

CAS CS 585

# Image and Video Computing

0.5 Lecture by Margrit Betke

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Face Detection, Hierarchical Image Analysis,  
Motion Analysis by Image Differencing,  
Template Matching, SSD, NCC

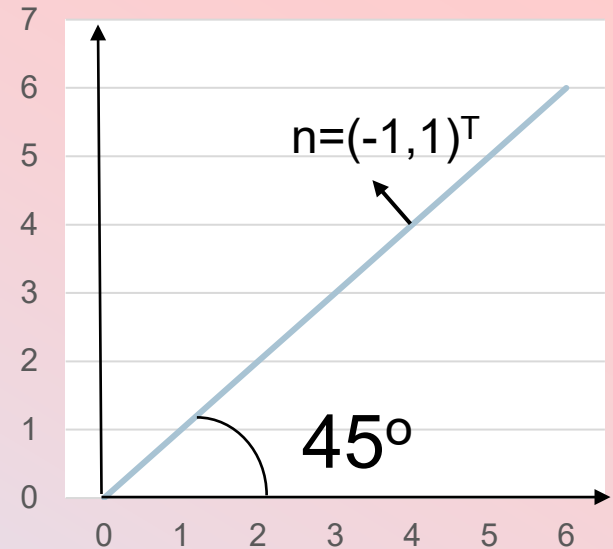
# Class Poll:

## Which line equation is wrong?



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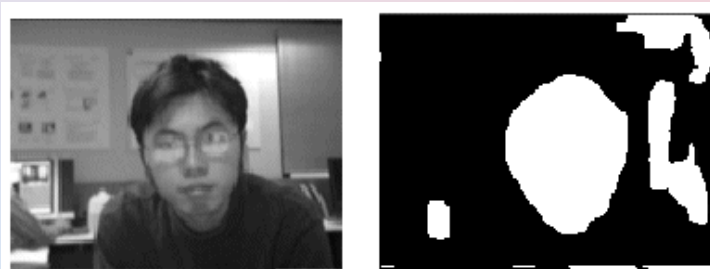
- A.  $y=mx+n$ , where  $m=1$ ,  $n=0$
- B.  $(-1,1)^T \mathbf{x} - g = 0$ , where  $g=\sqrt{2}$
- C.  $-x \sin \alpha + y \cos \alpha = 0$ , where  $\alpha = 45$  degrees
- D.  $(-\sin \pi/4, \cos \pi/4)^T \mathbf{x} = 0$



# Finding the Head and its Movement by Detecting Pixels with Skin Color



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Hope:

Largest skin color  
“blob” is face.

Fewer false positive  
skin pixels in  
background, e.g.,  
wooden door.

# Finding the Head and its Movement by Detecting Pixels with Skin Color



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(a) Input

(b) Color

*Common Trick in  
Computer Vision:*

Use

“**image pyramid**” = input image at difference scale.

Here: 6 levels, reduction in  $x, y$  by  $\frac{1}{4}$  (other schemes possible)

Then process result pyramid. Why?

# Finding Movement by Detecting Pixels with Brightness Changes



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(a) Input



(c) Motion

□  $DifferenceImage(x,y,t) = Image(x,y,t) - Image(x,y,t-1)$

□ Or  
 $DifferenceImage(x,y,t) = Image(x,y,t) - Image(x,y,t-k)$   
where  $k > 1$ , e.g., 10

□ Or  
 $DifferenceImage(x,y,t) = |Image(x,y,t) - Image(x,y,t-k)|$

Why absolute value?

# Finding the Face and its Movement by Locating the Best Match of a Face Template



Computer Science



(a) Input



Better matches shown brighter  
Best match: Blue pixel

# Finding the Face and its Movement by Locating the Best Match of a Face Template



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Use Jingbin's face as a template



Visualization  
of Match Values

How can we compute a match?

