

# Scalability of Multicast Delivery for Non-sequential Streaming Access\*

Shudong Jin      Azer Bestavros

Computer Science Department  
Boston University  
Boston, MA 02215  
{jins,best}@cs.bu.edu

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## Abstract

To serve asynchronous requests using multicast, two categories of techniques, stream merging and periodic broadcasting have been proposed. For sequential streaming access where requests are uninterrupted from the beginning to the end of an object, these techniques are highly scalable: the required server bandwidth for stream merging grows *logarithmically* as request arrival rate, and the required server bandwidth for periodic broadcasting varies *logarithmically* as the inverse of start-up delay. However, sequential access is inappropriate to model partial requests and client interactivity observed in various streaming access workloads. This paper analytically and experimentally studies the scalability of multicast delivery under a non-sequential access model where requests start at random points in the object. We show that the required server bandwidth for any protocols providing immediate service grows at least as the *square root* of request arrival rate, and the required server bandwidth for any protocols providing delayed service grows *linearly* with the inverse of start-up delay. We also investigate the impact of limited client receiving bandwidth on scalability. We optimize practical protocols which provide immediate service to non-sequential requests. The protocols utilize limited client receiving bandwidth, and they are near-optimal in that the required server bandwidth is very close to its lower bound.

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# 1 Introduction

Streaming media delivery presents formidable strain on server and network capacity. With the mushrooming demand for large electronic artifacts from Internet servers (ranging from Video-on-Demand servers to software repository servers), multicast has emerged as a promising scalable delivery technique for such content.

Multicast can be used in both a demand-driven (closed-loop) fashion and a data-centered (open-loop) fashion. In closed-loop approaches, service starts as soon as a request is made. However, as time goes by, it is possible that the service be delegated to an existing multicast stream. For example, consider a scenario in which two clients download a one-hour video, with the second client starting one minute after the first. Service to the second client starts immediately through a dedicated delivery of the first minute of the video to that client, with the remaining fifty nine minutes obtained (and buffered for play out one minute later) by joining the first client's multicast channel. In open-loop approaches, a server multicasts the object or the segments of the object periodically, and clients simply join such multicast channels. Since a server is not interactively responding to request arrivals, clients may have to wait before service could start.

Both closed-loop and open-loop approaches have been well-studied, including the early batching [13, 15], piggybacking [23, 24, 2, 30], and stream tapping/patching [10, 27, 9, 22, 41, 8] techniques, as well as the more recent stream merging [17, 18, 19, 7, 14, 33, 6, 44] and broadcasting protocols [43, 3, 28, 16, 21, 29, 36, 37, 38, 40, 39, 26, 42]. Two particular techniques—stream merging and periodic broadcasting—have been shown to be highly scalable.

Stream merging originated with the work of Eager, Vernon, and Zahorjan [17, 18, 20]. With stream merging, server bandwidth grows *logarithmically* with request arrival rate (or the average number of clients requesting an object simultaneously). Periodic broadcasting was introduced by Viswanathan and Imielinski [43]. With periodic broadcasting, clients may observe a small start-up delay but the required server bandwidth grows *logarithmically* with the inverse of that start-up delay. Both stream merging and periodic broadcasting techniques are built on the assumptions that clients have higher receiving bandwidth than the object play-back rate, and that they have local storage to keep prefetched portions of the object temporarily.

The scalability of both stream merging and periodic broadcasting rests on the assumption of sequential access. That is, clients request an object from the beginning and play it without interruption to the end. It is unknown how these techniques scale in a non-sequential access environment, in which clients may request the segments of an object. Indeed, recent studies on the characterization of streaming access workloads [34, 25, 12, 4] have revealed that client access is seldom sequential due to frequent client interactivity. While several studies have tried to minimize the bandwidth requirement for non-sequential access in Video-on-Demand servers [5, 31, 32, 1, 11, 35], it is still unknown what are the potential and limitations of multicast delivery in a non-sequential access environment.

We give two example applications with non-sequential access characteristics. The first example is interactive Video-on-Demand for remote learning in an educational environment, or for press releases in a corporate environment, for example. A potentially large number of clients may request an object within a short period of time (e.g. after a lecture is released, or after a press release is put out), but not all of them may settle for a continuous playout from beginning to end. Specifically, clients may jump frequently using VCR functionality such as pause, fast-forward, skip, and rewind. Clearly, it is desirable that the server be able to support a very large number of simultaneous requests while minimizing the start-up delay for the requests. The second example is real-time large software distribution applications. Here a large number of clients may download a new software release simultaneously. The entire large software package could be viewed as a streaming object and served using multicast. However, different clients may require different

components of the software due to customized installations, for example. This translates to “jumps” in the process of accessing the object.

## Paper Contributions and Overview

This paper considers the problem of using multicast to serve non-sequential requests. We derive a tight lower bound on the required server bandwidth for any protocols providing immediate or delayed service. The lower bound is validated through simulation. Our results indicate that the scalability of multicast delivery under a non-sequential access model is not as good as the logarithmic scalability achievable under a sequential access model. Specifically, we show that for non-sequential access the required server bandwidth for any protocol providing immediate service grows at least as fast as the *square root* of request arrival rate, and that the required server bandwidth for any protocol providing delayed service grows *linearly* with the inverse of the start-up delay. We also study how limited client receiving bandwidth may impact scalability. Finally, we propose practical and very simple delivery protocols that require server bandwidth very close to the lower bound. These protocols provide immediate service to clients, and they assume only limited client receiving bandwidth.

The paper is organized as follows. In Section 2, we present some background knowledge and related work on stream merging and periodic broadcasting techniques. In Section 3, we derive the lower bounds on required server bandwidth under a simple non-sequential access model. In Section 4, we present simulation results that validate our analytical results under more realistic non-sequential access models. In Section 5, we study the impact of limited client receiving bandwidth. In Section 6, we present optimized multicast delivery protocols for non-sequential access. We conclude in Section 6 with a summary and directions for future work.

## 2 Background and Related Work

This section briefly describes two previous techniques, namely stream merging and periodic broadcasting which utilize multicast delivery to serve streaming media objects. We present results from previous work on the scalability of these techniques when streaming accesses are sequential. In addition, we introduce a non-sequential access model (and notations thereof) used in this paper.

### 2.1 Stream Merging

In stream merging, a server immediately delivers the object in response to a client’s request. This means that the server initiates a stream for the client. However, assuming that the client receiving bandwidth is higher than the object’s playback rate,<sup>1</sup> it is possible for the client to listen to a second ongoing stream of the same object, initiated by an earlier client. As time goes by, it is possible that the first stream becomes no longer necessary since its future content would have been already prefetched from the second stream. Thus, the client is able to join an ongoing multicast session by virtue of making-up the content it missed from that session using a dedicated stream. This process of merging with multicast sessions that started earlier can be repeated many times, giving rise to *hierarchical* stream merging [20] as opposed to the stream tapping/patching techniques where merging occurs only once for each client.

Figure 1 gives an example where three clients ( $A$ ,  $B$ , and  $C$ ) request an object at times 0, 3, and 4, respectively. Figure 1(a) assumes that the clients’ receiving bandwidth is twice the object playback rate.

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<sup>1</sup>It is often assumed that the client can receive up to two streams at same time.

