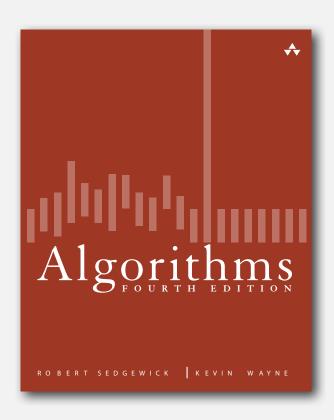
# 3.1 SYMBOL TABLES



- **API**
- sequential search
- binary search
- ordered operations

## ▶ API

- > sequential search
- ▶ binary search
- ordered operations

### Symbol tables

### Key-value pair abstraction.

- Insert a value with specified key.
- Given a key, search for the corresponding value.

### Ex. DNS lookup.

- Insert URL with specified IP address.
- Given URL, find corresponding IP address.

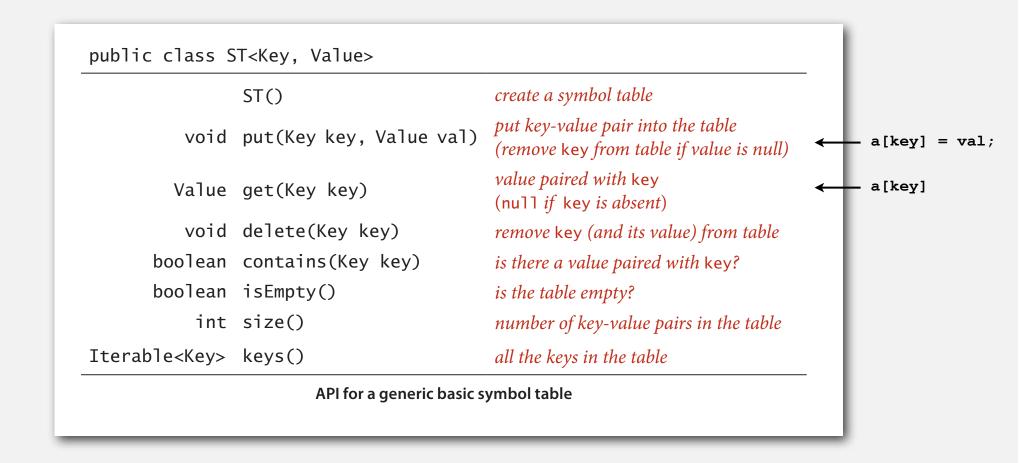
URL	IP address		
www.cs.princeton.edu	128.112.136.11		
www.princeton.edu	128.112.128.15		
www.yale.edu	130.132.143.21		
www.harvard.edu	128.103.060.55		
www.simpsons.com	209.052.165.60		
kev	value		

## Symbol table applications

application	purpose of search	key	value	
dictionary	find definition	word	definition	
book index	find relevant pages	term	list of page numbers	
file share	find song to download	name of song	computer ID	
financial account	process transactions	account number	transaction details	
web search	find relevant web pages	keyword	list of page names	
compiler	find properties of variables	variable name	type and value	
routing table	route Internet packets	destination	best route	
DNS	find IP address given URL	URL	IP address	
reverse DNS	find URL given IP address	IP address	URL	
genomics	find markers	DNA string	known positions	
file system	find file on disk	filename	location on disk	

### Symbol table API

Associative array abstraction. Associate one value with each key.



#### Conventions

- Values are not null.
- Method get() returns null if key not present.
- Method put () overwrites old value with new value.

### Intended consequences.

• Easy to implement contains ().

```
public boolean contains(Key key)
{ return get(key) != null; }
```

• Can implement lazy version of delete().

```
public void delete(Key key)
{  put(key, null); }
```

### Keys and values

Value type. Any generic type.

### Key type: several natural assumptions.

- Assume keys are Comparable, USE compareTo().
- Assume keys are any generic type, use equals() to test equality.
- Assume keys are any generic type, use equals() to test equality;
   use hashcode() to scramble key.

built-in to Java (stay tuned)

Best practices. Use immutable types for symbol table keys.

- Immutable in Java: String, Integer, Double, java.io.File, ...
- Mutable in Java: StringBuilder, java.net.URL, arrays, ...

specify Comparable in API.