# Template Matching with Sum-Squared Difference (SSD)



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- ❑ *Scene subimage  $s$ , template image  $m$*
- ❑ *same size images =  $n$  pixels*
- ❑  *$s_i$  =  $i$ th pixel in subimage of scene*
- ❑  *$m_i$  =  $i$ th pixel in template image  $m$*
  
- ❑  $SSD = \sum_{(i=1 \text{ to } n)} (s_i - m_i)^2$
  
- ❑ *Template matching = **exhaustive search algorithm** for position of scene subimage that best matches the template (where SSD is smallest)*

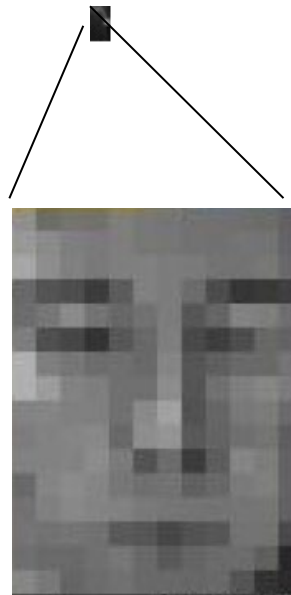


# Finding the Face and its Movement by Locating the Best Match of a Face Template



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Used average face as a template



Visualization of Match Values

# Normalized Correlation Coefficient (NCC)



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Paired pixels in image X and Image Y:

$$\{(x_1, y_1), \dots, (x_n, y_n)\}$$

Definition of NNC:

$$r_{xy} = \frac{\sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\sum_{i=1}^n (x_i - \bar{x})^2} \sqrt{\sum_{i=1}^n (y_i - \bar{y})^2}}$$

where the mean for the image X pixel values is

$$\bar{x} = \frac{1}{n} \sum_{i=1}^n x_i$$

The mean for Y is defined similarly.

The NCC is also called “Pearson coefficient.” Pearson was not the inventor. He is known for eugenics and scientific racism, so we will not use his name to describe the NCC in CS 585.

# Template Matching via with Normalized Correlation



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- ❑ Scene subimage  $s$ , template *image*  $m$

- ❑ *Normalized correlation coefficient*

$$r = 1/n \sum_i ((s_i - \text{mean}(s)) * (m_i - \text{mean}(m)) / (\sigma_s \sigma_m)) \text{ where}$$

$s_i$  and  $m_i$  are respective brightness values of the  $i$ th pixel  
 $\text{mean}(m)$  and  $\sigma_m$  are mean and standard deviation of all pixels in the template

$\text{mean}(s)$  and  $\sigma_s$  are mean and standard deviation of all pixels in the subimage of the scene

- ❑ Template matching = exhaustive search for position of subimage that produces highest  $r$

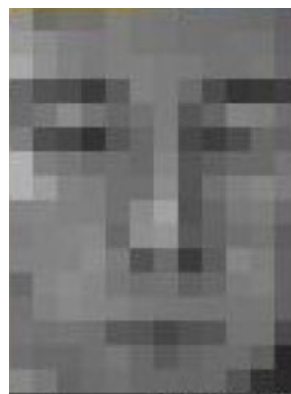
- ❑  $r$  can be between -1 and 1

# Finding the Face and its Movement by Locating the Best Match of a Face Template



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Used average face as a template



Visualization  
of Normalized  
Correlation  
Coefficient  
Match Values

# Finding the Face with Template Matching & the Normalized Correlation Coefficient



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(a) Input



(d) Correlation

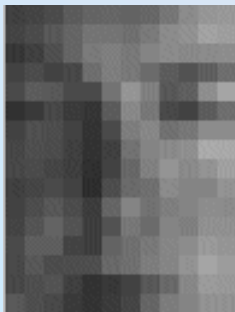
# Multi-Resolution Matching



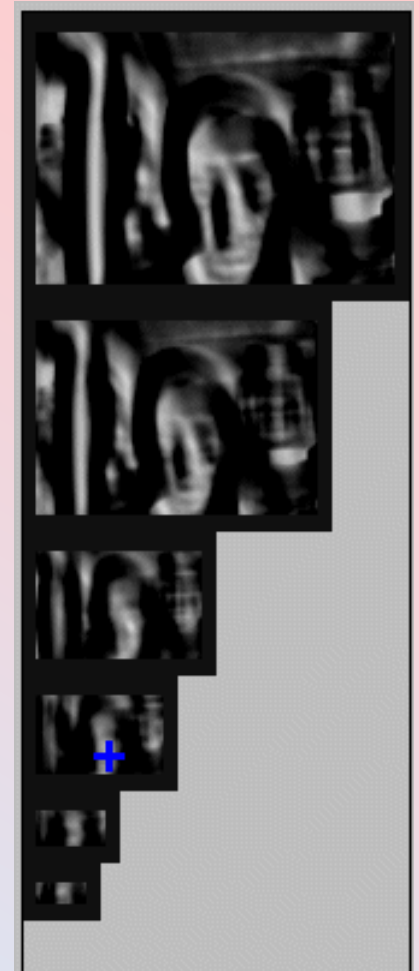
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Normalized correlation coefficient over multi-resolution search space:

$$r = \frac{1/n \sum_i (s_i - \text{mean}(s)) (m_i - \text{mean}(m))}{(\sigma_s \sigma_m)}$$