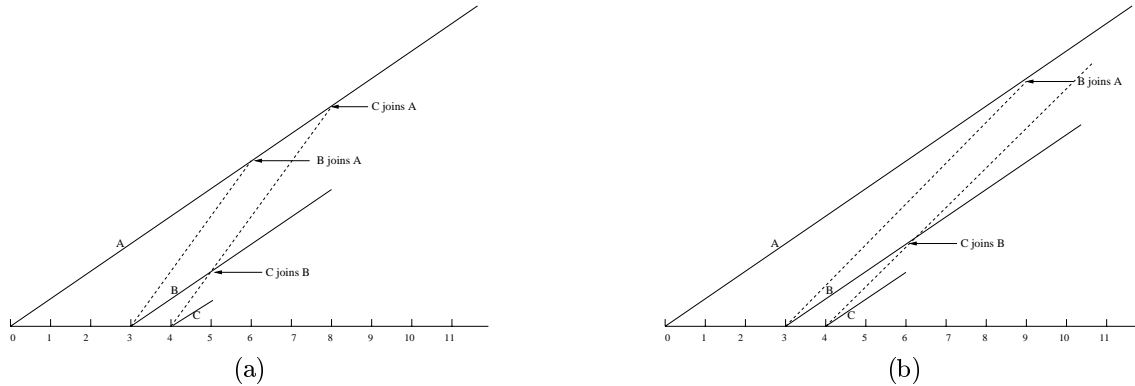


Figure 1: An example of hierarchical stream merging. In (a), client receiving bandwidth is twice the object playback rate. In (b), client receiving bandwidth is 1.5 times the object playback rate.

The server initiates one stream for each client. Client  $C$  also listens to the stream for  $B$  and prefetches data there. At time 5, the stream initiated for  $C$  is no longer necessary as  $C$  has already prefetched and will keep prefetching data from the stream for  $B$ . From this point on,  $C$  starts to listen to the stream for  $A$ . Notice that,  $B$  starts to listen to the first stream earlier.  $B$  virtually joins  $A$  at time 6 and  $C$  joins  $A$  at time 8. Also notice that, after time 6, the stream initiated for  $B$  is no longer necessary for  $B$ , but  $C$  has yet to retrieve the segment  $[3,5]$  of the object. The server may initiate a stream again for  $C$ , or simply prolongs the stream for  $B$  by two units of time until  $C$  joins  $A$  (as shown in the figure).

It is often the case that client receiving bandwidth is less than twice the object's playback rate. Bandwidth skimming protocols [19] works well in this case. Each stream is divided into  $k$  substreams using fine-grained interleaving, where  $k$  is a positive integer. Each substream is then transmitted on a channel with rate equal to  $1/k$  times the object playback rate. Stream merging is possible if clients can receive at least  $(k + 1)$  substreams at same time. Figure 1(b) gives an example when  $k = 2$ . In time interval  $[4,5]$ ,  $C$  receives two substreams of its own and prefetches only one substream of  $B$ . After that, in time interval  $[5,6]$ ,  $C$  need only receive one substream of its own and prefetches the two substreams of  $B$ . Eventually,  $C$  joins  $B$  at time 6. Similarly,  $B$  joins  $A$  at time 9, and  $C$  joins  $A$  at time 12. A salient feature of bandwidth skimming is that when client receiving bandwidth is slightly higher than the object playback rate (e.g., by 25%), the required server bandwidth is still comparable to that under unlimited receiving bandwidth assumption.

It has been shown that under both unlimited and limited receiving bandwidth assumptions, the required server bandwidth increases logarithmically with request arrival rate [20]. Thus, stream merging substantially outperforms stream tapping/patching techniques where the required server bandwidth increases as the square root of request arrival rate [22, 20].

## 2.2 Periodic Broadcasting

In periodic broadcasting schemes, a long object is divided into a series of segments with increasing sizes. Each segment is periodically broadcasted on a dedicated channel. When a client is playing an earlier segment, later segments are prefetched into the client's local buffer. To make this possible, the client must have higher receiving bandwidth than the object playback rate. Like stream merging, it is often assumed that the clients can receive two streams/segments at the same time. The segment size progression is made such that once the client starts playing the first segment, the whole object can be played out continuously.

Two important performance metrics of periodic broadcasting protocols are the required server bandwidth and the start-up delay. The required server bandwidth is equal to the number of segments, which is fixed, independent of request arrival rate. The maximum start-up delay is equal to the duration of the first segment. A desirable property of periodic broadcasting protocols is that the small first segment permits a small start-up delay while the larger later segments allow the total number of segments to remain small. To achieve the best tradeoffs between these two metrics, a broadcasting protocol need to find the quickest segment size progression.

Various periodic broadcasting protocols have been proposed in the literature. To understand the general idea behind these protocols, it suffices to describe one example, the *Skyscraper broadcasting* [28] protocol. Skyscraper broadcasting assumes that client receiving bandwidth is twice the object playback rate. The series of segment sizes is  $\{1, 2, 2, 5, 5, 12, 12, 25, 25, 52, 52, \dots\}$ . The broadcast schedule with seven segments is shown in Figure 2. The figure shows that two clients, starting in time interval  $(1, 2)$  and  $(16, 17)$ , respectively, are served with delay less than one unit of time, and henceforth can continuously play out the object. These two clients have different transmission schedules, as shown by the shaded segments; none of them needs to receive more than two segments at any time.

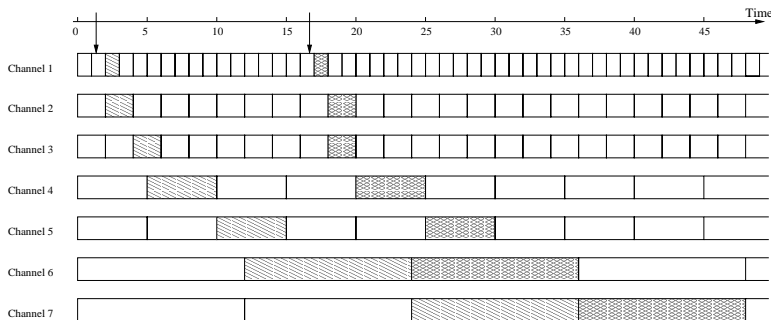


Figure 2: The schedule of Skyscraper broadcasting with 7 segments. The transmission plans for two clients are shown by the shaded segments. Each client receives at most two segments at the same time, and can continuously play out the object after a start-up delay smaller than the duration of the first segment.

The segment size progression of Skyscraper broadcasting has the following property: the size is at least doubled in every two steps. Different broadcasting protocols may have different segment size progressions, e.g., geometric series and Fibonacci series, but it is common that the size increases *exponentially*. Thus, the total number of segments (required server bandwidth) is a logarithmic function of the inverse of the first segment size (start-up delay).

### 2.3 Notations and Assumptions

Some of the notations used in this paper are listed in Table 1. Let  $T$  be the length of an object in bytes. Assuming the object has constant bit-rate of one byte per unit time, its duration is also  $T$  units of time. We consider the following simple model for non-sequential accesses. Request arrivals follow a Poisson process with arrival rate  $\lambda$ . Each request is for a segment of size  $S$  which starts from a random point in the object. We assume  $S < T$ . For simplicity, we assume that the object is cyclic, which means that access may proceed past the end of the object by cycling to the beginning of the object. Parameters  $T$ ,  $\lambda$ , and  $S$  uniquely specify a workload.

For ease of presentation, we introduce two other quantities  $N$  and  $M$ , which are derived from the three basic parameters  $T$ ,  $\lambda$ , and  $S$ . Let  $N$  denote the average number of clients being serviced at the same time. It is not difficult to show that  $N = \lambda S$  by Little's law. To assess the scalability of a multicast delivery

protocol, it is customary to find out how the server bandwidth  $B$  grows as a function of  $N$ . Similarly, let  $M$  denote the number of requests over a period of time  $T$ . Again, it follows that  $M = \lambda T$ . Notice that by definition,  $M > N$ .

Symbol	Definition
$T$	object duration (or length in bytes, assuming one byte per unit time)
$\lambda$	client request arrival rate
$S$	duration of each request
$N$	average number of clients requesting the object at same time, $N = \lambda S$
$M$	average number of requests arrived in $T$ , $M = \lambda T$ .
$B$	required server bandwidth (in units of object playback rate)
$d$	maximum start-up delay for each request
$n$	client receiving bandwidth (in units of object playback rate)

Table 1: Notations used throughout this paper.