### Equality test

All Java classes inherit a method equals ().

Java requirements. For any references x, y and z:

```
    Reflexive: x.equals(x) is true.
    Symmetric: x.equals(y) iff y.equals(x).
    Transitive: if x.equals(y) and y.equals(z), then x.equals(z).
```

• Non-null: x.equals(null) iS false.

```
do x and y refer to
the same object?
```

Default implementation. (x == y)

Customized implementations. Integer, Double, String, File, URL, ... User-defined implementations. Some care needed.

### Implementing equals for user-defined types

### Seems easy.

```
class Date implements Comparable<Date>
public
   private final int month;
   private final int day;
   private final int year;
   public boolean equals(Date that)
      if (this.day != that.day ) return false;
                                                             check that all significant
      if (this.month != that.month) return false; <--</pre>
                                                             fields are the same
      if (this.year != that.year ) return false;
      return true;
```

### Implementing equals for user-defined types

Seems easy, but requires some care. typically unsafe to use equals () with inheritance (would violate symmetry) public final class Date implements Comparable<Date> private final int month; must be Object. private final int day; Why? Experts still debate. private final int year; public boolean equals(Object y) optimize for true object equality if (y == this) return true; check for null if (y == null) return false; if (y.getClass() != this.getClass()) objects must be in the same class (religion: getClass() VS. instanceof) return false; cast is guaranteed to succeed Date that = (Date) y; if (this.day != that.day ) return false; check that all significant if (this.month != that.month) return false; fields are the same if (this.year != that.year ) return false; return true;

### Equals design

### "Standard" recipe for user-defined types.

- Optimization for reference equality.
- Check against null.
- Check that two objects are of the same type and cast.
- Compare each significant field:
  - if field is a primitive type, use == apply rule recursively
  - if field is an object, use equals ()
  - if field is an array, apply to each entry 

    alternatively, use Arrays.equals(a, b)

    or Arrays.deepEquals(a, b),

    but not a.equals(b)

#### Best practices.

- Compare fields mostly likely to differ first.
- No need to use calculated fields that depend on other fields.
- Make compare To () consistent with equals ().

```
\mathbf{x}.equals(\mathbf{y}) if and only if (\mathbf{x}.compareTo(\mathbf{y}) == 0)
```

#### ST test client for traces

Build ST by associating value i with  $i^{th}$  string from standard input.

```
public static void main(String[] args)
{
   ST<String, Integer> st = new ST<String, Integer>();
   for (int i = 0; !StdIn.isEmpty(); i++)
   {
      String key = StdIn.readString();
      st.put(key, i);
   }
   for (String s : st.keys())
      StdOut.println(s + " " + st.get(s));
}
```

```
keys S E A R C H E X A M P L E values 0 1 2 3 4 5 6 7 8 9 10 11 12
```

#### output

```
A 8
C 4
E 12
H 5
L 11
M 9
P 10
R 3
S 0
X 7
```

### ST test client for analysis

Frequency counter. Read a sequence of strings from standard input and print out one that occurs with highest frequency.

```
% more tinyTale.txt
it was the best of times
it was the worst of times
it was the age of wisdom
it was the age of foolishness
it was the epoch of belief
it was the epoch of incredulity
it was the season of light
it was the season of darkness
it was the spring of hope
it was the winter of despair
                                                        tiny example
% java FrequencyCounter 1 < tinyTale.txt</pre>
                                                        (60 words, 20 distinct)
it 10
                                                        real example
% java FrequencyCounter 8 < tale.txt</pre>
                                                        (135,635 words, 10,769 distinct)
business 122
                                                        real example
% java FrequencyCounter 10 < leipzig1M.txt 	</pre>
                                                        (21,191,455 words, 534,580 distinct)
government 24763
```

### Frequency counter implementation

```
public class FrequencyCounter
   public static void main(String[] args)
      int minlen = Integer.parseInt(args[0]);
                                                                            create ST
      ST<String, Integer> st = new ST<String, Integer>();
      while (!StdIn.isEmpty())
                                                     ignore short strings
         String word = StdIn.readString();
                                                                            read string and
          if (word.length() < minlen) continue;</pre>
                                                                            update frequency
          if (!st.contains(word)) st.put(word, 1);
         else
                                    st.put(word, st.get(word) + 1);
      String max = "";
      st.put(max, 0);
                                                                            print a string
                                                                            with max freq
      for (String word : st.keys())
          if (st.get(word) > st.get(max))
             max = word;
      StdOut.println(max + " " + st.get(max));
```

