




Dynamics of Network Resource Management

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The Internet is ...




HUGE

- So HUGE that no one really knows how big
- But, rough estimates:
 - Users ~ 1.8B in 2009 (source: eTForecasts)
 - Web sites > 182M active in Oct 2008 (source: netcraft)
 - Web pages ~ 150B (source: Internet archive)




The Internet is ...




DYNAMIC

- Users log in and out
- New services get added
- Routing policies change
- Denial-of-Service (DoS) attacks
-




Motivation

- How to manage such a huge and highly dynamic structure like the Internet?
- How can we build Future networks?
 - Can't build and hope they work
 - Understand the **steady-state** and **dynamics** of what we are building
- **Need methodologies**
 - Optimization Theory
 - Control Theory
 -



Focus

- **Congestion Control**
- **Adopt techniques from**
 - Optimization Theory
 - Control Theory
- **With emphasis on "Modeling"**
- **Prices**
 - Congestion Prices
 - Exogenous Prices
 - non-load related, e.g. random wireless losses



An Optimization Theoretical Framework


Utilities and Prices
Kelly's Framework
Fairness Criteria
Discussion

Utility

- Life ... involves daily decisions
- Gas Prices are affecting these decisions
 - Drivers will observe prices, decide
 - Walk
 - Bike
 - Stay home
 - Take the subway
 - Drive

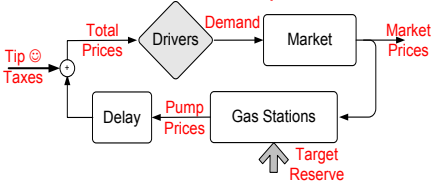
Can still go to the movies ☺
If it is raining

- Utility
 - How much driving means to me compared to other things in life?
 - Unknown to the gas stations
- Each driver has his/her own utility



A slightly bigger Gas Picture

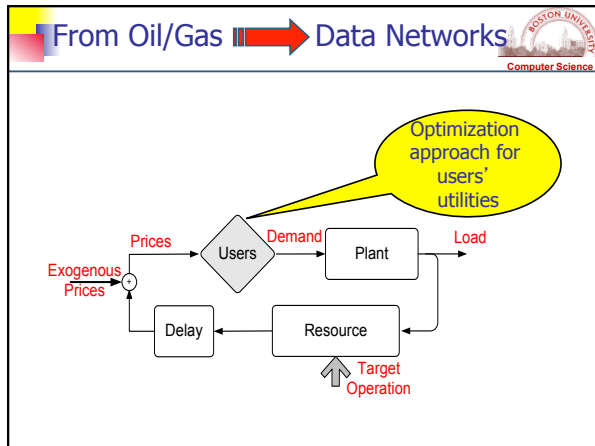
- Drivers, observe the gas price and drive the total demand
- Market (OPEC + Government + Oil companies), based on demand, sets the prices



- System is in equilibrium if demand is balanced with supply

From Oil/Gas → Data Networks

- Users drive the demand on the network
 - Have different Utilities
 - Download music, play games, make phone calls, deny service,...
- Network, observes the demand, sets prices
 - Price as real money
 - Smart Market [MV95], Paris metro [O97]
 - Price as a congestion measure
 - Queuing Delay, packet loss or marking, additional resources to be allocated
- What is the goal of Network Design? [S95]
 - Make users happy
 - Maximize the sum of Utilities for all users




Network users' Utilities

- Users have different utilities, however
 - Higher the rate, the better
 - Decreasing marginal utility
- Formally: Elastic traffic [S95]
 - User r has utility $U_r(x_r)$ when allocated $x_r > 0$ rate
 - $U_r(x_r)$ is an increasing function, strictly concave function of x_r
 - $U'_r(x_r)$ goes to ∞ as x_r goes to 0
 - $U'_r(x_r)$ goes to 0 as x_r goes to ∞

Network Model

- Consider a network of J resources
- Consider R the set of all possible routes
- Associate a route r with each user
- Define a 0-1 routing matrix A s.t.
 - $a_{jr} = 1$ if resource j is on route r
 - $a_{jr} = 0$ otherwise

1	0	1
0	1	0
0	0	0
1	0	1
0	1	0
1	0	0
0	1	1



An Optimization Problem [K97]

SYSTEM(U, A, C):

$$\max \sum_{r \in R} U_r(x_r)$$

subject to


$$Ax \leq C$$

over

$$x \geq 0.$$


C: Capacity vector
A: routing matrix
x: rates allocated

- A (unique) solution exists
- However, utilities are unknown to the network



Introducing prices ...