Let  $d$  denote the maximum delay before service for a request is started. Under an immediate service assumption,  $d = 0$ . Thus, immediate service is a special case of delayed service. For clarity, in our analysis of the next section, we first consider immediate service, and then consider the more general delayed service.

Let  $n$  denote the client receiving bandwidth in units of object playback rate. For example,  $n = 2$  means client can receive two streams concurrently. We first assume that  $n$  is unlimited in the derivation of the lower bound on the required server bandwidth. In Section 5, we use simulations to show that when client receiving bandwidth is limited, the required server bandwidth increases slightly.

Finally, we assume that the clients have large enough buffer, considering that storage is not expensive. Under this assumption, clients can always keep prefetched data in their buffer.

## 2.4 Scalability of Multicast for Sequential Access

For sequential access, requests start from the beginning of the object and continue uninterrupted until the end. Thus,  $S = T$ . Eager *et al.* [20, 33] derived a tight lower bound on the required server bandwidth for any protocol (including stream merging) that provides immediate service. The lower bound is:

$$B_{minimum}^{immediate,sequential} = \int_0^T \frac{dx}{x + 1/\lambda} = \ln(N + 1). \quad (1)$$

The bound is derived by considering an arbitrarily small portion of the object at offset  $x$ . This portion is multicasted. Later requests may join the multicast, until the first request after time  $x$  which has missed this portion. On average, the server needs to multicast this portion again after time  $x + 1/\lambda$ . This bound can be extended by adding a start-up delay  $d$  as follows:

$$B_{minimum}^{delay,sequential} = \int_0^T \frac{dx}{x + d + 1/\lambda} = \ln\left(\frac{N}{\lambda d + 1} + 1\right). \quad (2)$$

For periodic broadcast protocols which assume arbitrary large  $\lambda$ , the above lower bound is:

$$B_{minimum}^{periodic,sequential} = \ln\left(\frac{T}{d} + 1\right). \quad (3)$$

In summary, with sequential access, (1) the lower bound on the required server bandwidth for any protocol providing immediate service grows logarithmically with request arrival rate, and (2) the lower

bound on the required server bandwidth for any protocol providing delayed service grows logarithmically with the inverse of the start-up delay. These results provide the basic scalability arguments of multicast delivery under a sequential access model.

### 3 Scalability of Multicast Delivery for Non-Sequential Access

In this section, we consider non-sequential access and derive tight lower bounds on the required server bandwidth for any protocol providing immediate service and delayed service. We assume that client receiving bandwidth is unlimited.

#### 3.1 Scalability of Immediate Service Protocols

We consider protocols that provide immediate service under the simple non-sequential access model described in the last section. Let us consider an arbitrarily small portion of the object, say a byte. Assume that at time 0, this byte is multicasted. The question is, when does it need to be multicasted again?

Consider the random variable  $\tau$  which is the time elapsed until this byte *must* be multicasted again—i.e.,  $\tau$  is the latest point in time beyond which a request would be delayed if the byte were not multicasted again. Clearly, at time  $\tau$  this byte must be immediately needed by some request because, otherwise, the multicasting of the byte could have waited, which by definition of  $\tau$  is not the case. Such a request must have been initiated after time 0 because, otherwise, the byte could have been retrieved from the multicast at time 0. Our ultimate goal is to compute how frequently the byte is served—i.e. the expectation of  $\tau$ . To do so, it suffices to derive the probability density function of  $\tau$ , denoted  $f(\cdot)$ . We do so below.

Consider the arrival process  $\{X\}$ , where event  $X$  is the playout of the byte by some request. It is obvious that this arrival process is a Poisson process with an arrival rate  $\Lambda = N/T$ . That is, on average the byte is played out  $N$  times in  $T$ . As we explained earlier, the playout of the byte by some request at a given moment does not necessarily mean a multicast of the byte at that precise moment. Thus, what we are interested is another arrival process—namely those arrivals in  $\{X\}$  that necessitate that the byte be *multicast* again. Let  $\{X'\}$  denote such an arrival process and let  $\Lambda'$  denote the arrival rate for that process.

Arrivals in  $\{X'\}$  are clearly a subset of arrivals in  $\{X\}$ . Specifically, an arrival in  $\{X\}$  that could have retrieved the byte at time 0 must be excluded from  $\{X'\}$  since such an arrival would not require a re-multicasting of the byte at time  $\tau$ . Assume that an arbitrary  $X$  occurs at time  $x$ . If  $x \leq S$ , then with probability  $\frac{x}{S}$  it is also an event of  $\{X'\}$ . If  $x > S$ , then  $X$  is certainly (with probability 1) an event of  $\{X'\}$ . To summarize, the arrival rate  $\Lambda'$  is a function of the arrival time  $x$ .

$$\Lambda'(x) = \begin{cases} \Lambda x/S, & \text{if } x \leq S \\ \Lambda, & \text{if } x > S \end{cases}$$

We are now ready to derive the marginal and density functions of the random variable  $\tau$ . To do so, we first compute the expected number of events  $X'$  before time  $x$ .

$$\begin{aligned} \alpha(x) &= \int_0^x \Lambda'(x) dx \\ &= \begin{cases} \frac{\Lambda x^2}{2S}, & \text{if } x \leq S \\ \Lambda(x - \frac{S}{2}), & \text{if } x > S \end{cases} \end{aligned}$$

Notice that the probability that there is no arrival over time interval  $(0, x)$  is equal to  $e^{-\alpha(x)}$  since the

arrivals are independent. Hence, the marginal distribution function of  $\tau$  is:

$$\begin{aligned} F(x) &= P\{\tau > x\} \\ &= 1 - P\{\text{no arrival in interval } (0, x)\} \\ &= \begin{cases} 1 - e^{-\frac{\Lambda x^2}{2S}}, & \text{if } x \leq S \\ 1 - e^{-\Lambda(x-\frac{S}{2})}, & \text{if } x > S \end{cases} \end{aligned}$$

Consequently, the probability density function is:

$$\begin{aligned} f(x) &= \frac{dF(x)}{dx} \\ &= \begin{cases} \frac{\Lambda x}{S} e^{-\frac{\Lambda x^2}{2S}}, & \text{if } x \leq S \\ \Lambda e^{-\Lambda(x-\frac{S}{2})}, & \text{if } x > S \end{cases} \end{aligned}$$

The remainder of the derivation is straightforward. We compute the expectation of  $\tau$  as follows

$$\begin{aligned} E[\tau] &= \int_0^\infty x f(x) dx \\ &= \sqrt{\frac{2S}{\Lambda}} \gamma\left(\frac{3}{2}, \frac{\Lambda S}{2}\right) + e^{-\frac{\Lambda S}{2}} \left(S + \frac{1}{\Lambda}\right), \end{aligned}$$

where the incomplete gamma function  $\gamma(a, b)$  is defined as  $\int_0^b x^{a-1} e^{-x} dx$ . Finally, we obtain the average required server bandwidth as

$$\begin{aligned} B &= \frac{T}{E[\tau]} \\ &= \frac{T}{\sqrt{\frac{2S}{\Lambda}} \gamma\left(\frac{3}{2}, \frac{\Lambda S}{2}\right) + e^{-\frac{\Lambda S}{2}} \left(S + \frac{1}{\Lambda}\right)}. \end{aligned}$$

Substituting  $\Lambda$  with  $\frac{N}{T}$  and  $S$  with  $\frac{NT}{M}$ , we obtain the follows

$$B = \frac{1}{\sqrt{\frac{2}{M}} \gamma\left(\frac{3}{2}, \frac{N^2}{2M}\right) + e^{-\frac{N^2}{2M}} \left(\frac{N}{M} + \frac{1}{N}\right)}. \quad (4)$$

This above, seemingly complex result can be greatly simplified. When  $N^2 \gg 2M$ , the incomplete gamma function  $\gamma\left(\frac{3}{2}, \frac{N^2}{2M}\right)$  approaches the complete gamma function  $\gamma\left(\frac{3}{2}, \infty\right) = \sqrt{\pi}/2$  very fast. In addition, since  $e^{-\frac{N^2}{2M}}$  approaches zero very fast,  $e^{-\frac{N^2}{2M}} \left(\frac{N}{M} + \frac{1}{N}\right)$  is insignificant. Hence,  $B \approx \sqrt{\frac{2M}{\pi}} \approx 0.797\sqrt{M}$ . This means that when  $M$  is of the same order as  $N$ , the required server bandwidth is at the order of  $\sqrt{N}$ . This lower bound is much higher than the logarithmic bandwidth requirement of stream merging for sequential requests.

