

EUROCRYPT'17
Paris, May 2017

an IETF standard for

Verifiable Random Functions (VRF)

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hash function zoo

hash function:

- no key
- hash = **H**(input)
- Verify: Check hash = **H**(input)

SHA256

BLAKE

hash function zoo

hash function:

SHA256

- no key
- hash = $H(\text{input})$
- Verify: Check hash = $H(\text{input})$

BLAKE

pseudorandom function:

HMAC

- symmetric key k
- hash = $H(k, \text{input})$
- Verify: Cannot without k

hash function zoo

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SHA256

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pseudorandom function:

HMAC

- symmetric key **k**
- hash = **H**(**k**, input)
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verifiable random function (VRF):

- asymmetric key pair (**SK**, **PK**)
- hash = **VRF_hash**(**SK**, input)
- Verify: Use **PK**

hash function zoo

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- hash = $H(\text{input})$
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SHA256

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pseudorandom function:

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verifiable random function (VRF):

- asymmetric key pair (SK, PK)
- hash = $VRF_hash(SK, \text{input})$
- Verify: Use PK

First proposed by
Micali-Rabin-Vadhan
1999

VRF: verifiable random function

Verifier **PK**

Hasher
SK

VRF: verifiable random function

Verifier **PK**

Hasher **SK**



VRF: verifiable random function

Verifier **PK**

Hasher **SK**

input
→

hash = **hash**(**SK**, input)

proof = **prove**(**SK**, input)

VRF: verifiable random function

Verifier **PK**

Hasher **SK**

input
→

hash = **hash**(**SK**, input)

←
hash, proof

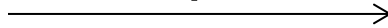
proof = **prove**(**SK**, input)

VRF: verifiable random function

Verifier **PK**

Hasher **SK**

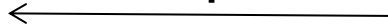
input



hash = **hash**(**SK**, input)

proof = **prove**(**SK**, input)

hash, proof



verify (**PK**, input, hash, proof)

VRF security: uniqueness and collision-resistance

Verifier **PK**

Hasher **SK**



input



hash = **hash**(**SK**, input)

proof = **prove**(**SK**, input)

hash, proof



verify (**PK**, input, hash, proof)

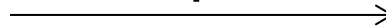
VRF security: uniqueness and collision-resistance

Verifier **PK**

Hasher **SK**



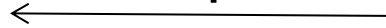
input



hash = **hash**(**SK**, input)

proof = **prove**(**SK**, input)

hash, proof



verify (**PK**, input, hash, proof)

Like any public hash function:

**output verifiably determined by input
and collisions hard to find**

VRF security: pseudorandomness

Verifier **PK**

Hasher **SK**

input
→

hash = **hash**(**SK**, input)

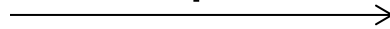
VRF security: pseudorandomness



Verifier **PK**

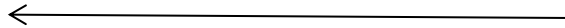
Hasher **SK**

input



hash = **hash**(**SK**, input)

hash but not proof



VRF security: pseudorandomness

Verifier **PK**



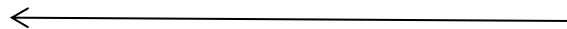
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hash = **hash**(**SK**, input)

hash but not proof



input-hash relationship
looks random
without the proof

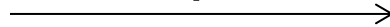
VRF security: pseudorandomness

Verifier **PK**



Hasher **SK**

input



hash = **hash**(**SK**, input)

hash but not proof



input-hash relationship
looks random
without the proof

Like a keyed hash function whose key you don't know

Why should you care?

VRFs Have:

- Collision Resistance (like hash functions)
- Uniqueness/Verifiability (like public hash functions)
- Pseudorandomness (like keyed hash functions)

**But why should we want
to standardize them?**

VRFs stop dictionary attacks on data structures

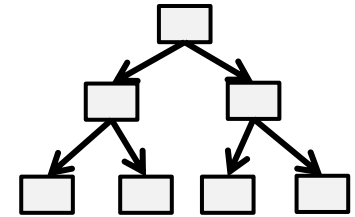
Verifier

Root of the
data structure



Prover

Authenticated
data structure



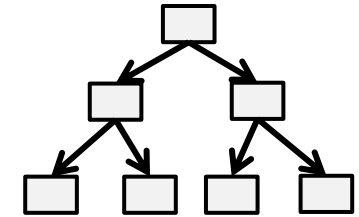
VRFs stop dictionary attacks on data structures