← Template  
matched over all  
resolutions →



# Finding the Face and its Movement by Locating the Best Match of a Face Template



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(a) Input

You can apply template matching to a small version of your input image and use that search result to start searching for a match in the 2<sup>nd</sup> smallest images. Repeat until the original size is processed.



(d) Correlation

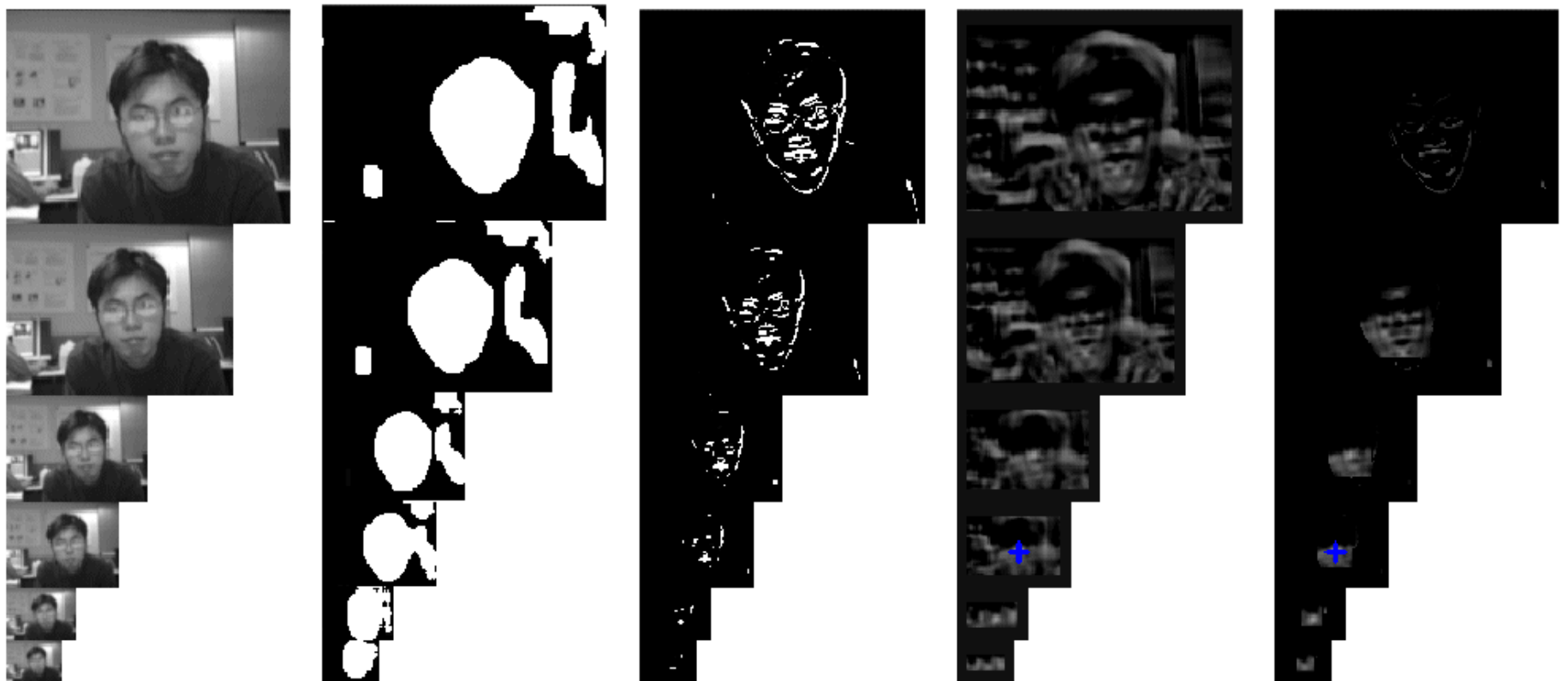


# Multi-scale Pyramids



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Combine the results of color and motion detection to mask the regions of interest for correlation-based template matching