Generally, when  $M$  increases,  $B$  also increases. For example, when  $2M = N^2$ , we compute the lower bound to be  $B \approx 0.54N$ , which is comparable to the required server bandwidth under a unicast service. Further increasing  $M$  results in diminishing advantage of multicast delivery, especially when multicast overhead is taken into consideration.

For the general case, it is easy to numerically solve equation (4). We have done so by varying  $N$  from 1 to 1,000 and varying  $M$  from  $N$  to  $100N$ . The results are shown in Figure 3. From Figure 3(a),

we observe that the required server bandwidth increases very fast when  $M$  increases ( $S$  decreases since  $S = NT/M$ ). Eventually, it is close to that of a unicast service. Notice that for sequential access, stream merging techniques can achieve the required server bandwidth lower bound  $\log(N + 1)$ , which would be at the bottom of the plot (not shown here). Figure 3(b) shows the same plot except that the axis are in log-scale. We observed that the log-value of the lower bound on bandwidth is approximately linear to that of  $N$  and  $M$ . This is because of the power-law relationship between  $B$  and  $N$ : the lower bound on bandwidth is at the order of  $\sqrt{N}$  when  $M$  is close to  $N$ , and when  $M$  increases to the order of  $N^2$ , the lower bound increases to the order of  $N$ .

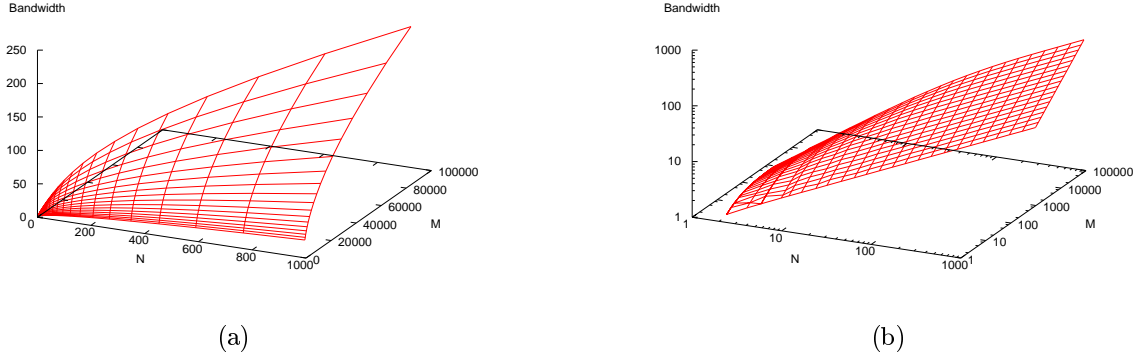


Figure 3: Lower bound on required server bandwidth for immediate service protocols, varying with the number of simultaneous requests  $N$  and segment request arrival rate  $M$ : (a) Linear scale, (b) Log scale.

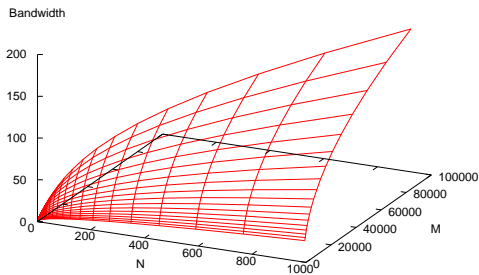
### 3.2 Scalability of Delayed Service Protocols

We now focus on the more general case—protocols that provide service within a fixed delay. We use the non-sequential access model described in the last section. Requests are satisfied in a slightly different way. Each client tolerates waiting for an interval of  $d$  time units (bytes) before it plays the requested segment of the object. During this interval, the client joins other streams to retrieve the bytes that will be played. Once the client starts to play the object, it continues retrieving later bytes whenever available. The client initiates a stream for those bytes that can not be retrieved from other ongoing streams. It is obvious that the immediate service model is a special case of this delayed service model when  $d = 0$ .

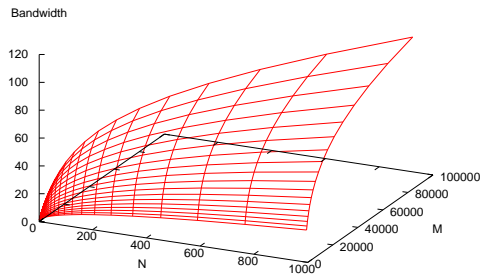
As before, assume that an arbitrary byte is multicasted at time 0. Let  $\tau$  denote the time when the byte must be multicasted again. Compared to the immediate service case, the expectation of  $\tau$  increases by  $d$ . Hence, we derive the lower bound of the required server bandwidth to be

$$B = \frac{1}{\sqrt{\frac{2}{M}} \gamma\left(\frac{3}{2}, \frac{N^2}{2M}\right) + e^{-\frac{N^2}{2M}} \left(\frac{N}{M} + \frac{1}{N}\right) + \frac{d}{T}}. \quad (5)$$

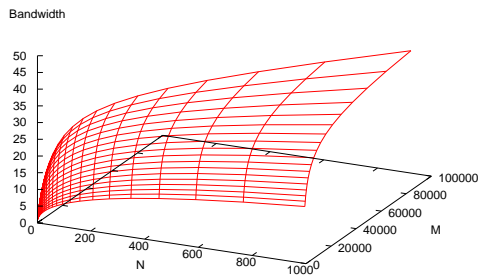
If  $d = 0$ , this lower bound is consistent with equation (4). When  $d/T$  is still very small compared to  $\sqrt{1/M}$ , this lower bound is close to that of immediate service. Generally, when  $d$  increases, this lower bound decreases. However, the rate at which the lower bound decreases is no higher than the inverse of  $d$ . This suggests that the use of delayed service is less effective under a non-sequential access model than it is under a sequential access model. Recall that for sequential access, periodic broadcasting techniques reduce bandwidth requirement linearly by increasing service delay logarithmically.



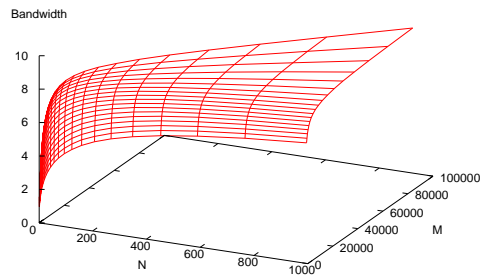
(a)  $d = 0.001T$



(b)  $d = 0.005T$



(c)  $d = 0.02T$



(d)  $d = 0.1T$

Figure 4: Lower bound on required server bandwidth for delayed service protocols when the delay is set to several typical values.

It is straightforward to numerically solve equation (5). We have done so by varying  $N$  from 1 to 1,000, varying  $M$  from  $N$  to  $100N$ , and choosing typical values for  $d$  ( $0.001T$ ,  $0.005T$ ,  $0.02T$ , and  $0.1T$ ). Results are shown in Figure 4. We observe that when  $d$  is small, for example  $d = 0.001T$ , the lower bound on bandwidth is close to that of immediate service shown in Figure 3. When  $d$  increases, the lower bound decreases. For all the cases, the lower bound is no larger than  $\frac{T}{d}$ . It is important to notice that, when  $d$  is larger, the lower bound approaches  $\frac{T}{d}$  faster as  $N$  and  $M$  increase. Further increases of  $N$  and  $M$  do not result in higher bandwidth requirement.