- Break the problem into:
 - R different problems, a problem for each user
 - 1 Network problem
- Prices act as a mediator between the network and the users
 - Prices can be used to measure utilities
 - Users choose an amount to pay for the service
 - Network, based on the load, charges a price



User Maximization Problem

- Let user r , pays w_r per unit time, to receive x_r proportional to w_r

$$\lambda_r = \frac{w_r}{x_r} \quad \left(\frac{\$/t}{b/t} = \$/b \right)$$
- λ_r is the charge per unit flow

USER $_r(U_r; \lambda_r)$:

$$\max U_r \left(\frac{w_r}{\lambda_r} \right) - w_r$$

over

$$w_r \geq 0.$$

Network Optimization Problem

- Let the network knows the vector W
- Then the Network Maximization problem:

$NETWORK(A, C; w):$

$$\max \sum_{r \in R} f(x_r, w_r)$$
 subject to

$$Ax \leq C$$
 over

$$x \geq 0.$$

Network Optimization Problem

- A Greedy network choice $\max \sum_{r \in R} x_r w_r$
- Indeed, for $w_r=1$, maximizes overall throughput
- But, lacks traditional fairness concepts
- Here is a simple example:

0
 6
 6
 Total = 12

Fairness criterion depends on the function that the network is optimizing for

Max-Min Fairness

- Fair**
 - all sources get an equal share on every link *provided they can use it*
- Efficient**
 - each link is utilized to the maximum load possible

F1
 150
 F2
 150
 F3
 150
 F4
 150
 (50, 50, 50, 100)

Fairness criterion (1/3)

- **Max-min Fairness**
 - No rate can increase, no matter how large, while decreasing another rate that is less than it, no matter how small
 - Absolute priority to small-rate users
- **X is proportionally fair if [K97]:**
 - Feasible $x \geq 0$ and $Ax \leq C$
 - For any other feasible vector x^* , the aggregate of proportional changes is zero or negative:
$$\sum_{r \in R} \frac{x_r^* - x_r}{x_r} \leq 0.$$

Fairness criterion (2/3)

- **X is weighted proportional fair if**

$$\sum_{r \in R} w_r \frac{x_r^* - x_r}{x_r} \leq 0.$$
 - A flow of $w=2$, is treated like 2 flows of $w=1$
- **Network would choose one of these**
 - $\max \min_{r \in R} x_r \implies$ Max-min Fairness
 - $\max \sum_{r \in R} \log x_r \implies$ Rates are proportionally fair
 - $\max \sum_{r \in R} w_r \log x_r \implies$ Rates are weighted proportionally fair

Fairness criterion (3/3)

▪ **In our previous example**

▪ **Maximizing total throughput**
● 0 ● 6 ● 6

▪ **Proportional allocation ($w_r=1$)**
● 2 ● 4 ● 4

▪ **Max min allocation**
● 3 ● 3 ● 3


General
Parameterized Utility
[MW00]

$$U(x) = \frac{x^{1-\alpha}}{1-\alpha}$$

← $\alpha \rightarrow 0$
(linear utility)


← $\alpha \rightarrow 1$
(log utility)

← $\alpha \rightarrow \infty$
(min utility)



Kelly [K97,K99,KMT98]

Computer Science



$NETWORK(A, C; w):$

$$\max \sum_{r \in R} w_r \log x_r \quad L(x, z; \mu) = \sum_{r \in R} w_r \log x_r + \mu^T (C - Ax)$$

 subject to


$$Ax \leq C \quad \frac{\partial L}{\partial x_r} = \frac{w_r}{x_r} - \sum_{j \in R} \mu_j$$

 over

$$x \geq 0.$$


$$x_r = \frac{w_r}{\sum_{j \in R} \mu_j}$$

- **Proof outline: Theory of constrained convex optimization and using Lagrange multipliers**
 - μ_j = cost incurred or shadow price of additional capacity (λ 's in earlier slides)
- **A solution exists**
 - X = weighted proportionally fair
 - Solves Network, User and System for log utility functions




Discussion

Computer Science




- **Just to recap**
 - Interested in maximizing the aggregate utilities
 - Network wouldn't know the utilities
 - Broke the problem into users and one network problem
 - So, we introduced the vector W as a mediator
 - Shown that a solution exists
 - Fairness criterion depends on the network maximization function