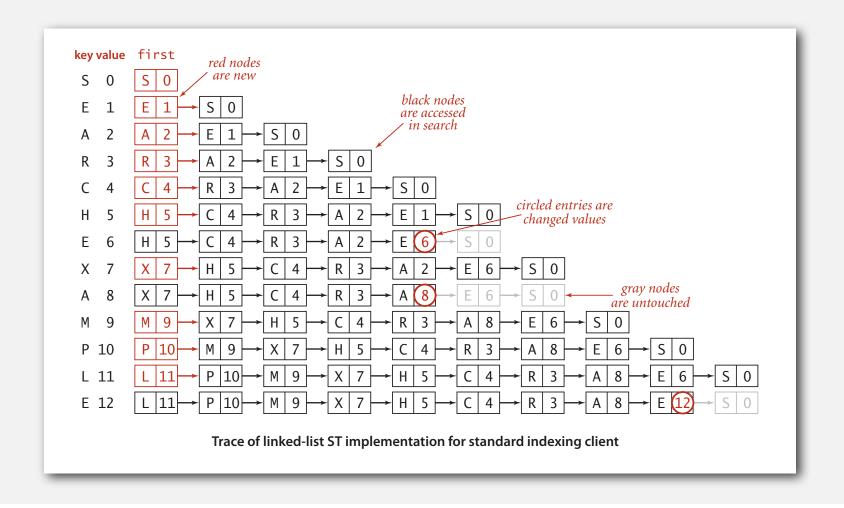
- sequential searchbinary search

### Sequential search in a linked list

Data structure. Maintain an (unordered) linked list of key-value pairs.

Search. Scan through all keys until find a match.

Insert. Scan through all keys until find a match; if no match add to front.



### Elementary ST implementations: summary

ST implementation	worst case		average case		ordered	operations
31 implementation	search	insert	search hit	insert	iteration?	on keys
sequential search (unordered list)	N	N	N / 2	N	no	equals()

Challenge. Efficient implementations of both search and insert.

- > sequential search
- binary searchordered symbol table ops

### Binary search

Data structure. Maintain an ordered array of key-value pairs.

Rank helper function. How many keys < k?

```
keys[]
                           1 2
successful search for P
        lo hi m
                                                                         entries in black
                                                                        are a[lo..hi]
                                                                 entry in red is a [m]
                                   H L M
                                                       loop exits with keys[m] = P: return 6
unsuccessful search for 0
        lo hi m
                   loop exits with lo > hi: return 7
                     Trace of binary search for rank in an ordered array
```

### Binary search: Java implementation

```
public Value get(Key key)
   if (isEmpty()) return null;
   int i = rank(key);
   if (i < N && keys[i].compareTo(key) == 0) return vals[i];</pre>
   else return null;
                                                number of keys < key
private int rank(Key key)
{
   int lo = 0, hi = N-1;
   while (lo <= hi)
       int mid = lo + (hi - lo) / 2;
       int cmp = key.compareTo(keys[mid]);
              (cmp < 0) hi = mid - 1;
       if
       else if (cmp > 0) lo = mid + 1;
       else if (cmp == 0) return mid;
  return lo;
```