## 4 Simulation Results

The lower bounds of the previous section were derived using an ideal non-sequential access model assuming independent arrivals and constant segment sizes. To validate these lower bounds and establish their robustness under more realistic conditions, we performed extensive simulations which we describe in this section.

## 4.1 Immediate Service

We have written a simulator for a protocol that provides immediate service. Assuming unlimited client receiving bandwidth, a client retrieves later bytes from ongoing streams whenever possible. If a byte cannot be obtained in this way before the time of play, it is multicasted as late as possible (at the time of play) so that other clients can fully utilize it. We varied a number of simulation parameters:  $N$  from 1 to 1,000 and  $M$  from  $N$  to  $100N$ . The results are shown in Figure 5.

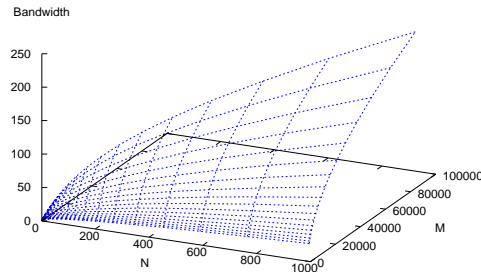


Figure 5: Required server bandwidth for immediate service protocols obtained through simulation, varying with the number of simultaneous requests  $N$  and segment request arrival rate  $M$ .

Comparing Figure 5 to Figure 3, we find that in all cases, the average required server bandwidth obtained through simulation is very close to that of our numerical analysis. This is expected since the derived lower bound is *tight*.

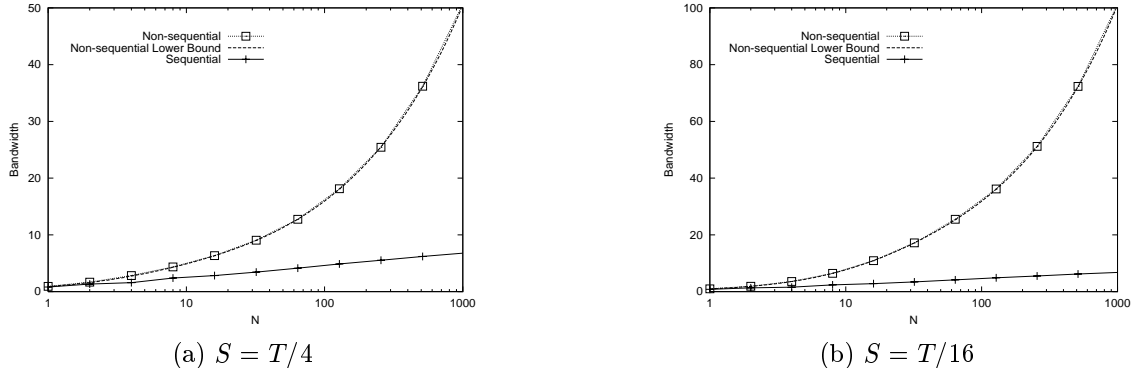


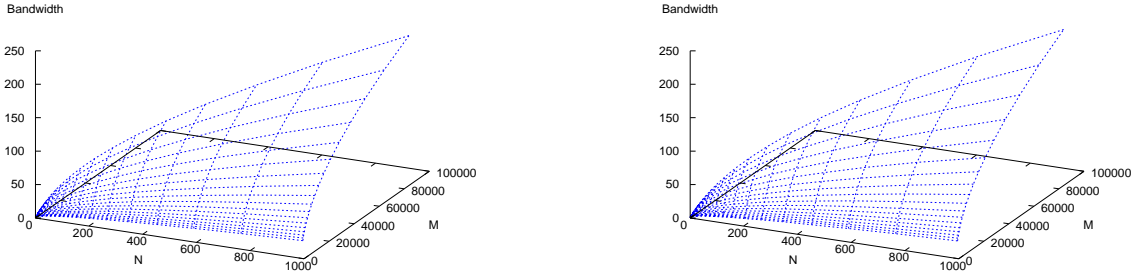
Figure 6: Comparison of the scalability of multicast delivery for immediate service protocols under sequential and non-sequential access models. Non-sequential requests are generated such that each request starts from a random point in the media object.

Figure 6 shows the average bandwidth for some special cases. The figure shows the required server bandwidth obtained through simulation, the lower bound, and the required server bandwidth (also obtained through simulation) for sequential access for comparison purposes. In particular, (a) shows the case when  $M = 4N$ . That is  $S = T/4$ , i.e., each client randomly requests a segment whose size is equal to one-fourth of the whole object. (b) shows the case  $M = 16N$ . That is  $S = T/16$ .

From Figure 6 we observe that the required server bandwidth for non-sequential access increases quite fast. Both the results from simulation and the lower bound are much higher than those for sequential

access. We have also compared the required server bandwidth for sequential access with its theoretical value (not shown),  $\log(N + 1)$ , and found that they match well. For sequential access, the required server bandwidth increases logarithmically with request arrival rate. For non-sequential access, the required server bandwidth increases with the square root of  $N$ . In addition, we observed that when  $M = 16N$  the required server bandwidth is roughly twice that obtained when  $M = 4N$ . This is consistent with the fact that the lower bound approximately increases as the square root of  $M$ .

**Effect of Variable Segment Size:** Note that in our analysis (last section) and in the above simulations, we consider that the segment size is a constant  $S$  equal to  $NT/M$ . In more realistic workloads, the segment size can vary according to some distribution. Thus, one question is whether the lower bound still holds for various distributions of  $S$ . To answer this question, we generated segment sizes that follow a uniform distribution and a Pareto distribution, respectively. The mean segment size is  $S = NT/M$ . For the uniform distribution, we let the segment size vary between 0 and  $2S$ . For the Pareto distribution, we let its shape parameter  $\alpha = 2.0$  and computed its scale parameter  $k$  to ensure a mean segment size of  $S = NT/M$ . We have also performed simulations with other values of  $\alpha$  and found that the corresponding effects on the required server bandwidth was negligible.



(a) Segment size follows Uniform distribution.

(b) Segment size follows Pareto distribution.

Figure 7: Required server bandwidth for immediate service protocols obtained through simulation, varying with the number of simultaneous requests  $N$  and segment request arrival rate  $M$ . Mean segment size is  $NT/M$ .

Figure 7 shows the results we obtained from simulations with variable segment sizes. Comparing these results with those obtained with a constant segment size (shown in Figure 5) and the lower bounds (shown in Figure 3), we found that the differences are almost negligible. We conclude that with variable segment size, the required server bandwidth also increases as the square root of request arrival rate.

**Effect of Request Correlations:** Our simulations so far were obtained under an assumption that requests are not correlated and that they start anywhere in the object. In the set of simulations we describe next, these assumptions were removed. To do so, we generated requests that exhibit characteristics observed in real streaming access workloads. Specifically, we consider the following model for client inter-activity. Each client starts a *session* from the beginning of an object. After receiving a segment of the object (the ON-segment), the client skips a portion of the object (the OFF-segment). This process repeats until a request or jump goes beyond the last byte of the object.