Discussion

Computer Science




- **But, we need to address few issues:**
 - Network does not know W
 - Network implicitly determines W from the user's behavior along its path, which is chosen by the network on behalf of the user
 - Or, Network puts an implicit weighting for relative utilities of different users
 - No central controller to know W and allocate rates

**Look into individual controllers
for the users and for the resources**



Network Dynamics & Control Theory Preliminaries

System Modeling and Feedback Control
TCP
AQM
TCP + RED



Control Problem


- **The basic control problem:** Control the output (results) for a given input

Inputs \Rightarrow Control System \Rightarrow Outputs

- **Examples:**

Price \Rightarrow User \Rightarrow Rate

Rates (Demand) \Rightarrow Resource \Rightarrow Prices



Questions to ask

- **Steady state**
 - What is the long range value of the output?
 - How far is it from the reference value?
- **Transient Response**
 - How does the system react to perturbations?
- **Stability**
 - Is this system stable?
- **Stability Margins**
 - How far is the system from being unstable?

Open-loop Control

- **There is no feedback**
 - Controlled directly by an input signal
- **Simple**
- **Example: Microwave**
 - Food will be heated for the duration specified
- **Not as common as closed-loop control**


Feedback (Closed-loop) Control

- **Feedback control is more interesting ...**
- **Multiple controllers may be present in the same control loop**


Feedback (Closed-loop) Control

- **Feedback control makes it possible to control well even if**
 - We don't know everything
 - We make errors in estimation/modeling
 - Things change
- **Flow/congestion control example:**
 - No need to EXACTLY know
 - Number of users
 - Connections' arrival rate
 - Resource's service rate
 - Continually measure & correct

Feedback (Closed-loop) Control




- Feedback delay is usually associated with feedback control




- Feedback delay:** Time taken from the generation of a control signal until the process reacts to it and this reaction takes effect at the resource and effect is observed by the user/controller
- Feedback delay can compromise stability!!**
 - The process may be reacting to some past condition that is no longer true

System Models

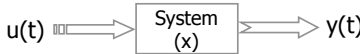


- Deterministic vs. Stochastic**
 - Are stochastic effects (noise, uncertainties) taken into account?
- Time-invariant vs. Time-varying**
 - Do system parameters change over time?
- Continuous-time vs. Discrete-time**
 - Is time divided into discrete-time steps?
- Linear vs. Non-linear**
 - Do dynamic equations contain non-linear terms?

System Modeling

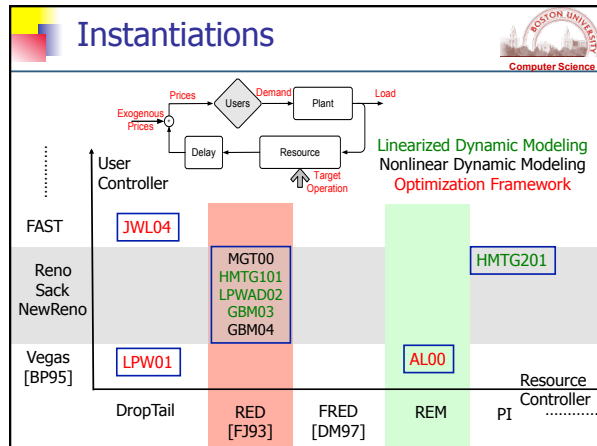


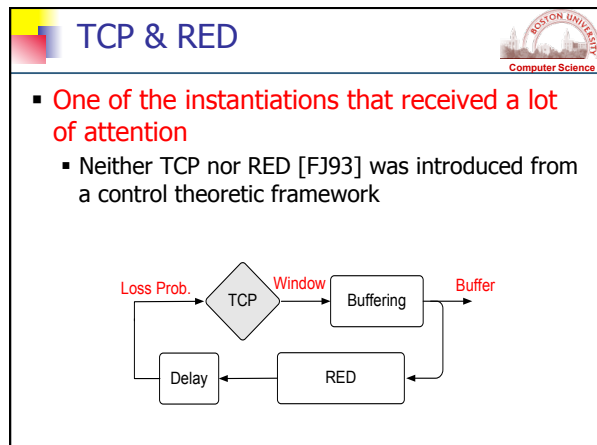
- Characterize the relationships among system variables as a function of time