(a) Input

(b) Color

(c) Motion  
(low-pass filter)

(d) Correlation

(e) Masked  
Correlation



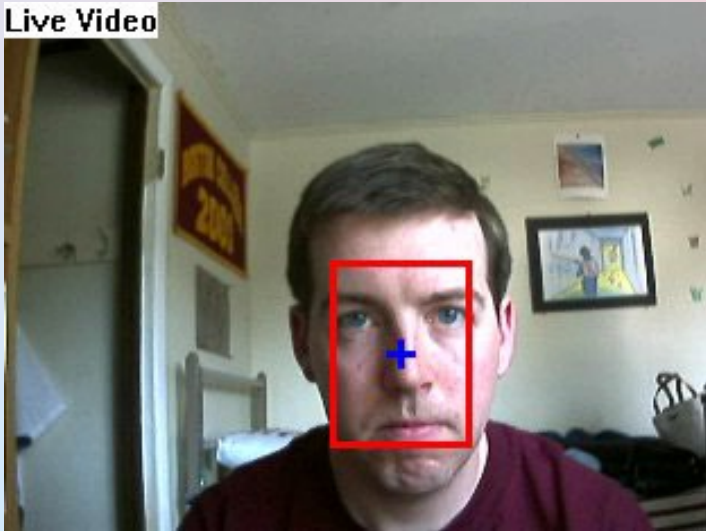
# Face Detection



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## Data Variability

Live Video

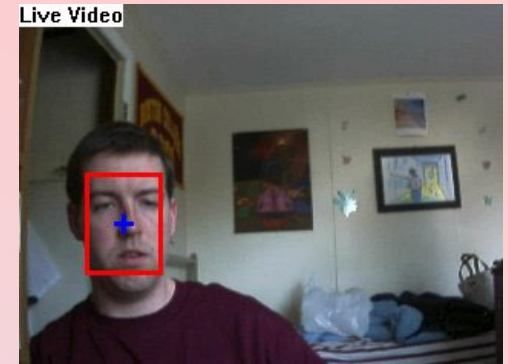


Live Video



Large Face

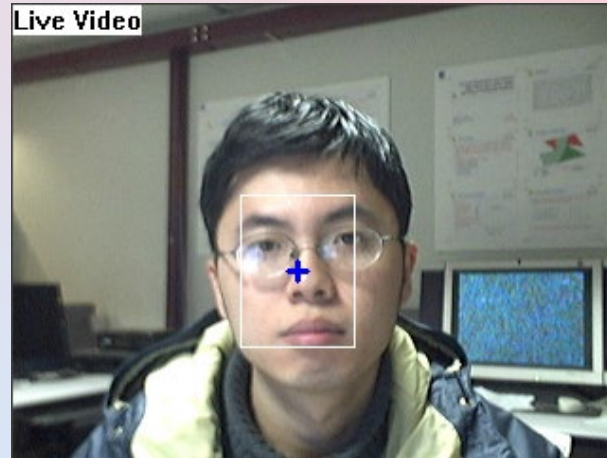
Live Video



Small Face

Shadows  
Cluttered background

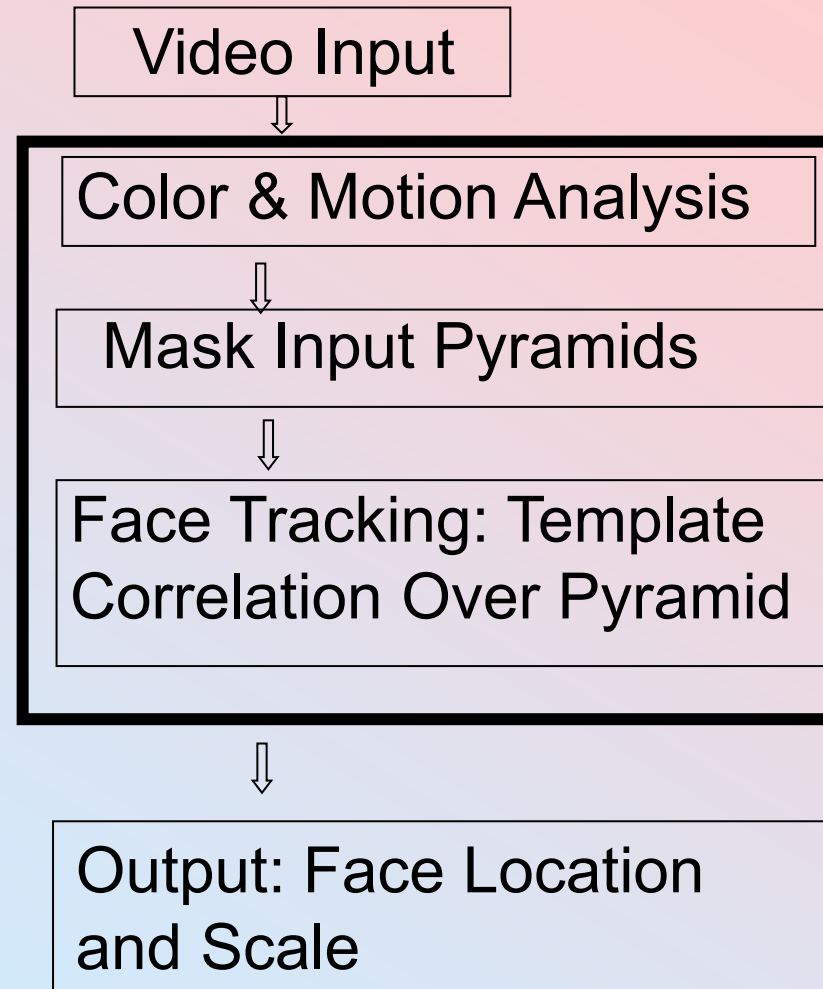
Live Video



# Algorithm: Multi-scale Face Detection



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# Face Detection Interface



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EyeMouse  
Control Show Train

**Live Video**

**B&W Video**

**Motion**

**Color**

**Correlation**

Scale: 6; Location: (136, 136)

The interface displays a central 'Live Video' window showing a man in a yellow shirt with a white bounding box around his face and a blue crosshair on his nose. To the right is a 'B&W Video' window