In prior studies that characterized streaming access [34, 4], it has been observed that the distributions of ON-segments tend to be heavy-tailed and that the Pareto distribution was found to be a close fit. Thus, in our simulations, we generated requests that exhibited such properties. For ON periods, we used a Pareto distribution with parameter  $\alpha = 2$  and we set the scale parameter  $k$  to achieve an average segment size of

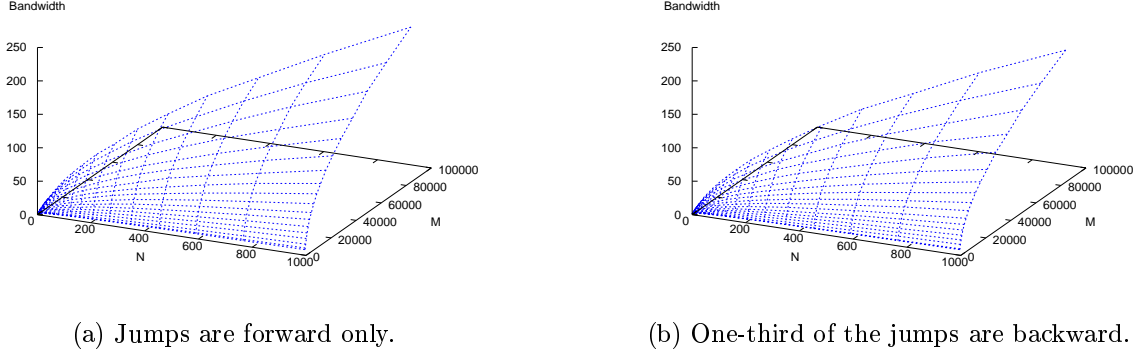


Figure 8: Required server bandwidth for immediate service protocols obtained through simulation, varying with the number of simultaneous requests  $N$  and segment request arrival rate  $M$ . Requests are generated using an ON-OFF model. ON-segment (request duration) and OFF-segment (jump distance) follow Pareto distribution.

$S = NT/M$ . For OFF periods, we also used a Pareto distribution with parameter  $\alpha = 2$  and we set the scale parameter  $k$  to achieve an average jump distance of  $S/2$ . Results from these simulations are shown in Figure 8. We have also experimented with other settings, but the results were quite similar.

Figure 8(a) shows the results when only forward jumps are allowed. That is, each client requests a segment and skips a segment to continue, and so on until the end of the object. Figure 8(b) shows the results when 33% of the jumps were backward jumps. Comparing these results to the lower bound in Figure 3 and the simulation results in Figure 5 and Figure 7, we found the required server bandwidth to be very close.

Comparing Figure 8(b) to (a), we found that with backward jumps, the required server bandwidth decreases slightly. We have estimated the difference and found it to be up to 15%. This can be explained as follows. In our simulation, we assumed that each client has large enough buffer to keep the segments of the object that have been played. With backward jumps, it is possible that the client plays a portion of the object kept in the buffer. This is equivalent to introducing a start-up delay for the request. Hence, it reduces the required server bandwidth. Nevertheless, the effects of backward jumps remain fairly limited.

From Figure 8, we also observe that when  $M$  is small, the required server bandwidth appears lower than those in Figure 3, 5, and 7. This is expected. When  $M$  is smaller, the average request duration is closer to  $T$ , and since the clients start to retrieve the object from the beginning, requests tend to be “sequential”. To understand this more clearly, we zoom in on the plot in Figure 8(a) and, in Figure 9, we show several special cases when  $M = 2N$ ,  $M = 4N$ ,  $M = 8N$ , and  $M = 16N$ . Note that when  $M$  is smaller, e.g.,  $M = 2N$ , the average request duration is  $T/2$ . In this case, access is closer to “sequential”, and the required server bandwidth is closer to the lower bound for sequential access. This is evident in Figure 9(a). When  $M$  increases, access becomes “less sequential”, resulting in a required server bandwidth that is more accurately predicted by the lower bound for non-sequential access. This is evident in Figure 9(b)-(d). Generally speaking, with only very few jumps during the time of a complete object playout, the required server bandwidth increases at least as the square root of request arrival rate.

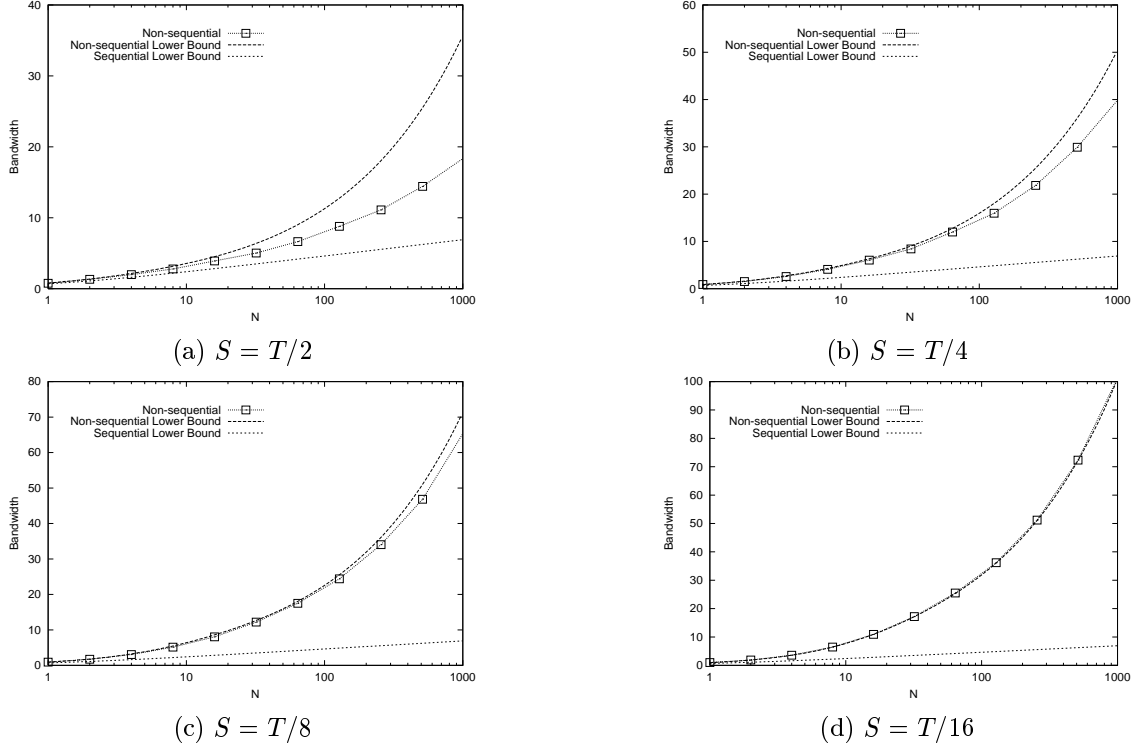


Figure 9: Required server bandwidth for immediate service protocols obtained through simulation, varying with the number of simultaneous requests  $N$ . Request arrival rate  $M$  is set to several values. Requests are generated using an ON-OFF model.

## 4.2 Delayed Service

We have also used simulations to validate the required server bandwidth of delayed service. We varied simulation parameters  $N$  from 1 to 1,000 and varied  $M$  from  $N$  to  $100N$ . We chose typical values for  $d$ —namely  $0.001T$ ,  $0.005T$ ,  $0.02T$ , and  $0.1T$ . For simulation run, we first generated a sequence of requests. Each request is delayed for time  $d$ . During the delay, later bytes are fetched from ongoing streams whenever possible. When a client is playing the object, later bytes can be still retrieved from ongoing streams. Any byte that cannot be obtained in this manner is retrieved from the server directly, and *as late as possible* such that later clients can fully utilize it. The results of our simulations are shown in Figure 10.

Comparing Figure 10 with Figure 4, we found that in all cases, the average required server bandwidth obtained through simulation is close to that we obtained through analysis.

Figure 11 shows how the required server bandwidth varies with delay  $d$ . We choose  $M = 4N$ , i.e., each request retrieves one-fourth of the whole object. Figure 11(a) shows results when  $N = 50$ , representing a less popular object, and Figure 11(b) shows the case when  $N = 1,000$ , representing a highly popular object. In each case, we plot the lower bound on the required server bandwidth for non-sequential access, as well as that obtained through simulations. In addition, for comparison purposes, we also plot the bandwidth-delay relationship for sequential access. In particular, we plot the minimum required server bandwidth for periodic broadcasting in equation (3), and the required server bandwidth measured from simulation for stream merging (assuming unlimited client receiving bandwidth).