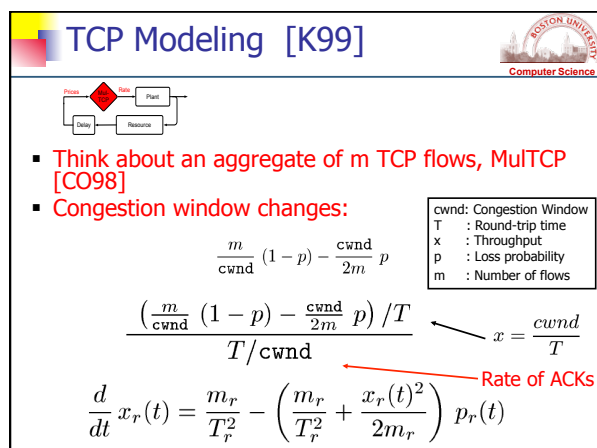


$$\begin{cases} \dot{x} = f(x, u) \\ y = h(x, u) \end{cases}$$

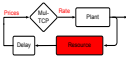
In general, f and h are nonlinear functions







TCP Modeling [K99]



- Depending on the total traffic passing through a resource, a congestion signal is generated with probability:

$$\mu_j(t) = p_j \left(\sum_{s:j \in s} x_s(t) \right)$$

$$\frac{d}{dt} x_r(t) = \frac{m_r}{T_r^2} - \left(\frac{m_r}{T_r^2} + \frac{x_r(t)^2}{2m_r} \right) p_r(t)$$

$p_r(t) = \sum_{j \in r} \mu_j(t)$

TCP-Reno Utility Function

$$\frac{d}{dt} x_r(t) = \frac{m_r}{T_r^2} - \left(\frac{m_r}{T_r^2} + \frac{x_r(t)^2}{2m_r} \right) p_r(t)$$

- For $m=1$ and small p , we have:

$$\frac{d}{dt} x(t) = \frac{1}{T^2} - \frac{x(t)^2}{2} p$$

$$\frac{d}{dt} x(t) = \frac{x(t)^2}{2} \left(\frac{2}{T^2 x(t)^2} - p \right)$$

$$\dot{U}(x) = \frac{2}{T^2 x(t)^2}, \quad U(x) = \frac{-2}{T^2 x}$$

Min potential delay allocation

E2E Congestion Avoidance TCP Vegas

- End-to-end, dynamic window, implicit
- Expected throughput = $\text{transmission_window_size} / \text{propagation_delay}$
- Numerator: known
- Denominator: measure *smallest* RTT
- Also know *actual* throughput, measure it every RTT
- Difference = how much to reduce/increase rate
- New Congestion Avoidance Algorithm
 - $(\text{expected} - \text{actual}) * \text{RTT}$ packets in bottleneck buffer
 - adjust sending rate *linearly* if this is too large or too small
- Generally loses to TCP Reno!

TCP-Vegas Utility Function

At steady state:

$$x = \frac{\alpha D}{T_q}$$

$$T_q = \frac{b}{C}, \dot{b}(t) = \frac{\dot{b}(t)}{C} = \frac{1}{C}(y(t) - C), T_q = \text{price}$$

$$\dot{U} = \frac{\alpha D}{x}, U = \alpha D \log(x) \quad \text{WPF allocation}$$

RED Modeling

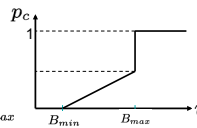
Buffer evolution

$$\dot{b}(t) = \sum x(t) - C$$

RED averaging

$$\dot{v}(t) = -\beta C(v(t) - b(t))$$

RED marking

$$p_c(t) = \begin{cases} 0 & v(t) \leq B_{min} \\ \sigma(v(t) - \varsigma) & B_{min} < v(t) < B_{max} \\ 1 & v(t) \geq B_{max} \end{cases}$$


RED Pricing Function

Assume linear function of instantaneous queue length: $p(t) = K q(t)$


$$\dot{p}(t) = K \dot{q}(t)$$

$$\dot{q}(t) = y(t) - C$$

$$\dot{p}(t) = K(y(t) - C)$$

p = Lagrangian multiplier (price)

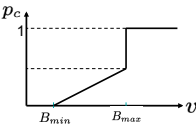
Nonlinear Models



- **Sources of nonlinearity**
 - Nonlinear components
 - Example: Rate Controlled MultTCP


$$\frac{d}{dt} x_r(t) = \frac{m_r}{T_r^2} - \left(\frac{m_r}{T_r^2} + \frac{x_r(t)^2}{2m_r} \right) p_r(t)$$

