CS 512 Formal Methods, Spring 2018	Instructor: Assaf Kfoury
CTL Examples	
February 15, 2018	Shreya Ramesh

(These lecture notes are **not** proofread and proof-checked by the instructor.)

### 1 Detailed solution for Assignment 3, Problem 1, Part e

Part e formula:  $\varphi \triangleq (\bigcirc (a \land b) \land \diamond (\neg a \land \neg b))$ Here,  $AP = \{a, b\}.$ 

### 1.1 Part i

We can split up the formula into subformulas as follows:

- $a \wedge b$  evaluates to  $q_4$ .
- $\bigcirc q_4$  evaluates to  $q_3$ . Therefore the left side of the formula evaluates to the  $\omega$ -regular expression  $(q_3q_4)^+q_3$ .
- $\neg a \land \neg b$  evaluates to  $q_1$ .
- $\diamond q_1$  evaluates to  $(q_3q_4)^*q_3q_1q_2^{\omega}$ .
- Now, because of the  $\wedge$  we need to find the common terms between the left and right paths. This ends up being  $(q_3q_4)^+q_3q_1q_2^{\omega}$ .

### 1.2 Part ii

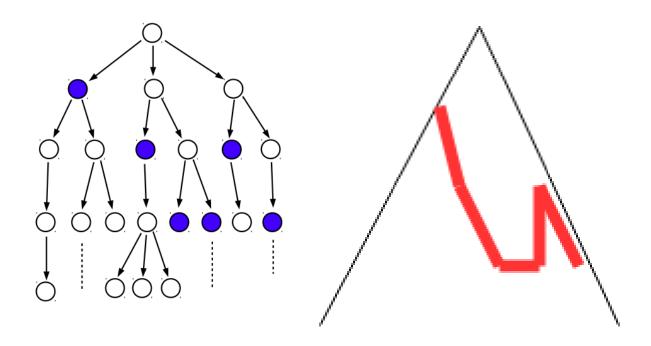
• No, because the path  $q_3 q_2^{\omega}$  is missing.

# 2 Example of visualization of behavior of temporal connectives (Based on Handout 11)

Consider the example where AP = p, q.

- An empty node can be denoted as  $\bar{p}\bar{q}$ .
- A blue node can be denoted as  $p\bar{q}$ .
- A red node can be denoted as  $\bar{p}q$ .

Below is another way of visualizing the constraint  $\forall \diamond p$ , which can be translated as "for all eventually". The cross section in the image below denotes the point where p is eventually entered in the path.



## 3 Algorithm for CTL Model Checking (Handout 13)

A useful technique for reducing/simplifying transition systems is to pre-process. For example, consider all the sub-WFFs of  $\Phi$ . Consider sub-WFF  $\varphi_0$ . By deleting all the states where  $\varphi_0 =$  false, we can potentially greatly reduce the space of our transition system, and make the problem simpler.

## 4 Dining Philosophers Problem represented in CTL

Assume  $AP = \{e_1, f_1, e_2, f_2, \dots, e_5, f_5\}$  where  $e_i$  means philospher i is eating and  $f_1$  means philosopher i is finished eating.

- Better way of writing Property 2 on Handout 12, page 4:  $\forall ((\neg e_1 \land \neg e_3 \land \neg e_4 \land \neg e_5) \sqcup e_2)$
- Property 4 on Handout 12, page 4 is an example of the liveness property.