Our observations are summarized as follows. First, the required server bandwidth under a non-sequential access model is much higher than that under a sequential access model. The difference is

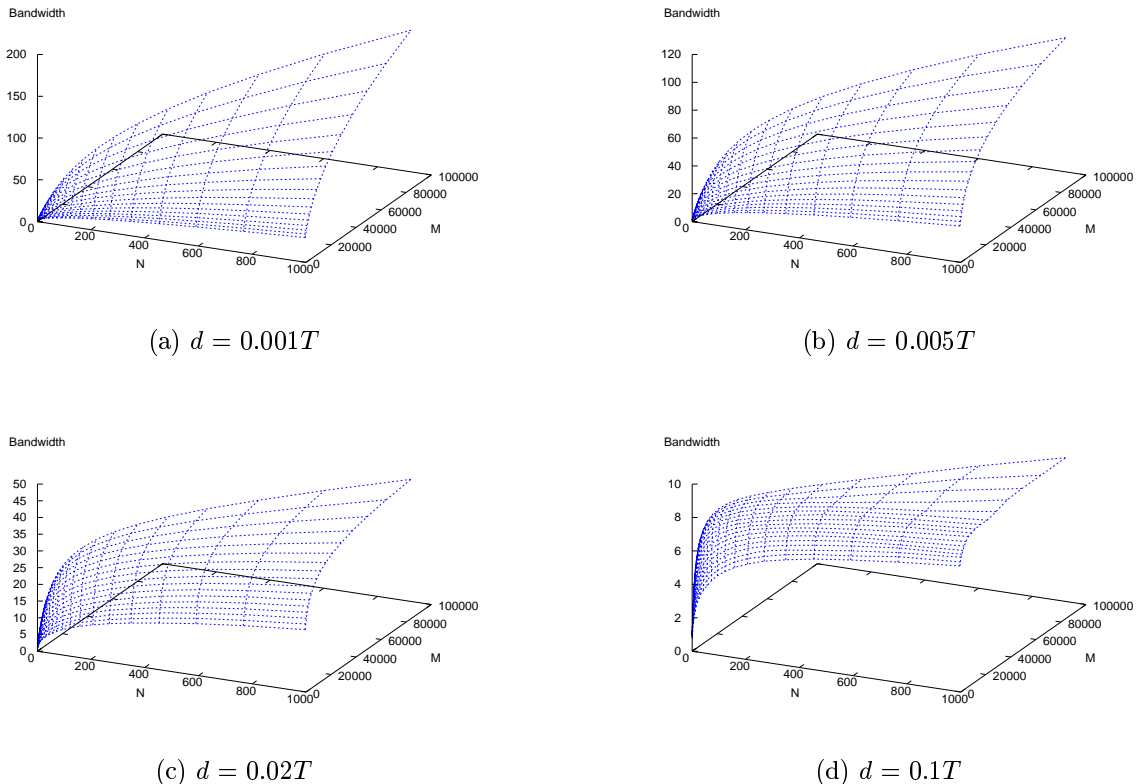


Figure 10: Required server bandwidth obtained through simulation when the delay is set to several typical values.

more pronounced for more popular objects. Notice that when  $d \rightarrow 0$ , the lower bound on required bandwidth under a non-sequential access model is close to  $\sqrt{M/2}$  which is much higher than the  $\log(N + 1)$  lower bound under a sequential access model. Second, under a sequential access model, stream merging techniques achieve lower required server bandwidth than broadcasting when delay is small. This is more obvious for less popular objects. This is because stream merging has a lower bound of  $\log(N + 1)$  when  $d \rightarrow 0$ , whereas broadcasting techniques have a lower bound of  $\log(\frac{T}{d} + 1)$ . So when  $d < \frac{T}{N}$ , the required server bandwidth for broadcasting is higher. In fact, in this figure, the simulation results for stream merging under a sequential access model are close to the bound given in equation (2).

## 5 The Impact of Limited Client Bandwidth

Previous sections assumed that clients have unlimited receiving bandwidth ( $n = \infty$ ). This section uses simulations to study how limited client receiving bandwidth affects the scalability of multicast delivery. We consider immediate service protocols. In order for multicast delivery to be possible, the client receiving bandwidth  $n > 1.0$  must hold.

In sequential-access context, there are advanced techniques for scheduling client requests using multicast streams. For example, Eager *et al.* [18] proposed several *hierarchical multicast stream merging* techniques which progressively merge asynchronous client requests into larger and larger groups. One problem that must be addressed relates to the scheduling of these mergers. Several heuristic policies were proposed. In

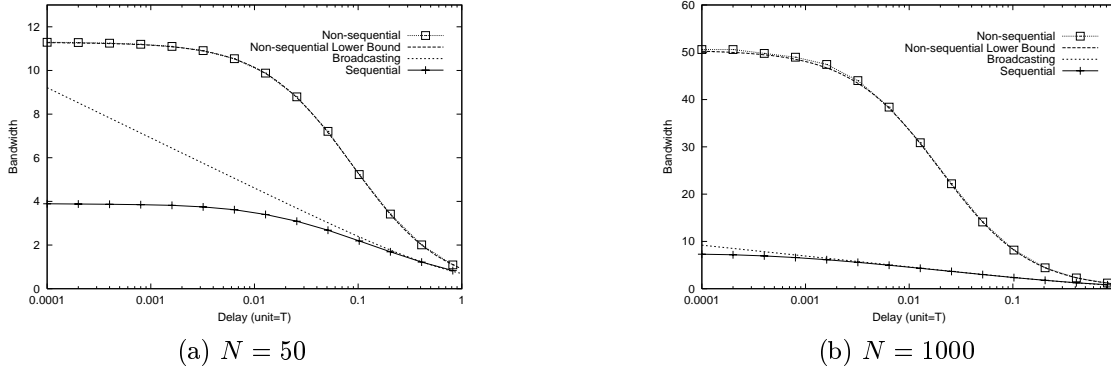


Figure 11: Required server bandwidth varying with start-up delay.

particular, assuming  $n = 2$ , the *closest target* policy requires each client to join the most recently initiated earlier stream that is still alive. Simulations showed that this policy performs very close to the off-line optimal algorithm (with known client request arrivals in advance), which is obtained by solving a dynamic programming problem.

Under a non-sequential access model, we modify the closest target merging policy when  $n = 2$ . The key point is how we define the *closest target* for each client. Since the requests may start anywhere in the object, the closest target is not necessarily the most recently initiated stream. Instead, we define the closest target of each client as the multicast stream that will be played by the client in the nearest future. The intuition behind this choice is that it is critical for the client to prefetch the portion of the data that will soon be played. In addition, the closest target will be redefined when the target itself is merged or is terminated.

When  $n < 2$ , we modify the *bandwidth skimming* technique [19]. Each multicast stream is divided into  $k$  substreams, where  $k$  is a positive integer. Each substream is then multicasted with rate equal to  $1/k$ -time the object playback rate. Each client is assumed to be capable of receiving at least  $(k + 1)$  substreams simultaneously (thus  $n = 1 + 1/k$ ). The closest target policy is then applied to the substreams: whenever the client has idle bandwidth, it listens to the substreams whose data will be played in the nearest future. The client may listen to up to  $(k + 1)$  substreams.

We developed a simulator for this stream merging/bandwidth skimming technique. Figure 12 shows the required server bandwidth we obtained through simulations in which we varied the number of concurrent clients ( $N$ ). The value of  $n$  is varied from 1.125 to  $\infty$ . In Figure 12(a), we set  $M = 4N$ , i.e.,  $S = T/4$ , each request is for one-fourth of the object. In Figure 12(b), we set  $M = 16N$ , i.e.,  $S = T/16$ .