- Different operating regions
 - Example: RED

$$p_c(t) = \begin{cases} 0 & v(t) \leq B_{min} \\ \sigma(v(t) - \varsigma) & B_{min} < v(t) < B_{max} \\ 1 & v(t) \geq B_{max} \end{cases}$$



- **Hard Nonlinearities**
- **Soft Nonlinearities**

Nonlinear Models




- **Nonlinear control theory deals directly with nonlinear differential equations**
 - Stability: Lyapunov functions
 - Transient Response: Numerical solutions
- **Sometimes it gets very complicated**
- **Linearization:** Process of transforming a nonlinear set of equations into a linear set of equations around a single point of operation

Linearization



$$\begin{aligned} \dot{x} &= f(x, u) \\ y &= h(x, u) \end{aligned}$$


Linearization
 around x_0

$$\begin{aligned} \dot{x} &= Ax + Bu \\ y &= Cx + Du \end{aligned}$$

- **Concerned with local stability**
- **Assumes a single operating point**
 - Studies perturbations around this point
- **Expands the nonlinear DE into Taylor series, then ignores high-order terms**

Linear Models

Computer Science

- Once we have a Linear Model
 - Apply classical (first-course) control theory
- See Control Theory Primer slides & notes

Linear vs. Nonlinear

Computer Science


- **Linear Control**
 - Rely on “small range of operation” assumption
 - Simple to use
 - Has a unique equilibrium point (if stable)
 - Satisfies the superposition property
- **Nonlinear Control**
 - Wide range of operation
 - Could be more complex to use
 - Multiple equilibrium points may exist
 - Most control systems are nonlinear

Nonlinear Model of Sources' and Network's Adaptations

Computer Science

- **Kelly's optimization framework**
 - Maximize users' utilities subject to the network's capacity constraints [K99]

$$\frac{d}{dt} x_r(t) = \kappa \left(\underbrace{w_r - x_r(t)}_{\text{Additive Increase}} \underbrace{\sum_{l \in r} p_l \left(\sum_{s \in l} x_s(t) \right)}_{\text{Multiplicative Decrease}} \right)$$




Steady-state and stability

- Steady state
 - Set the derivatives to 0, we get the steady-state point(s)
 - We have a single equilibrium point here

$$\frac{d}{dt} x_r(t) = \kappa \left(w_r - x_r(t) \sum_{l \in r} p_l \left(\sum_{s: l \in s} x_s(t) \right) \right) \Rightarrow x_r = \frac{w_r}{\sum_{j \in r} \mu_j}$$

- Stability
 - Provided through a Lyapunov function

$$\mathcal{U}(x) = \sum_{r \in R} w_r \log x_r - \sum_{j \in J} C_j \left(\sum_{s: j \in s} x_s \right) \quad \frac{d}{dy} C_j(y) = p_j(y)$$



Lyapunov


- Scalar function, strictly convergent
- Finding a function guarantees stability
- Not finding a function, doesn't say anything
- Art to find one

$$\frac{\partial}{\partial x_r} \mathcal{U}(x) = \frac{w_r}{x_r} - \sum_{j \in r} p_j \left(\sum_{s: j \in s} x_s \right)$$

$$\frac{d}{dt} \mathcal{U}(x(t)) = \sum_{r \in R} \frac{\partial \mathcal{U}}{\partial x_r} \cdot \frac{d}{dt} x_r(t)$$

$$= \sum_{r \in R} \frac{\kappa_r}{x_r(t)} \left(w_r - x_r(t) \sum_{j \in r} p_j \left(\sum_{s: j \in s} x_s(t) \right) \right)^2 > 0$$


(except at steady-state)



Difficult road ahead...