### Binary search: mathematical analysis

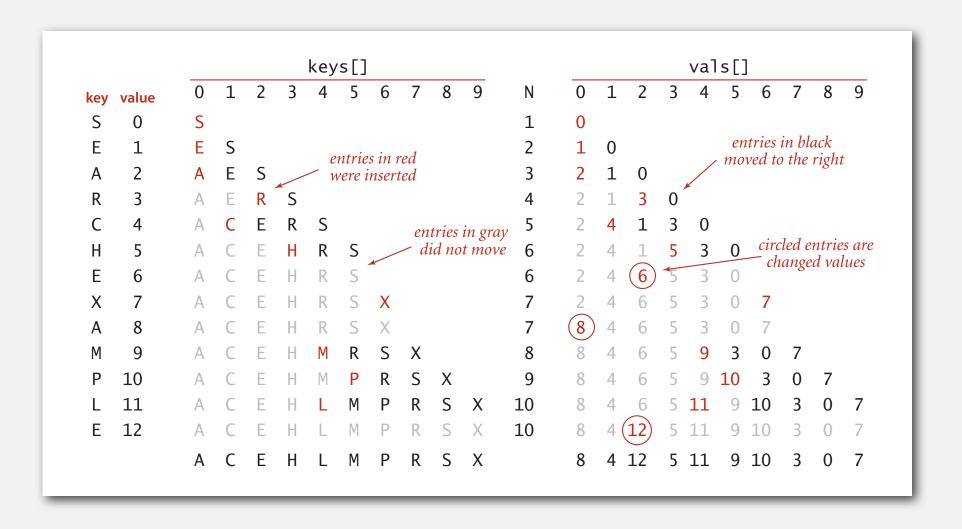
Proposition. Binary search uses  $\sim \lg N$  compares to search any array of size N.

Pf. 
$$T(N)$$
 = number of compares to binary search in a sorted array of size  $N$ .  
 $\leq T(\lfloor N/2 \rfloor) + 1$ 
left or right half

Recall lecture 2.

### Binary search: trace of standard indexing client

Problem. To insert, need to shift all greater keys over.



### Elementary ST implementations: summary

ST implementation	worst case		average case		ordered	operations
	search	insert	search hit	insert	iteration?	on keys
sequential search (unordered list)	N	N	N / 2	N	no	equals()
binary search (ordered array)	log N	N	log N	N / 2	yes	compareTo()

Challenge. Efficient implementations of both search and insert.

- ► API
- > sequential search
- binary search
- ordered operations

### Ordered symbol table API

```
values
                                 keys
                    min() \longrightarrow 09:00:00
                                          Chicago
                              09:00:03
                                          Phoenix
                              09:00:13 Houston
            get(09:00:13)—
                              09:00:59
                                          Chicago
                              09:01:10
                                          Houston
          floor(09:05:00) \longrightarrow 09:03:13
                                          Chicago
                              09:10:11
                                          Seattle
                select(7) \rightarrow 09:10:25
                                          Seattle
                              09:14:25
                                         Phoenix
                              09:19:32
                                          Chicago
                              09:19:46
                                          Chicago
keys(09:15:00, 09:25:00) \longrightarrow 09:21:05
                                          Chicago
                                          Seattle
                              09:22:43
                              09:22:54 Seattle
                              09:25:52 Chicago
        ceiling(09:30:00) \rightarrow 09:35:21 Chicago
                              09:36:14 Seattle
                    max() \longrightarrow 09:37:44
                                          Phoenix
size(09:15:00, 09:25:00) is 5
     rank(09:10:25) is 7
     Examples of ordered symbol-table operations
```

### Ordered symbol table API

```
public class ST<Key extends (Comparable) Key>, Value>
                 ST()
                                                create an ordered symbol table
                                                put key-value pair into the table
           void put(Key key, Value val)
                                                (remove key from table if value is null)
                                                value paired with key
         Value get(Key key)
                                                (null if key is absent)
           void delete(Key key)
                                                remove key (and its value) from table
       boolean contains(Key key)
                                                is there a value paired with key?
                                                is the table empty?
       boolean isEmpty()
            int size()
                                                number of key-value pairs
            Key min()
                                                smallest key
            Key max()
                                                largest key
            Key floor(Key key)
                                                largest key less than or equal to key
            Key ceiling(Key key)
                                                smallest key greater than or equal to key
            int rank(Key key)
                                                number of keys less than key
            Key select(int k)
                                                key of rank k
           void deleteMin()
                                                delete smallest key
           void deleteMax()
                                                delete largest key
            int size(Key lo, Key hi)
                                                number of keys in [lo..hi]
Iterable<Key> keys(Key lo, Key hi)
                                                keys in [lo..hi], in sorted order
Iterable<Key> keys()
                                                all keys in the table, in sorted order
```

### Binary search: ordered symbol table operations summary

	sequential search	binary search
search	N	lg N
insert	1	N
min / max	N	1
floor / ceiling	N	lg N
rank	N	lg N
select	N	1
ordered iteration	N log N	N

order of growth of the running time for ordered symbol table operations