

CS565: Data Mining

Written Assignment 2

Due Date: October 26th, 2007 at 4:30 PM in the drop box.

Problem 1 (Based on exercises 5.1 and 5.7)

The Apriori algorithm makes use of prior knowledge of subset support properties.

- 1. Given frequent itemset *L* and a subset *s* of *L*, prove formally that the confidence of the rule "f => L-f" cannot be more than the confidence of "s => L-s", where *f* is a subset of *s*.
- 2. A *partitioning* version of Apriori divides the transactions of a database *D* into *n* non-overlapping partitions. Prove that any *itemset* that is frequent in *D* must be frequent in at least one partition in *D*.
- 3. Suppose that all the frequent *itemsets* with minimum support *min_sup* for a large transaction database *D* are saved on a file. At some point, we add a new set of transactions δ into *D*. Discuss how to *efficiently* mine the new database $D + \delta$ to find frequent itemsets using the same minimum support threshold.

Problem 2

Consider the following database of transactions.

| TransID | Items Bought |
|---------|---------------|
| 1 | {a,b,d,e} |
| 2 | {b,c,d} |
| 3 | {a,b,d,e} |
| 4 | {a,c,d,e} |
| 5 | $\{b,c,d,e\}$ |
| 6 | {b,d,e} |
| 7 | $\{c,d,f\}$ |
| 8 | $\{a,b,c,f\}$ |
| 9 | {a,d,e} |
| 10 | {b,d} |

Assuming that $min_sup = 30\%$ (i.e. an itmeset is frequent if it appears in at least 3 transactions), use the FP-growth algorithm to generate all the frequent itemsets. Show the FP-tree, the conditional FP-trees and the frequent itemsets. Also, give the maximal frequent itemsets.

Problem 3

Consider a database that stores records with four attributes *A*, *B*, *C* and *Class*. The first three attributes are categorical attributes and the fourth is a class attribute. Build a Naive Bayesian Classifier (NBC) using the following training set:

| Α | В | С | Class |
|----|----|----|-------|
| A1 | B2 | C1 | Р |
| A2 | B1 | C2 | Ν |
| A1 | B1 | C2 | Ν |
| A1 | B2 | C1 | Р |
| A2 | B3 | C2 | Ν |
| A3 | B1 | C1 | Р |
| A1 | B3 | C1 | Ν |
| A3 | B3 | C1 | Р |
| A2 | B2 | C2 | Ν |
| A1 | B3 | C2 | Р |
| A2 | B2 | C1 | Р |
| A3 | B1 | C2 | Р |
| A3 | B2 | C2 | Ν |
| A3 | B1 | C1 | Р |

Using the NBC that you created, decide the class of the following records: R1=[A2, B1, C1], R2=[A3, B1, C2] and R3=[A1,B1,C1]

Problem 4

Given the following database below:

| Χ | Y | Ζ | Class |
|----|---|----|-------|
| 15 | 1 | A1 | Ν |
| 20 | 3 | A2 | Р |
| 25 | 2 | A1 | Ν |
| 30 | 4 | A1 | Ν |
| 35 | 2 | A2 | Р |
| 25 | 4 | A1 | Ν |
| 15 | 2 | A2 | Р |
| 20 | 4 | A1 | Р |

build the complete decision tree using binary splits and gini index.

Then, compute the accuracy of the classifier on the following testing dataset.

| X | Y | Ζ | Class |
|----|---|----|-------|
| 10 | 2 | A1 | Р |
| 20 | 1 | A2 | Ν |
| 30 | 3 | A1 | Р |
| 40 | 2 | A2 | Р |