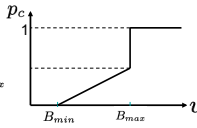
- Coming up with Lyapunov functions, even for simple models, is not easy
- As we move towards
 - More sophisticated models
 - Feedback delay
 - Different regions/aspects of TCP
 - Timeouts
 - Slow-start
 - Self-clocking
 - Challenging environments
 - High bandwidth-delay product networks
 - Effect of exogenous losses (e.g., wireless)
 - Accounting for different AQM at the resources
 - Interference processes as in DoS attacks
- It gets harder very quickly

Linear Models




Computer Science

- **Many sources of nonlinearity**
 - Nonlinear components
 - Example:
$$\frac{d}{dt} x_r(t) = \frac{m_r}{T_r^2} - \left(\frac{m_r}{T_r^2} + \frac{x_r(t)^2}{2m_r} \right) p_r(t)$$
- Different operating regions
 - Example: RED

$$p_c(t) = \begin{cases} 0 & v(t) \leq B_{min} \\ \sigma(v(t) - \varsigma) & B_{min} < v(t) < B_{max} \\ 1 & v(t) \geq B_{max} \end{cases}$$


- Need to study every point/region separately

Linearization



Computer Science

- **Concerned with local stability**
- **Assumes a single operating point**
 - Studies perturbations around this point
- **Expands the nonlinear DE into Taylor series, then ignores high-order terms**
 - Example: aggregating all sources and assuming one resource in


$$\frac{d}{dt} x_r(t) = \kappa \left(w_r - x_r(t) \sum_{l \in r} p_l \left(\sum_{i \in s} x_s(t) \right) \right)$$

$$\frac{d}{dt} x(t) = \kappa(w - x(t)p(x(t))) = f(x(t))$$

$$\frac{d}{dt} f(t) = -\kappa(p + p'x)f(t), \quad f(t) = x(t) - x$$

\downarrow
 $\frac{d}{dx(t)} f(t) \big|_{x(t)=x}$

Control Theoretic Analysis



Computer Science

- **Linearized Model**

$$\frac{d}{dt} f(t) = -\kappa(p + p'x)f(t), \quad f(t) = x(t) - x$$
- **Taking the Laplace Transform**

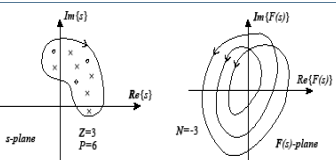
$$sF(s) - f(0) = -\kappa(p + p'x)F(s)$$

$$F(s) = \frac{f(0)}{s + \kappa(p + p'x)}$$
- **Stable if** $s = -\kappa(p + p'x) < 0$ **(overdamped)**
- **For impulse perturbation, steady-state error =**
 $\lim_{s \rightarrow 0} sF(s) = \text{zero}$

How about feedback delay?

- What if the system has feedback delay T ?
- Use Nyquist stability criterion ...

Cauchy's Principle



- Z : number of zeros of $F(s)$
- P : number of poles of $F(s)$
- N : number of encirclements of origin
- For $G(s)H(s)$, and contour around right-hand s -plane,
 - N : encirclements around -1
 - P : number of unstable poles of GH
 - Z : number of unstable zeros of $F = \text{closed-loop poles}$
 - If $P=0$, and $N=0$, then $Z=0$ and system is stable

Nyquist Test

- What if the system has feedback delay T ?
- If the plot of the open-loop $G(j\omega)H(j\omega)$ does not encircle the point -1 as ω is varied from $-\infty$ to $+\infty$, then the system is stable
- The number of unstable closed-loop poles (Z) is equal to the number of unstable open-loop poles (P) plus the number of encirclements (N) of the point $(-1, j0)$ of the Nyquist plot of GH , that is: $Z = P + N$

Nyquist Test

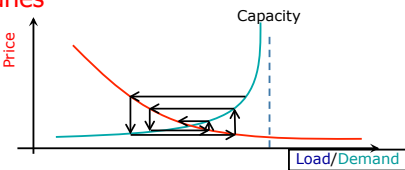
- What if the system has feedback delay T ?
- If the plot of the open-loop $G(j\omega)H(j\omega)$ does not encircle the point -1 as ω is varied from $-\infty$ to $+\infty$, then the system is stable
- Thus, we need to study the behavior of:

$$\frac{e^{-j\omega T}}{j\omega}$$
 as ω is varied
- Sufficient condition for stability:

$$\kappa T(p + p'x) < \pi / 2$$

Routing is also a dynamical system!


- Link price functions reflect prices fed back to routing as the load on the links varies




- Convergence and stability can be proved using Lyapunov functions

Lyapunov for Routing

- Need to show that mapping function is contractive, i.e., range of function reduces
- Consider an adaptive routing system over two paths, with “ N ” total traffic, and fraction α being re-routed based on path prices
- Find necessary condition for stability
- Show it is also sufficient




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