Verifier

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Root of the
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queries

responses



VRFs stop dictionary attacks on data structures

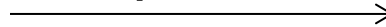
Verifier

Prover

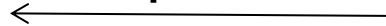
Root of the
data structure



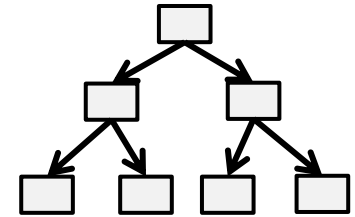
queries



responses



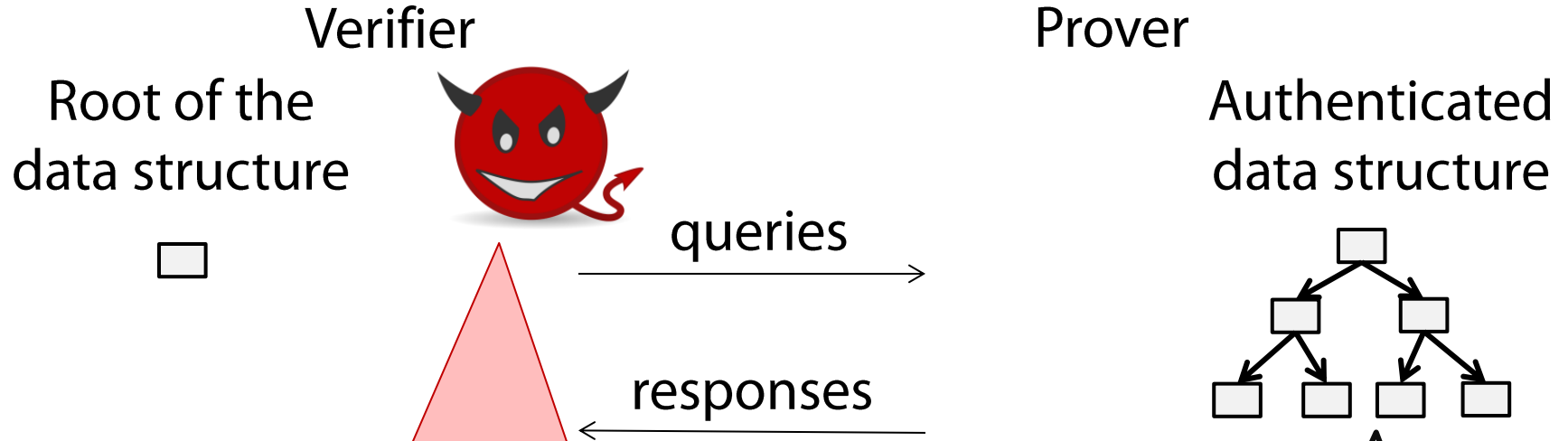
Authenticated
data structure



Problem:

can use dictionary attacks
to learn about data not queried

VRFs stop dictionary attacks on data structures



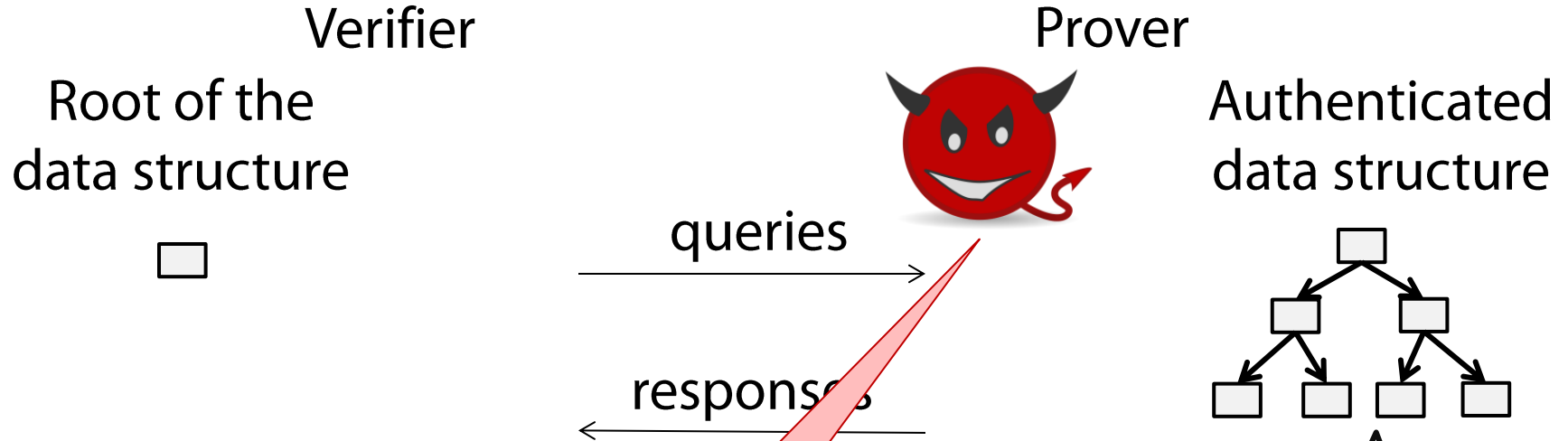
Problem:

can use dictionary attacks to learn about data not queried

Solution:

store VRF hashes of data instead of actual data.
VRF pseudorandomness \Rightarrow verifier learns nothing extra

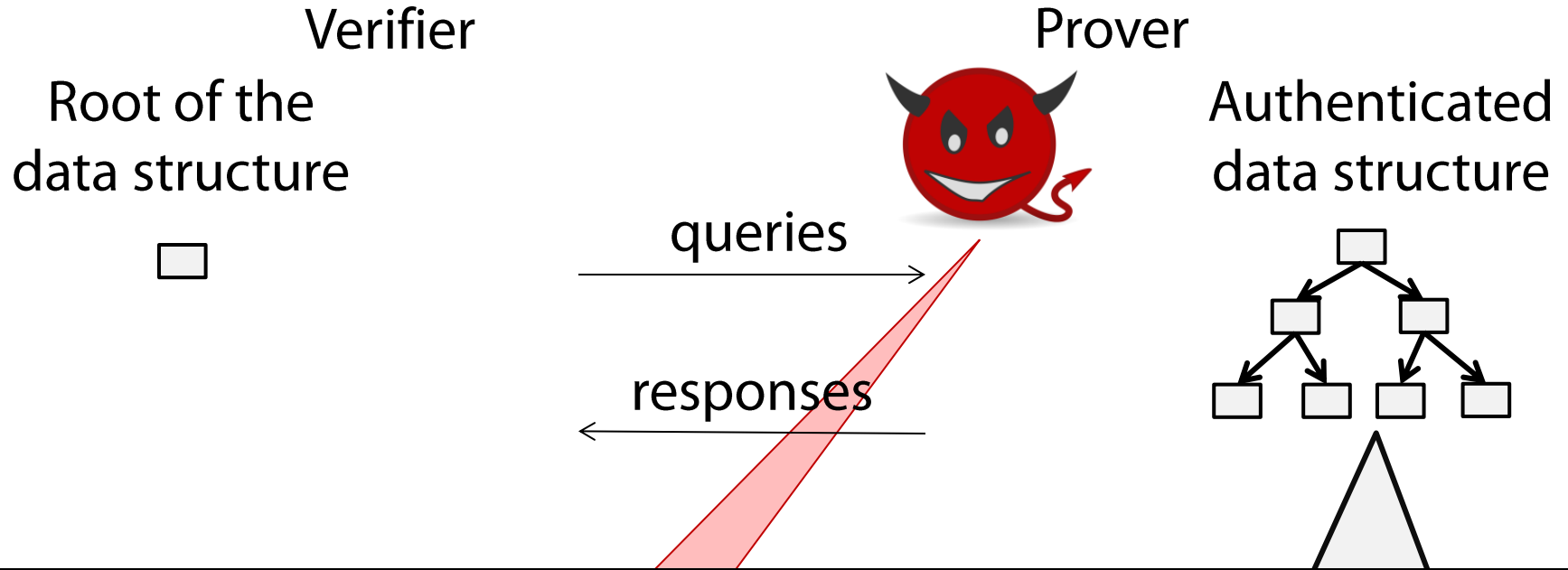
VRFs stop dictionary attacks on data structures



Because of VRF uniqueness, prover still can't lie about the data.

Solution:
store VRF hashes of data instead of actual data.
VRF pseudorandomness \Rightarrow verifier learns nothing extra

VRFs stop dictionary attacks on data structures



Useful for:

- **DNSSEC (NSEC5 denial of existence)**
- **Certificate transparency**
- **End-user key verification (CONIKS)**
- **Cryptocurrencies**

If interested in standardizing VRFs,

please talk to us!

If you use VRFs,

please talk to us!

Draft is out at

<https://tools.ietf.org/html/draft-goldbe-vrf-00>

(working through saag and cfrg)

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