showing the same scene in grayscale. Below the live video are three smaller windows: 'Color' showing a high-contrast, thresholded version of the face, 'Motion' which is mostly black, and 'Correlation' showing a grayscale correlation map. At the bottom, the text 'Scale: 6; Location: (136, 136)' indicates the detected face's parameters.

Live Video



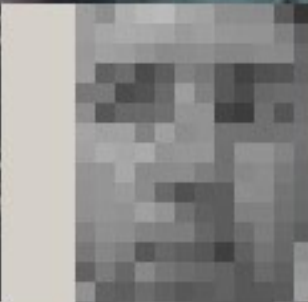
B&W Video



Motion



Color



Correlation

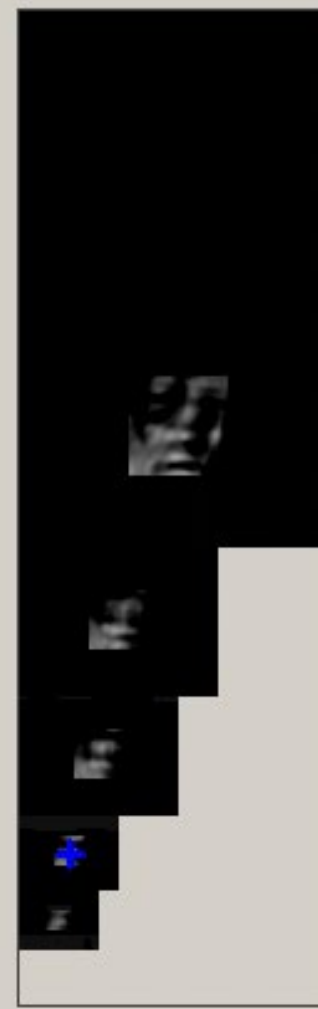


Max Score: 193; Scale: 6; Location: (160, 120)

OK

Cancel

Pyramid Display



Close



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# Learning Objectives



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Can explain and apply to image analysis problems:

- ❑ Detection by Color Analysis
- ❑ Hierarchical Image Analysis
- ❑ Motion Analysis by Image Differencing
- ❑ Sum-squared Difference (SSD)
- ❑ Normalized Correlation Coefficient (NCC)
- ❑ Template Matching with SSD or NCC