \sum_i (s_i - \text{mean}(s)) (m_i - \text{mean}(m))}{(\sigma_s \sigma_m)}$$



← Template  
matched over all  
resolutions →



Live Video



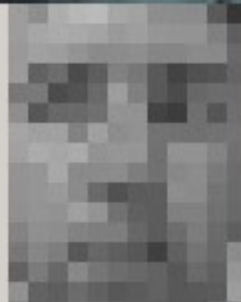
B&W Video



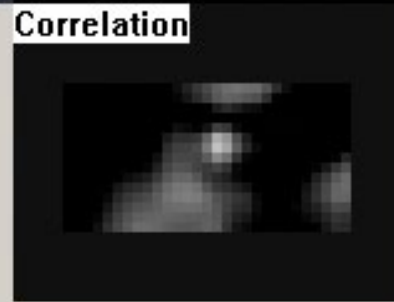
Motion



Color



Correlation

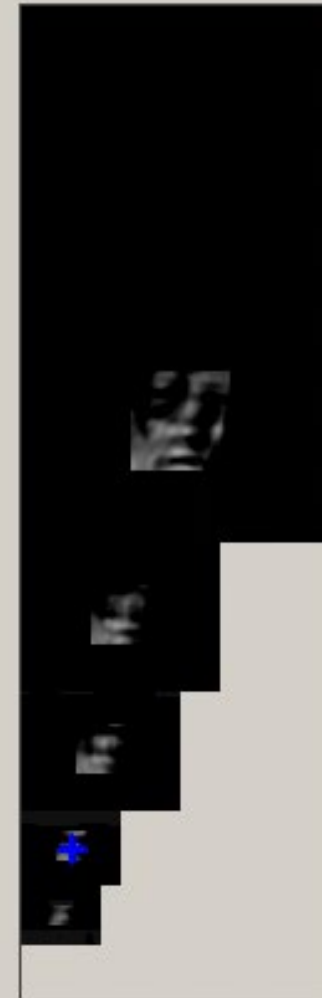


Max Score: 193; Scale: 6; Location: (160, 120)

OK

Cancel

☒ Pyramid Display



Clo

# Learning Objectives for this Lecture



Computer Science

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