From Figure 12, we observe that when a client's receiving bandwidth is limited, the required server bandwidth increases only slightly. For example, when  $N = 1,000$  and  $n = 1.5$  (i.e., one-third of the client bandwidth is used for prefetching), our simulations indicate that the required server bandwidth is about 1.69 times that required under unlimited client receiving bandwidth assumption ( $n = \infty$ ). When  $n = 2$ , our simulations indicate that the required server bandwidth is close to that under unlimited client receiving bandwidth assumption. We estimate that the difference is around 12% for large values of  $N$ . These results suggest that even with a limited client receiving bandwidth, it is possible for a protocol to have required server bandwidth that is quite close to its lower bound. In the next section, we study practical multicast delivery protocols that achieve this goal.

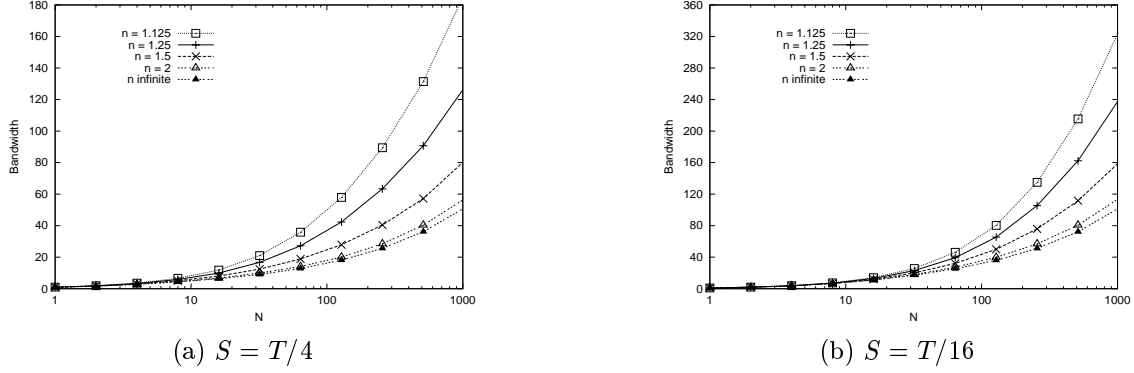


Figure 12: Required server bandwidth of immediate service protocols when client receiving bandwidth is limited.

## 6 Practical Multicast Delivery Protocols

The protocols considered in the previous sections either assume unlimited client receiving bandwidth or are too sophisticated to be practical. For example, in the modified closest target merging policy, each client may join and leave the multicast streams frequently. Such a behavior may incur high overhead on servers. In this section, we describe practical multicast delivery protocols and optimize them by minimizing the required server bandwidth.

### 6.1 Protocols

We consider the following protocol which provides immediate service to the clients. *The server multicasts an object for every interval of length  $x$ . Each client joins the temporally closest multicast stream. The missed portion of the requested segment is immediately unicasted from the server.* Such a protocol is simple in that for each request, the client need only join one multicast stream.

The above protocol is readily usable by a client whose receiving bandwidth is twice the object playback rate, i.e.,  $n = 2$ . Both the multicast and unicast streams are sent at playback rate. Assuming that a client requests a segment which was most recently multicasted  $t$  units of time ago, then the client receives a unicast stream of length  $t$ , while concurrently prefetching data from that multicast stream.

It is also easy to generalize this protocol for clients with lower receiving bandwidth, i.e.,  $1 < n < 2$ . We capitalize on the ideas from bandwidth skimming techniques. Namely, each stream (both unicast or multicast) is divided into  $k$  substreams using fine-grained interleaving, where  $k$  is a positive integer. Each substream is sent with rate equal to  $1/k$  time the playback rate. The clients can receive  $(k + 1)$  substreams (thus  $n = 1 + 1/k$ ). Assume a client requests a segment which was most recently multicasted  $t$  units of time ago. The client receives  $k$  unicast substreams immediately from the server and meanwhile it prefetches data from one multicast substream. Then,  $t$  units of time later, the client need only receive  $(k - 1)$  unicast substreams, and can prefetch two multicast substreams. Another  $t$  units of time later, the client need only receive  $(k - 2)$  can prefetch three multicast substreams, and so on. Eventually, no unicast substream is needed.

## 6.2 Optimization

To optimize our protocol, we determine the value of  $x$ , which controls the frequency of multicasting the object. Assume that each request is for a segment of constant length  $S$ . Now we compute the average cost of unicast. Assume a client requests a segment which was most recently multicasted  $t$  units of time ago. From the description of the protocols above, it is not difficult to find that the total duration of the unicast substreams is  $\sum_{i=1}^k it = \frac{k(k+1)}{2}t$ , assuming  $S \geq kt$ . On average this is equal to  $\frac{k(k+1)}{4}x$ . Since the sending rate is  $1/k$  times the playback rate, the number of bytes unicasted is  $\frac{k+1}{4}x$ . Over a period of time  $T$ , there are  $M$  requests, so there are  $\frac{(k+1)M}{4}x$  bytes unicasted. In addition, over a period of time  $T$ , the object is multicasted  $T/x$  times, so there are  $T^2/x$  bytes multicasted.

We are now ready to optimize our protocol by minimizing the total cost of the protocol over a period of time  $T$ . This cost is given by:

$$g(x) = \frac{(k+1)M}{4}x + \frac{T^2}{x}.$$

The optimal solution is  $g^* = \sqrt{(k+1)MT}$  when  $x^* = \frac{2T}{\sqrt{(k+1)M}}$ . This yields a required server bandwidth of  $\sqrt{(k+1)M}$ .

When  $k = 1$  and  $n = 2$ , the required server bandwidth is  $\sqrt{2M}$ , which is approximately 1.773 times the lower bound given in equation (4). This means that such a simple protocol needs less than twice the server bandwidth required for the rather impractical protocols we assumed in our simulations. Even when  $k$  increases (i.e.,  $n$  approaches unity), the required server bandwidth for this simple protocol increases only as the square root of  $k + 1$ . For example, when 33% of the client bandwidth is used for prefetching ( $k = 2$  and  $n = 1.5$ ), the required server bandwidth is only  $1.732\sqrt{M}$  which is about 2.173 times the lower bound.

Although it is possible to further decrease the required server bandwidth by using more sophisticated protocols, the payoff from such an exercise is fairly limited. Recall that in the last section, our simulation results have shown that when  $n = 1.5$ , the sophisticated earliest target first merging algorithm we discussed requires server bandwidth roughly equal to 1.69 times the lower bound—allowing only a limited “room for improvement” over the 2.173 times the lower bound achieved using the protocol described above.

## 7 Summary and Conclusion

In this paper, we have analytically derived the tight lower bounds on the required server bandwidth for protocols in a multicast environment when access to streaming objects is not sequential. In particular, we have shown that in such systems, the required server bandwidth for any protocol providing immediate service grows as the square root of request arrival rate, and that the required server bandwidth of any protocol providing delayed service is inversely proportional to the maximum allowable start-up delay. The robustness of our analytical results have been confirmed using extensive simulations under realistic workloads. Also, the impact of limited client receiving bandwidth was investigated. Finally, based on our findings, we proposed a practical, near-optimal multicast-based delivery protocol, which results in a server bandwidth requirement that is fairly close to its lower bound under both abundant and limited client receiving bandwidth assumptions.

Our findings suggest that for non-sequential access, multicast delivery is not a panacea for scalability. Therefore, for large-scale content delivery applications that require non-sequential access of large artifacts (e.g., interactive video delivery and real-time software distribution), we should seek alternative or complementary techniques (e.g. caching, buffering, and replication) that increase the scalability of streaming delivery mechanisms.

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